

# Accelerating IISPH 

A parallel GPGPU solution using CUDA

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This thesis is submitted to the Faculty of Computing at Blekinge Institute of Technology in partial fulfillment of the requirements for the degree of Master of Science in Game and Software Engineering. The thesis is equivalent to 20 weeks of full time studies.

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## Abstract

Context. Simulating realistic fluid behavior in incompressible fluids for computer graphics has been pioneered with the implicit incompressible smoothed particle hydrodynamics (IISPH) solver. The algorithm converges faster than other incompressible SPH-solvers, but real-time performance (in the perspective of video games, 30 frames per second) is still an issue when the particle count increases.
Objectives. This thesis aims at improving the performance of the IISPH-solver by proposing a parallel solution that runs on the GPU using CUDA. The solution should not compromise the physical accuracy of the original solution. Investigated aspects are execution time, memory usage and physical accuracy.
Methods. The proposed implementation uses a fine-grained approach where each particle is calculated on a separate thread. It is compared to a sequential and a parallel OpenMP implementation running on the CPU.
Results and Conclusions. It is shown that the parallel CUDA solution allow for real-time performance for approximately 19 times the amount of particles than that of the sequential implementation. For approximately 175000 particles the simulation runs at the constraint of real-time performance, more particles are still considered interactive. The visual result of the proposed implementation deviated slightly from the ones on the CPU.

Keywords: implicit incompressible smoothed particle hydrodynamics, fluid simulation, real-time, GPGPU

## Preface

## Acknowledgment

We would like to thank Prashant Goswami for the proposed research area and his invaluable knowledge and help.

We would also like thank fellow student Mattias Frid Kastrati for giving feedback and proof-reading our thesis.

Finally we would like to thank our peers who gave us valuable feedback with their oppositions.

## About abbreviations

Throughout this thesis certain terms are abbreviated to ease reading. At the first occurrence they are written in full (except from units, such as MB). They are also listed below.

AoS - Array of Structs
API - Application Programming Interface
EOS - Equation Of State
FPS - Frames Per Second
GPGPU - General-Purpose computing on Graphics Processing Unit
ISPH - Incompressible Smoothed Particle Hydrodynamics
IISPH - Implicit Incompressible Smoothed Particle Hydrodynamics
PCISPH - Predictive-Corrective Incompressible Smoothed Particle Hydrodynamics
PPE - Pressure Poisson Equation

PSNR - Peak Signal-to-Noise Ratio
SPH - Smoothed Particle Hydrodynamics
SoA - Structure of Arrays
SSIM - Structured Similarity Index Measure

VRAM - Video Random Access Memory
WCSPH - Weakly Compressible Smoothed Particle Hydrodynamics

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## Chapter 1

## Introduction

Fluids are common elements included in the environments of video game worlds. The behavior of them can be achieved with various techniques, such as animating a height-map. This technique is limited to only simulate the surface of the fluid however and require additional methods for water splashes and sub-surface simulation. To simulate the entire body of a fluid, alternative methods such as smoothed particle hydrodynamics (SPH) [1] can be used.

In video games, real-time performance is assumed to range between 30 to 60 or more frames per second (FPS) to ensure the player an acceptable experience [2]. This infers that the time between two consecutive frames may not exceed at the most 33 ms ; which includes the time to compute the scene of the frame and to render it on screen.

Implicit incompressible SPH (IISPH) is a state-of-art SPH-solver which allows for realistic fluid behaviors of incompressible fluids (such as water) [3]. In order for IISPH to be suitable for simulating fluids in games, it would need to meet the requirement for real-time performance. Other limiting factors would be interaction with game objects and computations to be completed within a given time-frame together with other logic, however this is out of the scope of this thesis.

With the increased use of general-purpose computing on GPU (GPGPU) for massive parallel data computation it is a logical strategy to implement IISPH to be run on the GPU to overcome the real-time performance barrier.

### 1.1 SPH based methods

In this section a brief description on how realistic fluid behavior can be achieved for computer graphics using particles and how it has been improved in terms of performance and compressibility.

### 1.1.1 Smoothed Particle Hydrodynamics

Realistic fluid simulations can be achieved with the SPH method where the fluid's body is represented as a set of particles. SPH uses various external forces, such
as gravity and viscosity, combined with internal pressure forces to calculate the velocities of the particles [1].

The pressure is computed with an equation of state (EOS). An EOS is an equation describing the physical state of a system according to a set of variables known as state variables which have an internal relationship with each other, such as mass, density and pressure. However, this pressure computation also results in forces which penalize compression [3].

SPH allows for easy boundary handling and mass conservation which can accomplish realistic movement and behavior, and effects such as water splashes. SPH is not without its limitations though. Restrictions such as a non-real-time performance [4] and an abundance of efficient incompressible SPH-solvers [3, 4, $5,6]$ render the method unsuitable in application areas such as video games.

### 1.1.2 Weakly Compressible SPH

Much work has been done to improve SPH in terms of visual quality and performance. Weakly compressible SPH (WCSPH) [7] utilizes a stiff EOS in order to address compressibility. Density fluctuations are kept low by assuming a high speed of sound in the medium. Though the computations of SPH and WCSPH are inexpensive per frame, compared to alternative approaches [3]; a higher stiffness requires smaller time-steps (time simulated between two frames) in the physics simulation, which results in that the total number of frames required for a given time-frame increases when compressibility decreases.

### 1.1.3 Incompressible SPH

It was suggested that by solving a pressure projection equation similar to the Eulerian methods [8], rather than the EOS in SPH and WCSPH, an enforcement of incompressibility could be achieved. Then by projecting either the intermediate velocity field [9] or the variation of particles' density [10] onto a divergence-free space, incompressibility can be enforced through a pressure Poisson equation (PPE). Incompressible SPH (ISPH) allows for use of larger time-steps but at an expense of additional computation cost per time-step (frame).

### 1.1.4 Predictive-Corrective Incompressible SPH

Further improvements suggest predictor-corrective schemes to combine the advantage of large time-steps from the ISPH method with WCSPH's low computation cost per time-step. The predictive-corrective incompressible SPH (PCISPH) [6] method is such an approach which utilizes a predictor-corrective scheme of the EOS. The velocity of the particle is predicted based on previous velocity and then corrects it based on the new pressure. It is an iterative process that repeats its process for as long as the density error is above a specified user-defined threshold
(e.g. if the error margin is within $0.1 \%$ deviation from the rest density). PCISPH outperforms WCSPH in terms of performance in regard to incompressibility with as much as a factor of 55 while approaching incompressibility as well.

### 1.1.5 Local Poisson SPH

An alternative approach to combine the advantages of WCSPH and ISPH was proposed by He et al. [11] with Local Poisson SPH. The PPE is solved by converting the differential PPE to a continuous integral. A discretization method is used to convert this form to a discretized summation in the local pressure integration domain for all particles. The pressure solver is then integrated into a predictive-corrective framework. The result was improvements in both density error and convergence rate of the solver, rivaling the performance of PCISPH.

### 1.1.6 Implicit Incompressible SPH

Another discretization of the PPE was proposed by Ihmsen et al. [3] with IISPH, which is an improvement of the PCISPH-method. An issue with traditional ISPHsolvers is that they do not scale well with large-scale scenarios comprising of millions of particles. IISPH gained a significant speed-up compared to ISPH and PCISPH as a result of a discretization of the PPE, reportedly a speed-up factor of 6.2 and 5.2 times compared to PCISPH for two different scenarios. This resulted in a performance that scaled better with large-scale scenarios while further enforcing incompressibility.

Any further details of the algorithm are being referred to chapter 4.

### 1.2 Problem

Incompressible SPH-solvers addressed the issue with incompressibility in the fluid. It was further improved with the implementation of the state-of-the-art incompressible SPH-solver IISPH [3]. However, because of it being a sequential implementation running on the CPU, there is still a gap in performance. IISPH cannot by itself be considered a feasible solution for fluid simulations in real-time applications. As a consequence this severely limits the utility of IISPH in certain fields where real-time performance are considered important e.g. video games and virtual reality.

### 1.3 GPGPU and CUDA

The basics of GPGPU is to utilize the graphics card's processing units to compute general tasks. The three major application programming interfaces (APIs)
are NVIDIA ${ }^{\circledR}$ CUDA ${ }^{\circledR}{ }^{1}$ [21], Microsoft ${ }^{\circledR}$ Direct Compute and the Apple ${ }^{\circledR}{ }^{2}$ and Khronos ${ }^{\text {TM }}$ Group OpenCL ${ }^{\text {TM }}{ }^{3}$. These APIs allow programmers to utilize the GPU's computational power in areas where massive computations can be executed in parallel. This has resulted in increased performance of computationally heavy applications, such as in analyzing air traffic flows and visualizations of molecules [21].

CUDA was the chosen programming platform because of its computational power, its interoperability with Microsoft ${ }^{\circledR}$ DirectX ${ }^{\circledR}{ }^{4}$ rendering API and because of the project outline preferring CUDA. The supporting development languages are C, C++ and Fortran.

CUDA Toolkit 7.0 was used during the implementation and is distributed with supplementary libraries. Thrust [22] is one of those libraries and was originally created by Hoberock and Bell. Thrust is a parallel algorithms library with CUDA interoperability providing parallel implementations of basic algorithms such as sort, transform and reduce.

### 1.4 Thesis Outline

So far a brief introduction to fluid simulations with various SPH-solvers has been given as well as the problem and a short introduction of CUDA. In chapter 2 a more explanatory description of the problem and the research questions this thesis aims to answer are given. This is followed in chapter 3 by other related work that has aimed at similar areas as this thesis. The IISPH-algorithm is described in detail in chapter 4 and in chapter 5 the implementations of it are covered. Chapter 6 describes the methodology of the experiments with the results summarized in chapter 7 . This is followed by a discussion of what was achieved in chapter 8 and finally a short conclusion and future work in chapter 9 .

[^0]
## Chapter 2

## Aims, Objectives and Research Question

This thesis aims to improve the performance of the IISPH-algorithm by proposing a parallel implementation which can run on the GPU. The proposed algorithm was implemented and experimented on using CUDA and comparisons was made to a sequential and parallel CPU-implementation.

### 2.1 Objectives

To achieve this goal a set of sub-tasks was created to track the progress; of which some were required to be completed before others, whereas some could be done in parallel:

- Get accustomed to either the original or a reconstructed implementation of the proposed algorithm in [3]. Two reasons existed for this task:
- With the actual code available, a detailed study of the algorithm's nature could be acquired which alleviated the workload and understanding of it when proposing the parallel one.
- To evaluate the performance of the proposed parallel CUDA-implementation it was necessary to gather data and compare test results with a sequential as well as a parallel CPU-implementation in order to make any conclusions regarding the proposed CUDA-implementation.
- With the in-depth study, areas which could be beneficial of running in parallel was identified. Suitable methods of parallelization were proposed for one and each of the parts of the algorithm. If any part had been required to run sequentially it would had been of importance to identify it and decide whether it would cause problems or if it could have been solved with an alternative approach.
- Using the parallel proposal and the knowledge from the sequential CPUcode the CUDA-version was implemented.
- To see a visual representation of the simulations, rendering the particles was required. In the CPU-version the necessary particle data was sent to the GPU for rendering each frame. In the CUDA-version it was desirable to not have to copy this data from the GPU to the CPU and back again; thus connecting CUDA to DirectX to allow it to modify the buffers was desired.
- Creating appropriate scenarios to be run when measuring performance. Aspects such as the number of particles and the layout of test scene itself could be affecting the result.
- Suitable measurements were needed to evaluate two aspects in experiments using the scenarios. The performance in terms of execution time and the visual quality in terms of identical visual outcome were necessary to be examined.
- An analysis of the gathered data was made to evaluate whether a positive result had been achieved or if further improvements were necessary to achieve a sufficient result.


### 2.2 Research questions

This thesis aims to answer the following research questions:
RQ1. Is it possible to achieve real-time performance of IISPH using CUDA?

1. What sections of the algorithm are the most time consuming?
2. For how many particles can the proposed solution be considered realtime?

RQ2. Will a parallel implementation with CUDA achieve better performance than that of a parallel version on the CPU?

RQ3. Can IISPH gain increased performance utilizing a parallel implementation with CUDA but without compromising the physical accuracy?

## Hypothesis:

- It is believed that the memory usage between the implementations will be similar.


## Chapter 3

## Related Work

Various improvements have been proposed for CPU and GPU oriented approaches of SPH [12]. While some of these have already been covered in section 1.1, this chapter will focus on related parallelization and optimizations of SPH- and ISPHsolvers.

In this thesis the approach of parallelizing IISPH was by using a fine-grained (data parallelism) approach on the GPU. Each particle is run in parallel and they are themselves responsible for calculating their own values. An alternative coarse-grained (task parallelism) approach on the GPU is presented by Goswami et al. [13] which utilizes groups of particles using shared memory and CUDA. By dividing the particles into small groups and utilizing shared memory a significant performance increase of SPH was gained.

A recent study by Thaler et al. [14] shows a parallel multi-core implementation of IISPH with focus on a fine-grained approach with promising performance results, however without any information about how the visual results compare to a sequential implementation. In this thesis a similar algorithm structure is proposed; with variables being calculated in sections with synchronization in-between when necessary. In their multi-core solution it is necessary to communicate and balance the load efficiently between cores to fully utilize the cores capabilities.

Another shared memory approach with CUDA for PCISPH is presented by Nie et al. [15]. A good speed-up was achieved compared to both sequential and multi-core CPU-implementations. They also found that the sorting method for neighbor search to be a bottleneck and provide with a new parallel sorting method to increase performance. The implementation utilizes a structure of arrays (SoA) pattern for particle data due to better coalesced memory access which is crucial to maximize the bandwidth the GPU supports. Using a SoA pattern means that each variable is a separate array stored in a consecutive section of memory.

## Chapter 4

## IISPH

In this chapter an overview of the IISPH-algorithm will be given and details that may not be obvious will be addressed as well. Any details on the derivation of the algorithm are considered out-of-scope of the thesis and are being referred to the paper by Ihmsen et al. [3]. All equations and details in this chapter are cited from the same paper unless stated otherwise.

```
Algorithm 1: IISPH-algorithm proposed by Ihmsen et al. [3].
    Procedure ADVECTION PREDICTION
        foreach particle \(i\) do
            compute \(\rho_{i}(t)=\sum_{j} m_{j} W_{i j}(t)\)
            predict \(\mathbf{v}_{i}^{a d v}=\mathbf{v}_{i}(t)+\Delta t \frac{\mathbf{F}_{i}^{a d v}(t)}{m_{i}}\)
            \(\mathbf{d}_{i i}=\Delta t^{2} \sum_{j}-\frac{m_{j}}{\rho_{i}^{2}} \nabla W_{i j}(t)\)
        foreach particle \(i\) do
            \(\rho_{i}^{a d v}=\rho_{i}(t)+\Delta t \sum_{j} m_{j}\left(\mathbf{v}_{i j}^{a d v}\right) \nabla W_{i j}(t)\)
            \(p_{i}^{0}=0.5 p_{i}(t-\Delta t)\)
            compute \(a_{i i}(4.5)\)
    Procedure PRESSURE SOLVE
        \(l=0\)
        while \(\rho_{\text {avg }}^{l}-\rho_{0}>\eta \vee l<2\) do
            foreach particle \(i\) do
                \(\sum_{j} \mathbf{d}_{i j} p_{j}^{l}=\Delta t^{2} \sum_{j}-\frac{m_{j}}{\rho_{j}^{2}(t)} \nabla W_{i j}(t)\)
            foreach particle \(i\) do
                    compute \(p_{i}^{l+1}(4.8)\)
                \(p_{i}(t)=p_{i}^{l+1}\)
            \(l=l+1\)
    Procedure INTEGRATION
        foreach particle \(i\) do
            \(\mathbf{v}_{i}(t+\Delta t)=\mathbf{v}_{i}^{a d v}+\Delta t \frac{\mathbf{F}_{i}^{p}(t)}{m_{i}}\)
            \(\mathbf{x}_{i}(t+\Delta t)=\mathbf{x}_{i}(t)+\Delta t \mathbf{v}_{i}(t+\Delta t)\)
```


### 4.1 Terminology

An overview of the algorithm is presented as pseudo code by Ihmsen et al. [3] in Algorithm 1. It consists of three parts labeled as procedure, viz. advection prediction, pressure solve and integration.

Bold variables indicate three dimensional vectors whereas italic variables are considered as scalar values.

The W's are kernel functions used to sample the influence a particle has on a neighboring particle dependent of the distance between the two.

A specific particle in the fluid is identified with an index denoted with the subscript of $i$. The $j$ denotes one of the neighbors of $i$ and $k$ denotes the neighbors of $j$. It is worth to note that in the set of neighbors $k$ the particle with index $i$ is included, since if $j$ is a neighbor to $i$ it follows that $i$ is a neighbor of $j$.

The nabla symbol $\nabla$ indicates the del operator that operates in the scalar field of W to produce a non-normalized direction vector between the particles. In the cases where the results that are to be computed are scalar values the dot product is used which will be mentioned in the subsequent sections.

In the computations a global support radius is needed for various tasks. An illustration of it can be seen in Figure 4.1. It is computed as $n * 2 r$, where $r$ is the radius of the particle and $n \in \mathbb{N}$ defining how many particle widths from the center point of the particle neighbors are considered to influence it.


Figure 4.1: A particle (center circle) with its particle spacing (dashed circle) being equal to twice its radius as illustrated by the red line. The particle to the right has its center point within the particle spacing and is thus considered to be a neighbor.

### 4.2 Kernel functions

Three sets of kernels was provided by Prashant Goswami and are used when simulating IISPH: $\mathrm{W}_{\text {poly } 6}, \mathrm{~W}_{\text {spiky }}$ and $\mathrm{W}_{\text {viscosity }}$, see Figure $4.2 . \mathrm{W}_{\text {poly } 6}$ is used when calculating density, $\mathrm{W}_{\text {spiky }}$ is used in pressure related computations and $\mathrm{W}_{\text {viscosity }}$


Figure 4.2: The three kernels visualized with a global support radius of 0.18 m . Left: $W_{\text {poly6 }}$. Middle: $W_{\text {spiky }}$. Right: $W_{v i s c o s i t y . ~ I n ~ a l l ~ k e r n e l s ~ t h e ~ i n f l u e n c e ~ i s ~ d e c r e a s i n g ~ w h e n ~ n e a r i n g ~ t h e ~}^{\text {ne }}$ support radius. Full influence in the graphs is visualized with 1 or -1 and no influence as 0 .
is used in the particles' viscosity equation. Each kernel is used to determine the influence that a particle provides to a neighbor based on the distance to it; closer particles impart higher influence whereas those beyond the support radius provide none.

Each kernel returns zero if either the provided distance $d$ between two particles is zero (special case) or if the distance is larger than a provided global support radius $R$ (not to be confused with the particles radius which was used to compute the support radius). This effectively limits the number of particles which influence a specific particle.

$$
W_{\text {poly } 6}(d, R)= \begin{cases}0 & \text { if } d<0 \text { or } d \geq R  \tag{4.1}\\ \frac{8\left(1-6 s^{2}+6 s^{3}\right)}{\pi R^{3}} & \text { if } \frac{d}{R}<0.5 \\ \frac{16(1-s)^{3}}{\pi R^{3}} & \text { if } \frac{d}{R} \geq 0.5\end{cases}
$$

The $\mathrm{W}_{\text {poly6 }}$ is constructed as a cubic spline [1] according to (4.1), where $s=\frac{d}{R}$. Although it is possible to use alternative kernels, a study by Fulk and Quinn [16] have found that no other kernels give a significantly better result for density computations than the cubic spline.

$$
W_{\text {spiky }}(d, R)= \begin{cases}0 & \text { if } d<0 \text { or } d \geq R  \tag{4.2}\\ \frac{-8 * 3465}{512 \pi R^{5}} *\left(\frac{1-d^{2}}{R^{2}}\right)^{3} & \end{cases}
$$

The function for $\mathrm{W}_{\text {spiky }}$ (4.2) follows an ordinary $\cos (x)$ pattern. The major difference is that it only returns negative values instead of in the range of $[-1: 1]$.

$$
W_{\text {viscosity }}(d, R)= \begin{cases}0 & \text { if } d<0 \text { or } d \geq R  \tag{4.3}\\ \frac{45(R-d)}{\pi R^{6}} & \end{cases}
$$

$\mathrm{W}_{\text {viscosity }}$ returns an influence value according to a linear function (4.3).

### 4.3 Advection prediction

Advection is the conserved movement of a property in a fluid due to its bulk motion. When a fluid is flowing the internal properties such as regional density and pressure fluctuations will follow. As an example, imagine a river of water flowing in one direction. When dripping some color into the water it too will follow downstream rather than instantly disperse in all directions. The first component in IISPH is to predict this physical behavior for each particle.

In order to do this, iterating each particle in two passes is required. In the first pass (lines 3-5 Algorithm 1) density $\rho_{i}$, intermediate velocity $\mathbf{v}_{i}^{a d v}$ and displacement factor $\mathbf{d}_{i i}$ is calculated. During the second pass (lines 7-9 Algorithm 1) intermediate density $\rho_{i}^{a d v}$, initial pressure value $p_{i}^{0}$ and advection factor $a_{i i}$ is computed.

In the first pass of advection prediction the density of a particle $\rho_{i}$ (line 3) can be calculated as the summation of the products from each of its neighboring particle's mass $m_{j}$ and a finite support kernel function $W_{i j}$ which uses the distance between particles $i$ and $j$ as an input parameter.

Then an intermediate velocity $\mathbf{v}_{i}^{\text {adv }}$ (line 4) can be predicted as the particle's current velocity $\mathbf{v}_{i}$ and by taking Newton's second law of motion into account for all external non-pressure forces $\mathbf{F}_{i}^{a d v}$ (such as gravity and viscosity). This is done by combining all those forces into a single net force, divide it with the particle's mass $m_{i}$ and multiply with the time-step $\Delta t$, resulting in a velocity caused by non-pressure forces which is added to the current velocity.

$$
\begin{equation*}
\mathbf{F}_{i}^{v i s c}=-\sum_{j}\left(\mathbf{v}_{i}-\mathbf{v}_{j}\right)\left(\frac{m_{j}}{\rho_{i}}\right)^{2} \text { Const }_{v i s c} W_{i j} \tag{4.4}
\end{equation*}
$$

The viscosity force for a particle $i$ is calculated according to Equation 4.4 where Const visc is computed as $2 *$ sizeFactor and the kernel used is $\mathrm{W}_{\text {viscosity }}$.

Displacement is a quantity that measures a particle's distance of movement from its equilibrium position in the fluid as the fluid is transmitting a wave. The last part of the first pass is to compute each particle's displacement factor $\mathbf{d}_{i i}$ (line $5)$ which is repeatedly used in the following equations. It is the square of the timestep $\Delta t^{2}$ multiplied with the summation of the negative value of each neighbor's mass $m_{j}$ divided by the particle's calculated density squared $\rho_{i}^{2}$ multiplied with $\mathrm{W}_{\text {spiky }}$ which also uses the distance between $i$ and $j$ as an input parameter.

In the second pass of advection prediction the first variable to be calculated is the intermediate density $\rho_{i}^{\text {adv }}$ (line 7). This incorporates the contribution of advection created through pressure forces. It is the sum of the current density $\rho_{i}$ and the multiplication of the time-step $\Delta t$ and a summation of multiplications iterating for each neighbor. The multiplications are between the mass of the neighbor $m_{j}$, the dot product of the intermediate velocity vector $\mathbf{v}_{i j}{ }^{\text {adv }}$ between $i$ and $j$ and the non-normalized distance vector and finally the $\mathrm{W}_{\text {spiky }}$ previously used with the distance between $i$ and $j$ as input parameter.

The initial pressure value $p_{i}^{0}$ (line 8 ) is set to 0.5 of the previous frame's pressure value $p_{i}$ in order to receive optimal convergence. This was empirically proven by Ihmsen et al. [3]. In the first frame it is set to 0 .

$$
\begin{equation*}
a_{i i}=\sum_{j} m_{j}\left(\mathbf{d}_{i i}-\mathbf{d}_{j i}\right) \nabla W_{i j} \tag{4.5}
\end{equation*}
$$

The advection factor $a_{i i}$ which will be needed in the pressure solver is finally computed according to (4.5) where $m_{j}$ is the neighbor's mass. The displacement factor $\mathbf{d}_{i i}$ is already computed and $\mathbf{d}_{j i}$ can be computed according to (4.6) which is similar to how $\mathbf{d}_{i i}$ was calculated, only that it is not a summation over all neighbors, the mass $m_{i}$ is the particle's mass and the non-normalized vector to multiply with $\mathrm{W}_{\text {spiky }}$ is spanning from $j$ to $i$. A dot product is used (4.5) between the difference vector from the displacement factors and the non-normalized distance vector of $j$ and $i$.

$$
\begin{equation*}
\mathbf{d}_{j i}=-\Delta t^{2} \frac{m_{j}}{\rho_{j}^{2}} \nabla W_{i j} \tag{4.6}
\end{equation*}
$$

### 4.4 Pressure solve

The second component of the algorithm is to solve the pressure equation. Similarly to advection prediction it requires to iterate each particle in two passes. In the first pass (line 14 Algorithm 1) the total movement due to pressure forces from neighboring particles $\sum_{j} \mathbf{d}_{i j} p_{j}^{l}$ are computed. The second pass (lines 1617 Algorithm 1) computes the pressure $p_{i}^{l+1}$ for the next frame and assigns it. The pressure equation is solved employing relaxed Jacobi, which is an iterative process for approximating a solution to an equation [17]. This makes the nature of the solver iterative, meaning the two passes are iterated in a loop as it converges towards the pressure value. The average density of the next frame can be predicted according to (4.7). Due to this the iterative process can be controlled by terminating when the error in density is less than a threshold $\eta$. That is when the difference of the average predicted density $\rho_{l}^{a v g}$ and the fluid's rest density $\rho_{0}$ (the average density value of the fluid when perfectly still) is smaller than the threshold value $\eta$.

$$
\begin{align*}
\rho_{i}^{l+1}= & \rho_{i}^{a d v}+p_{i} \sum_{j} m_{j}\left(\mathbf{d}_{i i}-\mathbf{d}_{j i}\right) \nabla W_{i j}+ \\
& \sum_{j} m_{j}\left(\sum_{j} \mathbf{d}_{i j} p_{j}-\mathbf{d}_{j j} p_{j}-\sum_{k \neq i} \mathbf{d}_{j k} p_{k}\right) \nabla W_{i j} \tag{4.7}
\end{align*}
$$

The sum of movement caused by the pressure of neighboring particles is computed similarly to the displacement factor in advection prediction. It differs in
that instead of dividing the neighbor's mass with the particle's density, it is divided by the neighbor's density and that the resulting quotient is multiplied with the neighbor's pressure $p_{j}^{l}$ for this iteration.

$$
\begin{align*}
p_{i}^{l+1}= & (1-\omega) p_{i}^{l}+\omega \frac{1}{a_{i i}}\left(\rho_{0}-\rho_{i}^{a d v}-\right. \\
& \left.\sum_{j} m_{j}\left(\sum_{j} \mathbf{d}_{i j} p_{j}^{l}-\mathbf{d}_{j j} p_{j}-\sum_{k \neq i} \mathbf{d}_{j k} p_{k}^{l}\right) \nabla W_{i j}\right) \tag{4.8}
\end{align*}
$$

Computing the pressure is achieved according to (4.8). The calculation utilizes the current iteration's pressure values $p_{i}^{l}$ in order to get the next iteration's values $p_{i}^{l+1}$. The first term $(1-\omega) p_{i}^{l}$ is altering the pressure using a relaxation factor $\omega$. Optimal convergence is achieved by setting it to the value of 0.5 . The second term is calculated as the relaxation factor $\omega$ divided with the advection factor $a_{i i}$ and multiplied with the deviation from the rest density, computed as $\rho_{0}$ minus the intermediate density $\rho_{i}^{\text {adv }}$ and (4.9).

$$
\begin{equation*}
\sum_{j} m_{j}\left(\sum_{j} \mathbf{d}_{i j} p_{j}^{l}-\mathbf{d}_{j j} p_{j}^{l}-\sum_{k \neq i} \mathbf{d}_{j k} p_{k}^{l}\right) \nabla W_{i j} \tag{4.9}
\end{equation*}
$$

The summation of (4.9) should only add pressure values caused by each neighboring particle. All terms to this have already been computed with one exception. The movement caused by neighbors' pressure forces $\sum_{j} \mathbf{d}_{i j} p_{j}^{l}$ was computed in the previous pass. The product $\mathbf{d}_{j j} p_{j}^{l}$ is the product of the neighbor's displacement factor and pressure, both of which are calculated and available to use. The $\sum_{k \neq i} \mathbf{d}_{i j} p_{j}^{l}$ is the same as (4.10) which is partially computed.

$$
\begin{equation*}
\sum_{k \neq i} \mathbf{d}_{j k} p_{k}^{l}=\sum_{k} \mathbf{d}_{j k} p_{k}^{l}-\mathbf{d}_{j i} p_{i}^{l} \tag{4.10}
\end{equation*}
$$

The first term in (4.10) is the neighbor's movement caused by pressure forces from its neighbors and too has already been computed in the previous pass. The second term however is the movement of the neighbor caused by the particle's pressure (particle $i$ of which the pressure is being calculated), thus it should be excluded since only pressure values from neighbors to particle $i$ should be considered.

$$
\begin{equation*}
\mathbf{d}_{j i} p_{i}=-\Delta t^{2}\left(\frac{m_{i}}{\rho_{i}^{2}(t)} p_{i}^{l} \nabla W_{j i}(t)\right) \tag{4.11}
\end{equation*}
$$

This is calculated according to (4.11), where $m_{i}$ is the particle's mass, $\rho_{i}^{2}$ is the particle's density squared and $p_{i}^{l}$ is the particles pressure in the current iteration. The vector to be multiplied with $\mathrm{W}_{\text {spiky }}$ is spanning between $j$ and $i$. Once the movement caused by the particle itself is excluded the result is multiplied as according to (4.9) with the neighbor's mass $m_{j}$, the dot product of the result and
the vector between the particle $i$ and neighbor $j$ and $\mathrm{W}_{\text {spiky }}$ function which is using the distance between $i$ and $j$ as parameter. Finally the computed pressure is assigned to the particle, if the value would be negative it is clamped to zero due to negative pressure values not being allowed.

In order to control the compression the density error needs to be calculated as well. As mentioned above it can be solved according to (4.7). Most values are already computed, the intermediate density $\rho_{i}^{a d v}$ was used before when computing the pressure $p_{i}$. The second term's summation for each neighbor uses the difference of the displacement factor $\mathbf{d}_{i i}$ (already available) and the neighbors' displacements due to the particle itself $\mathbf{d}_{j i}$ (can be calculated again (4.11) excluding the pressure $p_{i}^{l}$ ). $\mathrm{W}_{\text {spiky }}$ again utilizes the distance between $i$ and $j$ and the support radius as input. The third term is the exactly the same as (4.9).

### 4.5 Integration

Once the pressure is computed it is possible to update the particles with correct velocities $\mathbf{v}_{i}(t+\Delta t)$ and positions $\mathbf{x}_{i}(t+\Delta t)$ achieved in the integration procedure (lines 21-22 Algorithm 1).

The velocity $\mathbf{v}_{i}(t+\Delta t)$ is calculated as the intermediate velocity $\mathbf{v}_{i}^{\text {adv }}$ which were calculated in advection prediction and by adding the velocity caused by the pressure force $\mathbf{F}_{i}^{p}(t)$ according to Newton's second law of motion. The pressure force $\mathbf{F}_{i}^{p}(t)$ should preserve momentum and is obtained according to (4.12) [1, 3].

$$
\begin{equation*}
\mathbf{F}_{i}^{p}(t)=-m_{i} \sum_{j} m_{j}\left(\frac{p_{i}(t)}{\rho_{i}^{2}(t)}+\frac{p_{j}(t)}{\rho_{j}^{2}(t)}\right) \nabla W_{i j}(t) \tag{4.12}
\end{equation*}
$$

The position $\mathbf{x}_{i}(t+\Delta t)$ is then updated by adding the product of the time-step $\Delta t$ and the velocity $\mathbf{v}_{i}(t+\Delta t)$ to the current position $\mathbf{x}_{i}(t)$.

## Chapter 5

## Implementation

Three versions of the algorithm were implemented. The first one was a sequential version running on the CPU. The second one was the proposed parallel version running on the GPU. A parallel implementation of the CPU-version was also developed using OpenMP. All three versions are based on the proposed IISPHalgorithm by Ihmsen et al. [3], see Algorithm 1, implemented in C++.

DirectX 11.0 is used for rendering, billboards are used to represent each particle. Billboards were used because it made it possible to render more particles due to the small amount of triangles compared to a spherical object. DirectX 11.0 was chosen due to previous experience and it allowed for reusing an already existing graphics engine and basic program structure.

Microsoft Visual Studio ${ }^{\circledR} 2013{ }^{1}$ was used as developing environment because of previous experience have been exclusively utilizing it. Additional software used was the NVIDIA Nsight ${ }^{T M}$ Visual Studio Edition ${ }^{2}$ in order to assist with GPU debugging and profiling.

IISPH needs a set of variables whose values are constant throughout the simulation, such as the gravity constant, viscosity constant, time-step etc. These variables can be seen in Figure 5.1. They are collected into a single static class which can be accessed from anywhere within the program.

Figure 5.2 illustrate the information needed for each particle. However, how it was implemented differs between the CPU-versions and the GPU-version. This will be covered in respective implementation details below.

To keep the particles inside the specified simulation domain, a set of particles called boundary particles are utilized. These do not move during the simulation; instead they have a fixed position and act as impenetrable walls, providing the necessary forces to keep the moving fluid particles within the simulation domain.

[^1]```
// defines particle resolution
float sizeFactor
double globalSupportRadius
// time step
float deltaT
// physical quantities
double fluidParticleSpacing
float gravityConst
float fluidRestDensity
float initialMass
float fluidGasConst
float fluidViscConst
float densityError
// convergence constant
float relaxationFactor
// Iteration values for
// pressure solve loop
uint minIterations
uint maxIterations
```

Figure 5.1: Constant variables data structure. These variables are used throughout the physics simulation but their values are never modified once initialized.

### 5.1 CPU

During the initialization of the simulation a neighbor grid is created which divides the simulation domain into a uniform grid. Each cell receives a unique identifier and calculates which other cells that are neighbors of it and stores theirs identifiers. The cell is thereafter stored in a vector container.

The particles' data are stored in the manner of array of structs (AoS), that is each particle is an object consisting of the data according to Figure 5.2 and the data being localized in a consecutive section of memory.

The particles are created according to a user specified scene as the struct mentioned above. The variables of the algorithm in Algorithm 1 correlate to the ones in the struct as can be seen in Table 5.1. In the creation process all values are set to default values of zero except from the position and whether the particle is a boundary particle or not. The last two variables in Figure 5.2 indicate whether a particle is a boundary particle and at which cell ID (from now on denounced as z-index) the particle is currently residing in. These variables are implementation specific to assist with various tasks, such as finding particle neighbors, hence they are not represented in Algorithm 1.

The following sections describes the reoccurring events for each simulated frame.

```
float3 position
float3 velocity
float density
float pressure
float advection
float densityAdvection
float3 velocityAdvection
float3 displacement
float3 sumPressureMovement
bool isStaticBoundaryParticle
uint index
```

Figure 5.2: The particle data structure. These are the variables that are stored for each particle. Total memory usage per particle reaches 81 bytes. Note that indexations to identify neighbor particles are not included.

| Struct | Algorithm |
| ---: | :--- |
| position | $\mathbf{x}_{i}$ |
| velocity | $\mathbf{v}_{i}$ |
| density | $\rho_{i}$ |
| pressure | $p_{i}^{l+1}$ |
| advection | $a_{i i}$ |
| densityAdvection | $\rho_{i}^{\text {adv }}$ |
| velocityAdvection | $\mathbf{v}_{i}^{\text {adv }}$ |
| displacement | $\mathbf{d} i i$ |
| sumPressureMovement | $\sum_{j} \mathbf{d}_{i j} p_{j}^{l}$ |

Table 5.1: Mapping of the variables in the particle data struct to the ones in the IISPHalgorithm.

### 5.1.1 Neighbors

Before calculating how the particles are distributed in the grid and finding each particle's neighbors they need to be sorted. This is done according to which cell they belong to by using the cell's identifier, calculated as described in section 3.1 in Goswami et al. [13]. After the sorting, the particles belonging to the same cell have been grouped together, see Figure 5.3. Thrust's CPU-version of sort is used for the particle sorting.

To make it easier to find a particle's neighbors, each cell stores the container index of the first occurring particle which is inside of the cell and saves how many of the following particles which also exist inside the cell.

To find all neighbors of a particle, it is required to scan the cell the particle resides in and the 26 neighboring cells. Since each cell knows which particles resides in them from previous calculations, it is only a matter of iterating through those particles and check if they are closer or equal to a global support radius, if closer, then a reference to that particle is added to the current particle. Since a


Figure 5.3: Illustrating how particle's IDs are sorted based on location in the spatial uniform grid. Throughout the simulation, particles will change which cell they are spatially located in (top part). In each frame a sorting occurs grouping particles with the same cell ID together, illustrated with a black arrow. The result is particles stored by cell ID (bottom part).
particle's neighbors are available, the directions between a particle and its neighbors and the influence of every kernel are computed and stored as well, to later be used during physics computations.

### 5.1.2 Advection prediction

Advection prediction is divided into two major sections, each section iterating the particles. In both sections a particle's neighbors are fetched once, temporarily stored locally, to later be iterated when calculating density, viscosity and displacement since these calculations require data from surrounding neighbors.

The first section computes the density, intermediate velocity and displacement factor for each particle according to lines 3-5 in Algorithm 1 and stores the resulting values in their respective variables density, velocityAdvection and displacement. When calculating a particle density, its own density contribution is added before iterating over its neighbors adding their contribution to the particle density.

By using the stored results from the first section, the second section calculates each particle's intermediate density, initial pressure and advection factor according to lines 7-9 in Algorithm 1. These are stored in the variables densityAdvection, pressure and advection. The initial pressure can be stored in the pressure variable by multiplying itself with 0.5 , as mentioned in section 4.3.

### 5.1.3 Pressure solve

Computing pressure values are done according to section 4.4 with certain modifications. A safeguard was added to the while-loop to prevent it from locking in an infinite loop by not only checking if the average density error is smaller than the acceptable error but also if the iteration counter $l<50$.

According to Algorithm 1 the pressure should be split into two for-loops, the first one calculates the movement due to neighboring particles' pressure values and
stores it in sumPressureMovement. The second loop computes the next iteration's pressure before storing it in pressure. Both loops are implemented according to the pseudo code in Algorithm 1 with no modifications.

As previously mentioned it is possible to predict the density in the next frame in order to compute the average density error, thus a third for-loop was added. For each particle the density of it in the next iteration is computed as Equation 4.7. Only density values greater than the fluid's rest density are considered as errors. Should the value be less than the rest density, the contribution to the error is clamped to 0 .

### 5.1.4 Integration

The integration works accordingly to the algorithm with a few additions and changes. Collision handling is added to ensure that the particles stay inside the simulation domain and also to avoid getting invalid cell indices due to particles going outside of the uniform grid. It has been modified so particles that are flagged as boundaries are not updating their positions and velocities. Finally in the function the new position and velocity are stored in their respective variables position and velocity.

### 5.2 GPU

One of many performance issues that has to be taken into account when designing an algorithm or programming on the GPU is the memory transfer bottleneck occurring when moving memory back and forth to the CPU. One naïve approach would be to do all the computations on the GPU and, to render the results, one would copy the data back to the CPU to be able to update the buffers used when rendering.

However due to the interoperability with DirectX, once the particles are in GPU memory they are never transferred back to the CPU. This effectively removes the memory transfer bottleneck for rendering. In addition to avoiding the slow transfer rates between CPU and GPU, by removing a synchronization point even more time is saved.This also makes it possible to save overall memory since there is no longer a need to have a copy of the data on the CPU and another one on the GPU.

CUDA textures [23] are used throughout the implementation whenever repeated access to an array of data is used within a function. This is due to their fundamental nature of utilizing the GPU's cache to improve the overall speed when repeatedly fetching contiguous data. The gained speed is highly dependent on how the memory is accessed and if the data has enough locality to allow coalescing. This usage is read-only and thus cannot be utilized if an array must be read from and written to during the same kernel.

Furthermore whenever a kernel directly modifies or does computations on a particle or cell, that kernel is launched so every particle or cell gets assigned one thread. For that, the necessary number of CUDA blocks needs to be computed. It is computed as $\operatorname{ceil}(t / s)$, where $t$ is the total number of threads needed and $s$ is a specified number of threads for each block. This can create threads that will be unused, this is handled by checking if a threads global id which is calculated as blockIdx. $x$ * blockDim. $x+$ threadIdx.x is lower than the total number of objects available, if so then the thread will continue to run and if not it will terminate.

The number of threads per block is limited by the graphics card's compute capability, e.g. a modern graphics card with compute capability 5.x can have a maximum of 1024 threads for each block, for more details about the different compute capabilities see the CUDA Toolkit Documentation [23]. An overview of kernels used can be seen in Algorithm 2.

### 5.2.1 Initialization

The CUDA implementation requires initialization and allocation of device memory, which is video RAM (VRAM), from the host. Constant variables used throughout the program as global constants such as the FluidConstants are initialized on the host and copied to constant memory on the device.

Unlike the CPU-versions the data of the particles are arranged into SoA in the GPU-version. One advantage of SoA is that it allows for coalesced memory access of consecutive threads. SoA also avoids the issue of padding between elements due to memory alignment which may occur with AoS. The host allocates the arrays in device memory and initializes the particles' starting positions; transferring the position data to the corresponding array in device memory.

In order to render the simulation, data such as the particles' positions and colors are necessary. This information can be shared from CUDA to DirectX without the need to copy the data from the device to the host and back again by using interoperability, this is covered in subsection 5.2.6.

```
uint deviceParticleHash[N]
uint deviceParticleId[N]
uint2 deviceCellGrid[N] //start(x), end(y)
//position(x,y,z), isBoundary(w)
float4 deviceParticlePosition[N]
float4 deviceParticleVelocity[N]
float deviceParticleDensity[N]
float deviceParticlePressure[N]
float deviceParticleDensityAdv[N]
float4 deviceParticleVelocityAdv[N]
float4 deviceParticleSumPressureMovement[N]
//displacement(x,y,z), advection(w)
float4 deviceParticleDisplacement[N]
float deviceParticleDensityNextIteration[N]
uint deviceNeighborGrid[N]
uint deviceParticleNeighbors[N]
```

Figure 5.4: The different buffers allocated on the device and used in the physics calculations. Buffers beginning with deviceParticle are corresponding to the variables in the particle struct seen in Figure 5.2.

The initialization begins by constructing the scene of particles precisely as the CPU version does. After the creation the constant variables in Figure 5.1 are transferred to the constant memory on the GPU. It is followed by the initialization of all buffers (see Figure 5.4) used during the simulation by allocating memory and setting default values. The buffers are allocated as mentioned above as contiguous linear memory blocks residing in global memory on the GPU.

The total allocation size depends on the number of particles. For one particle 264 bytes are needed for the physics simulation (104 bytes for the particle data and 160 bytes allocated for neighbors), additional 56 bytes are used when swapping values during the data sort and finally 36 bytes are used for rendering. Note that only 20 bytes (float 4 color and float scale) are required for the rendering, the additional 16 bytes (float4 position) acts as a separator between the rendering
and physics. As such a total of 356 bytes are needed for each particle throughout the implementation.

After the buffer initialization a parallel version of createGridNeighbors is launched to create and store the grid structure directly on the GPU.

The final step in the initialization is the initial data transfer, the transfer cannot begin before the necessary rendering resources are bound to the physics, see function one in Figure 5.8. When the resources are bound the previously created particles data is transferred to global memory with the addition of rendering data such as color and scale for the two types of particles, boundary and fluid.

### 5.2.2 Neighbors

The first kernel launch calcIndex in the physics loop calculates the z-index for each particle according to section 3.1 in Goswami et al. [13] and stores it in deviceParticleHash. It also stores an identifier in deviceParticleId which is used when sorting the particles in the next kernel.

After the z-index and identifier assignment the particles are grouped together by their z-index value and sorted according to their id using Thrusts sort_by_key algorithm. The ids stored are no longer following a sequence, each element is instead indicating which particle that should be stored at that buffer location in the buffers. This is crucial in sortParticlesData where the variables used between updates; position, velocity, color, scale and pressure needs to be relocated accordingly to the new z-index values.

```
Algorithm 3: FindGridCellStartEnd
    gridIndex = zValue[index]
    sharedIndex[t.x+1] = gridIndex
    if index \(>0\) \&\& \(t \cdot x==0\) then
        sharedIndex[0] = zValue[index - 1]
    end
    cell[index] = default
    __syncthreads()
    if index \(==0| |\) gridIndex \(!=\) sharedIndex[t.x] then
        cell.x = index
        if index \(>0\) then
            cell[sharedIndex[t.x]].y = index
        end
    end
    if index \(==\) numParticles -1 then
        cell[gridIndex].y = index + 1
    end
```

FindGridCellStartEnd is launched to make finding a particle's neighbors more convenient and efficiently, the goal for this kernel is described in subsection 5.1.1. To avoid the need for iterating every particle and check if it is a valid
neighbor, the kernel runs according to Algorithm 3 which is inspired by a particle demo by NVIDIA [24]. Where index is the global thread index, t.x is the same as threadIdx.x and sharedIndex// is a shared memory array with an allocated size of CUDA blocksize +1 .

The updateNeighbors works as described in subsection 5.1.1, with one major difference. Instead of sequentially iterating every particle, each particle is assigned one thread to find all of its neighbors. Apart from the algorithm itself, the way it is stored differs as well; since there is no such thing as a vector container on the GPU, especially not a vector container of vector containers which the CPU version utilizes. The GPU stores the neighbors in deviceParticleNeighbors which is allocated as a contiguous memory block with room for the (total number of particles * max number of neighbors allowed) elements. This is a 2D array stored as a 1D array, as such it is accessed as $[x, y]=x *$ max number of neighbors allowed $+y$.

Because of the contiguous memory allocation and for simplicity it was decided not to store pre-computed frame based values such as distances between particles, which is done in the CPU-implementations.

```
Algorithm 4: AdvectionPrediction_CPU Algorithm 5: AdvectionPrediction_CUDA
    Procedure ADVECTION PREDICTION Procedure ADVECTION PREDICTION
        foreach particle \(i\) do
                            Kernel computeDisplacementFactor
            compute \(\rho_{i}(t)=\sum_{j} m_{j} W_{i j}(t)\)
            predict \(\mathbf{v}_{i}^{a d v}=\mathbf{v}_{i}(t)+\Delta t \frac{\mathbf{F}_{i}^{a d v}(t)}{m_{i}}\)
            \(\mathbf{d}_{i i}=\Delta t^{2} \sum_{j}-\frac{m_{j}}{\rho_{i}^{2}} \nabla W_{i j}(t)\)
        foreach particle \(i\) do
            \(\rho_{i}^{a d v}=\rho_{i}(t)+\Delta t \sum_{j} m_{j}\left(\mathbf{v}_{i j}^{a d v}\right) \nabla W_{i j}(t)\)
            \(p_{i}^{0}=0.5 p_{i}(t-\Delta t)\)
            compute \(a_{i i}(4.5)\)
            foreach particle \(i\) do
                            compute \(\rho_{i}(t)\)
                            predict \(\mathbf{v}_{i}^{\text {adv }}\)
                    compute \(\mathbf{d}_{i i}\)
        Kernel computeAdvectionFactor
            foreach particle \(i\) do
                    compute \(\rho_{i}^{a d v}\)
                    compute \(p_{i}^{0}\)
                            compute \(a_{i i}(4.5)\)
```

Figure 5.5: Comparison between CPU- (left) and CUDA-solution (right) for advection prediction. The two kernels in the CUDA-solution correspond to the for-loops in the CPU-solution. A thread will be allocated for each particle $i$.

### 5.2.3 Advection prediction

Due to the necessity of the advection prediction part to run its two loops separately, one after the other, it is required to have a synchronization barrier between the two when developing a parallel version. This can be achieved either by using thread synchronization (using __syncthreads) or by launching each loop as a separate kernel since kernel launches are done in sequence on the CPU. Using __syncthreads will only allow threads within a block to be synchronized [25], thus only a single block would be possible to be utilized if this method were cho-
sen. Due to this restriction, the separation into two kernel launches was chosen, see Figure 5.5.

Parallelism is achieved by assigning each particle a thread to compute its values and removing the two outer for-loops which the CPU iterated over for each particle. Input-parameters with repeated access to arrays are fetched as textures to alleviate the accessing from global memory. Because of the outputs from computeDisplacementFactor are completed before computeAdvectionFactor can begin it is safe to access the dependent data using texture fetches.

### 5.2.4 Pressure solve

The pressure solver can be parallelized with the same strategy as advection prediction, that is, each particle will be assigned a thread and the for-loops is replaced by kernel launches. However, due to that these loops are themselves iterated repeatedly as long as the average density error is greater than an acceptable threshold, this strategy will restrict how much of the pressure solver that is executed on the GPU. Kernel launches are done from the CPU and thus the while-loop and its conditional checks too will be CPU-code. An alternative solution is discussed in subsection 5.3.2.

```
Algorithm 6: PressureSolve_CPU Algorithm 7: PressureSolve_CUDA
    Procedure PRESSURE SOLVE Procedure PRESSURE SOLVE
        \(l=0\)
        while \(\rho_{i}^{\text {err }}>\eta \vee l<2\) do
            foreach particle \(i\) do
                \(\sum_{j} \mathbf{d}_{i j} p_{j}^{l}=\Delta t^{2} \sum_{j}-\frac{m_{j}}{\rho_{j}^{2}(t)} \nabla W_{i j}(t)\)
            foreach particle \(i\) do
                compute \(p_{i}^{l+1}(4.8)\)
                \(p_{i}(t)=p_{i}^{l+1}\)
            foreach particle \(i\) do
            L compute \(\rho_{i}^{l+1}\) (4.7)
            foreach particle \(i\) do
                \(\left\lfloor\right.\) reduce \(\rho_{i}^{\text {err }}=\max \left(\rho_{i}^{l+1}-\rho_{0}, 0\right)\)
            \(l=l+1\)
        \(l=0\)
        while \(\rho_{i}^{\text {err }}>\eta \vee l<2\) do
            Kernel computeSumPressureMovement
                foreach particle \(i\) do
                    compute \(\sum_{j} \mathbf{d}_{i j} p_{j}^{l}\)
            Kernel computePressure
                foreach particle \(i\) do
                compute \(p_{i}^{l+1}(4.8)\)
            rnel predictDensity
                foreach particle \(i\) do
                                    compute \(\rho_{i}^{l+1}\) (4.7)
            Kernel calcDensityError
                                foreach particle \(i\) do
                                    reduce \(\rho_{i}^{\text {err }}\)
                            \(l=l+1\)
```

Figure 5.6: Comparison between $C P U$ - (left) and $C U D A$-solution (right) for pressure solve. The four kernels in the CUDA-solution correspond to the for-loops in the CPU-solution. A thread will be allocated for each particle $i$. The condition check for the while-loop is still executed on the $C P U$.

As can be seen in Figure 5.6 another kernel is added beside the ones that computes the movements due to pressure, pressure values and the one that tries
to predict the density for the density error. The kernel calcDensityError is a small kernel that adds up the estimated density values using Thrust reduce.

As with advection prediction, pressure solve kernels use texture fetches to reduce global memory access for input-parameters.

### 5.2.5 Integration

This procedure is the least changed, see Figure 5.7, due to its simple and straightforward structure. Just as in the CPU-version it has the additional collision handling and the boundary particles do not update their velocities nor positions. It is launched as every other kernel and utilizes CUDA textures whenever possible.

| Algorithm 8: Integration_CPU | Algorithm 9: Integration_CUDA |
| :---: | :---: |
| $\begin{aligned} & \text { Procedure INTEGRATION } \\ & \qquad \begin{array}{l} \text { foreach particle } i \text { do } \\ \qquad \begin{array}{l} \mathbf{v}_{i}(t+\Delta t)=\mathbf{v}_{i}^{\text {adv }}+\Delta t \mathbf{F}_{i}^{p}(t) \\ \mathbf{x}_{i} \end{array}(t+\Delta t)=\mathbf{x}_{i}(t)+\Delta t \mathbf{v}_{i}(t+\Delta t) \end{array} \end{aligned}$ | Procedure INTEGRATION Kernel integration foreach particle $i$ do compute $\mathbf{v}_{i}(t+\Delta t)$ compute $\mathrm{x}_{i}(t+\Delta t)$ |

Figure 5.7: Comparison between $C P U$ - (left) and $C U D A$-solution (right) for integration. The kernel in the CUDA-solution corresponds to the for-loop in the CPU-solution. A thread will be allocated for each particle $i$.

### 5.2.6 DirectX interoperability

```
cudaGraphicsD3D11RegisterResource(cudaGraphicsResource **resource,
ID3D11Resource *pD3DResource, unsigned int flags)
cudaGraphicsUnregisterResource(cudaGraphicsResource_t resource)
cudaGraphicsMapResources(int count, cudaGraphicsResource_t *resources,
cudaStream_t stream = (cudaStream_t)0)
cudaGraphicsUnmapResources(int count, cudaGraphicsResource_t *resources,
cudaStream_t stream = (cudaStream_t)0)
cudaGraphicsResourceGetMappedPointer(void **devPtr, size_t *size,
cudaGraphicsResource_t resource)
```

Figure 5.8: The interoperability commands used which allow CUDA to manipulate the buffers for DirectX.

To connect CUDA to DirectX four functions where used, their signatures can be seen in Figure 5.8. The functions always returns a cudaError_t indicating if anything went wrong or if the function call succeeded, e.g. an error indicating an invalid value or a unknown error [26].

The first function is used to tell CUDA to register a given resource accompanied with optional flags. The flags give CUDA a hint to how the resource is
going to be used e.g. as a surface reference. However, there are limitations on which Direct3D resources that can be registered, a few of those limitations are resources allocated as shared and the primary render target cannot be registered. The second function is used to unregister a registered resource [26].

The third and fourth functions are used to map and unmap count resources to allow access from CUDA. While the resources are mapped, access is granted. However, if DirectX should try to access the resources while it is bound it will cause undefined behavior. Function three guarantees any DirectX API calls are done before any following CUDA work begins, while function four guarantees that all CUDA work is completed before new DirectX calls are issued [26].

The final function is used to get a void** pointer which points to the first element in the provided resource. If desired, the accessible size can also be provided. Otherwise providing the function with nullptr will block the function from returning a size [26].

These functions are used for each connected Direct3D resource. The resources used are allocated in three structured buffers containing the positions, colors and scales for each particle. Function one is used only once for each resource after the initialization of the physics and graphics, function two is used when the physics destructor is called.

Since function three and four are synchronization points in the program they should not be used in abundance because, if not carefully placed, they could very well limit the program's overall performance. Therefore, in the implementation each of the three resources call function three closely followed by function five at the beginning of each reoccurring update while function four is the final call in each update.

### 5.3 Alternative approaches

The proposed implementation was one of few alternatives that emerged during the implementation stage. Alternatives ranged from function changes to fundamental structure changes in kernels. Those worth mentioning are the shared memory approach and adjustments due to newer compute capabilities.

### 5.3.1 Shared memory

A solution based on Goswami et al. [13] was implemented. This was done by inserting one stage before advection prediction and after finding all cells start and end particles, this stage copies the buffer containing cells start and end particles indices to a new buffer and modifies it. In the new buffer all the empty cells were removed and the cells with a particle count above 27 was divided into chunks, each containing up to a maximum of 27 particles.

To be able to use the new buffer with the kernels, modifications had to be made accordingly. Kernels were now launched with a fixed number of threads, viz. 27, one for each particle with as many blocks as the new buffer had cells.

All kernels had to be slightly modified to accompany the new solution. The initial process was changed to determine the maximum amount of possible neighbors residing in neighboring cells. Before iterating through the maximum amount of neighbors each thread copies its particle's relevant data into shared memory. During the frame each thread copies a neighboring particle into shared memory and synchronizes the threads directly afterwards without leaving the frame. Finally during the frames each thread iterates over the data residing in shared memory and runs the desired computations such as calculating density for the assigned particle.

### 5.3.2 Compute Capability 5.X

Due to hardware limitations on the development platform, it was necessary to restrict the solution to compute capability 3.0. This effectively restricted which features in CUDA that could be used.

With the introduction of compute capability 3.5 dynamic parallelism was supported [23]. This allows for a kernel to launch separate kernels that are run in parallel. The control loop for the compression when solving the pressure equation could take advantage of this feature by launching its subsequent kernels (the kernels to compute movement due to pressure, pressure values, calculate a predicted density and the average density error) as child kernels. Thus unnecessary returns to CPU in order to launch kernels could have been avoided.

Another feature set introduced with compute capability 3.5 is the atomic min and max operations. This could have been used in the kernel for finding a cell's start and end indices. With these atomic operations the branching factor could have been reduced by the possibility to eliminate certain if statements. This in turn could have led to better performance.

## Chapter 6

## Experimental Method

Experiments were conducted on all versions by running identical scenarios with implemented test scenes and measuring the computation times required to complete each scenario. Due to the aim of the thesis and that it is commonly done [3, $13,14]$, measuring the time required for running the simulation was deemed as the best method to gather relevant data. All scenarios assume identical relative camera position and view direction.

Additionally, the particles' memory usage was gathered as well. Since a single graphics card only has a certain amount of memory it is a limiting factor on how many particles that can be residing in memory simultaneously. For instance a 4 GB graphics card can theoretically hold approximately 12 million particles with the proposed solution.

The SPH CUDA algorithm presented by Goswami et al. [13] was modified to the proposed fine-grained solution so the performance cost of adding incompressibility to fluids could be observed.

The experiments were run on two different hardware setups according to Table 6.1.

|  | Setup 1 | Setup 2 |
| :---: | :---: | :---: |
| CPU | Intel ${ }^{(8)}$ Core $^{\text {TM }}{ }^{1}$ i7-3770, $3.4 \mathrm{GHz}, 8 \mathrm{MB}$ Cache | Intel ${ }^{(8)}$ Xeon ${ }^{(8)}{ }^{1} \mathrm{E} 5-1650,3.2 \mathrm{GHz}, 12 \mathrm{MB}$ Cache |
| GPU | MSI GeForce GTX 970 Gaming 4G | NVIDIA Quadro K4000 |
| RAM | Corsair Vengeance DDR3, 1600MHz, 16GB | DDR3, 1600MHz, 16GB |
| OS | Windows ${ }^{\circledR}{ }^{2} 7$ Ultimate 64 -bit | Windows ${ }^{\circledR}{ }^{2}$ 8.1 Enterprise 64 -bit |

Table 6.1: Computer specifications for experiments.

### 6.1 Time measurement functions

To measure the time and to get as close accuracy as possible in terms of what was measured, three separate timers were used: one for CPU-code, one for CUDA-

[^2]code and one for rendering. Timings of the physics simulation were conducted using two approaches. Both methods computed the time used per frame and calculated an average time usage. The first one created a time stamp right before launching the physics simulation, ran the current frame's simulation and created a new time stamp right after the end of the simulation, which allowed for an evaluation of total time required by the frame. Adding one layer of detail, the second method used the same approach but on comparable (CPU compared to GPU) subsections inside of the physics-function. This allowed for identification of which sections of the physics simulation that were the most computationally expensive. The two approaches were run separately to not cause inaccurate timings due to overhead.

The CPU-version utilizes the QueryPerformanceCounter API available in Microsoft Windows which can provide the frequency of the CPU core as well as the number of clock ticks between two time stamps [27]. The time can thus be evaluated in milliseconds and seconds, and finally converted to FPS.

CUDA provides the methods cudaEventRecord, which is used to record an event, and cudaEventElapsedTime [28] which evaluates the time between two recorded events. The GPU-timer for CUDA measurements used this.

The time required to render each frame was measured using the ID3D11Query interface which is used to query the graphics card for data. Using D3D11_QUERY_TIMESTAMP and D3D11_QUERY_TIMESTAMP_DISJOINT it is possible to receive reliable time stamps in clock ticks and the GPU core frequency [29, 30] which is used to convert the result similar to how the CPU-timer does.

### 6.2 Test scenes

Four different test scenes were implemented with varying complexity, simple, breaking dam, two blocks and gallery, see Figure 6.1. All scenes are of the same dimensions and use identical setup for static boundary particles and collision boxes. The boundary particles creates a box with an open top domain. This can be seen in Figure 6.2 where the green particles represent the static boundary particles and the blue ones are the fluid particles. The number of particles ranged from 4000 to 200000 particles.

In simple-scene a block of fluid particles begins by falling towards the bottom of the box before collapsing. In breaking dam the fluid particles are stacked directly on the bottom as a block alongside one of the walls, collapsing into the box. The two blocks-scene is similar to the simple-scene but consist of two smaller separate blocks which fall towards the bottom of the box. The last scene, gallery, is more complex. It contains obstructions created with static boundary particles which were used to build a wall and some pillars. A small block of fluid particles begins by falling towards the "ground" before interacting with the walls and pillars.


Figure 6.1: The four test scenes. Top left: simple, 121000 particles. Top right: breaking dam, 114000 particles. Bottom left: two blocks, 116000 particles. Bottom right: gallery, 99 000 particles. Note that boundary particles have been omitted during rendering.


Figure 6.2: The gallery scene with 51000 boundary particles (green) and 48000 fluid particles (blue).

### 6.3 Memory usage

To measure the total memory allocated by the CUDA-solution, the CUDA allocation function was wrapped in a new function which then was used instead when allocating new buffers. In the function a variable was increased by the allocated size every time a new buffer was allocated. The memory footprint for the constant variables seen in Figure 5.1 is neglected in the tests since the memory usage for these variables are equal between the implementations.

Since the CPU-version utilizes C++ std::vector it is troublesome to get an accurate number of the total amount of memory allocated due to the dynamic nature of the container. This is only a problem for the std::vector containing the particles' neighbors since the number of neighbors differ between frames. As such an average number of neighbors where calculated during each simulation. To get how much memory a struct was allocating the C+ function sizeof was
used. To get the total allocated size for the CPU-implementation, the size of each struct was multiplied with its corresponding count e.g. the number of particles multiplied with the size of the particle struct.

### 6.4 Physical precision comparison

The parallel GPGPU-implementation should not alter the visual quality of IISPH; thus a verification of this was necessary to be performed. Two common techniques to measure errors and noise in images are the peak signal-to-noise ratio (PSNR) and structured similarity index measure (SSIM) [18]. Both methods are sensitive for different image degradations due to lossy compressions. SSIM has been criticized for giving an unreliable result [19].

The PSNR was chosen as the metric for comparing the simulations. An acceptable value for images with bit depths of 8-bit ranges between $30-40 \mathrm{~dB}$. The higher the value, the better the result is.

The comparison images were saved as portable network graphics (PNG), which is a lossless format, to avoid issues due to image degradation.

## Chapter 7

## Results

To ease further reading this section will only present a compilation of processed data. All collected data can be reviewed in Appendix A. Multiple test runs were executed. The data presented is from a single run but has been cross-validated with the others to ensure the values being reasonable.


Figure 7.1: All four scenes visualized at the same time interval. From top to bottom: simplescene ( 121000 particles), breaking dam ( 114000 particles), gallery (99 000 particles) and two blocks (116 000 particles). In this case a time-step of 3.5 ms and particle spacing of 0.05 $m$ was used.

In all measured scenarios a fixed time-step of 3.5 ms and particle spacing of 0.09 m was used. All kernels were launched with blocks of a maximum of 256 threads per block. To increase or decrease the total number of particles in a scene the dimension was changed. Each of the scenes used the same set of dimensions, hence the number of particles varied between scenes. To ensure accuracy of the time measurements the average frame-time was computed from test scenarios running for 300 and 1000 frames. The deviation between these two cases was considered negligible and thus only data from the 1000 frames scenarios are being presented in this section.

A time-lapse for the scenes can be seen in Figure 7.1.

### 7.1 Time usage

Note that the lines for the graphs comparing the scenes in this section ends at different x -values. This is due to the amount of particles varying between scenes and all scenes were running with the same dimension changes to scale them up (resulting in increased amount of particles) during the experiments.


Figure 7.2: The graph visualizes the computation time of the algorithm per frame on setup 1 for the CUDA-solution compared to OpenMP. All four tests scenes used a time-step of 3.5 ms and a particles spacing of 0.09 m . Measurements was taken over 1000 frames. The black horizontal dashed line denotes the 30 FPS mark.

The CUDA-solution is able to achieve higher performance than an OpenMPimplementation on the CPU according to Figures 7.2 and 7.3. The CPU has a steady time per frame regardless of scene while the CUDA times fluctuate ever
so slightly on computer setup 2, but on setup 1 the fluctuation is greater. The cause for the fluctuation in setup 1 is unknown.

Although the scenes differ slightly from each other, they still follow a linear growth when the amount of particles increases. As an example, on setup 1 the gallery-scene with approximately 150000 particles required 25.4 ms per frame to compute the physics calculations using the proposed CUDA-implementation. In the same scenario using OpenMP, the time required was 183.1 ms . On setup 2 the corresponding values were 58.1 ms with CUDA and 124.6 ms with OpenMP.


Figure 7.3: The graph visualizes the computation time of the algorithm per frame on setup 2 for the CUDA-solution compared to OpenMP. All four tests scenes used a time-step of 3.5 ms and a particles spacing of 0.09 m . Measurements was taken over 1000 frames. The black horizontal dashed line denotes the 30 FPS mark.

As seen in Figure 7.4 the sequential CPU-solution also follows a linear growth rate and the times compared with the CUDA-solution is significantly slower. The same fluctuations can be observed for the CUDA-implementation as in Figure 7.2. Computer setup 2 was tested as well but the result was not as good as on setup 1 and is thus not included in this chapter.

When disabling OpenMP, the CPU-version required for the gallery-scene with approximately 150000 particles 582.6 ms to calculate the physics each frame.

Figure 7.5 show a linear growth for time spent in the majority of the kernels in the implementation except for FindGridCellStartEnd and DensityError which seems to be more or less constant during the experiment. All measurements can be directly mapped to the kernels in Algorithm 2. Note that these are the total execution times for a single frame, meaning that the kernels in the pressure solve procedure are the total execution time per frame and not per iteration.


Figure 7.4: The graph visualizes the computation time of the algorithm per frame on setup 1 for the CUDA-solution compared to the sequential CPU-implementation. All four tests scenes used a time-step of 3.5 ms and a particles spacing of 0.09 m . Measurements was taken over 1000 frames.


Figure 7.5: Visualizing the computation time for each kernel in each frame in the breaking dam scene. A time-step of 3.5 ms and particle spacing of 0.09 m was used. Measurements was taken over 300 frames on computer setup 1.

As such it is clear that the execution time for the advection prediction and pressure solve procedures are the majority of the total execution time each frame. Where pressure solve is the slower one of the two.

To show the cost of incompressibility the fine-grained approach presented was applied to SPH and measured with both setups, the results can be seen in Table 7.1. The results for both setups in Table 7.1 follow a linear growth rate just as IISPH does where setup 2 are slightly steeper than setup 1 .

| SPH CUDA | Setup 1 |  | Setup 2 |  |
| ---: | ---: | ---: | ---: | ---: |
| Particles | time (ms) | FPS | time (ms) | FPS |
| 7600 | 0.79 | 1268 | 1.42 | 707 |
| 20000 | 1.15 | 874 | 3.89 | 277 |
| 54000 | 3.19 | 329 | 6.90 | 146 |
| 103000 | 7.42 | 173 | 14.04 | 76 |
| 175000 | 16.55 | 64 | 22.19 | 46 |

Table 7.1: Table showing the results of a SPH implementation according the fine-grained approach presented in this thesis.

### 7.2 Memory usage



Figure 7.6: The memory usage in all scenes is growing linearly with the number of particles.
A similar linear growth in memory usage was detected in both the CPUand the GPU-implementation for all test scenes when the number of particles increased, see Figure 7.6. As an example the gallery-scene noted for approximately

150000 particles a usage of 126 MB on the CPU-versions and 59 MB on the GPU-version whereas the result in the breaking dam scene was 128 MB and 56 MB respectively.

### 7.3 Physical precision

The simple-scene was used when doing the image comparison. The program took a screen capture every 50 frame for each solution, sequential, OpenMP and CUDA. The boundary particles are not rendered while doing the comparisons since they remain constant throughout the simulation and they are not relevant for rendering, because they are only used during physics computations to get a better wall collision. For all the screen captures the camera's position and view direction are identical.

The results can be seen in Figures 7.7 and 7.8. There is no difference between the sequential and the OpenM- version as can be seen in the bottom row in Figure 7.7. There is however differences between the sequential and CUDA-version, see the bottom row in Figure 7.8, the most noticeable is the back section in frame 150 is quite scattered compared to the sequential and slight differences in the front.


Figure 7.7: Screen comparison of simple scene every 50 frame with 43000 fluid particles. This is frame $50-150$. Top row: sequential. Middle row: OpenMP. Bottom row: PSNR difference between top and middle. No difference was measured between the two. The fading of the bottom row is a result from the tool used and does not imply anything.


Figure 7.8: Screen comparison of simple scene every 50 frame with 43000 fluid particles. This is frame 50-150. Top row: sequential. Middle row: CUDA. Bottom row: PSNR difference between top and middle, note that red indicates difference, however, not how much it differs. The fading of the bottom row is a result from the tool used and does not imply anything.

### 7.4 Shared memory

The numbers in Table 7.2 are from an early development stage where a shared memory approach was explored for the first section of advection prediction. The difference between approaches is the kernel structure and how much preparations is needed. For the global approach an additional 94.6 ms is required for preparations once each frame, for such as finding neighbors. This is not needed in the shared memory approach. However similar differences between the other kernels was observed.

|  | Dimension |  |  |  |  |
| ---: | ---: | ---: | ---: | ---: | :---: |
| Approach | Grid | Block | Duration (ms) | Occupancy (\%) | Block limit reason |
| Global | $\{817,1,1\}$ | $\{256,1,1\}$ | 14.1 | 75 | Registers |
| Shared | $\{17251,1,1\}$ | $\{27,1,1\}$ | 129.8 | 25 | Blocks |

Table 7.2: Performance for first part of advection prediction with 220000 particles. Nsight's profiler was used for the numbers for the different approaches. The global approach is the proposed implementation and shared is the alternative approach.

## Chapter 8

## Analysis and Discussion

Based on the results certain conclusions can be made regarding the performance of the proposed implementation as well as the qualitative result.

### 8.1 Time usage

By averaging the measured time results, the usage of an average scene for a certain amount of particles can be compiled. For setup 1 this can be seen in Table 8.1 and for setup 2 in Table 8.2. Setup 1 achieved a speed-up of the parallel GPUsolution compared to the parallel CPU-version with a factor of $\sim 6$. In setup 2 the speed-up was lower than that of setup 2 with a speed-up factor of $\sim 2$.

| Setup 1 | Physics - GPU |  | Physics - CPU <br> (OpenMP) |  |  |
| ---: | ---: | ---: | ---: | ---: | :---: |
|  | Time (ms) | FPS | Time (ms) | FPS | Speedup |
| 7600 | 2.58 | 388 | 6.89 | 146 | 2.67 |
| 20000 | 4.06 | 247 | 22.18 | 45 | 5.47 |
| 54000 | 10.21 | 100 | 64.20 | 16 | 6.29 |
| 103000 | 21.07 | 49 | 126.80 | 8 | 6.02 |
| 175000 | 39.18 | 28 | 221.16 | 5 | 5.64 |

Table 8.1: The average time measured on computer setup 1 for each scene with a calculated speed-up between the GPU and CPU, OpenMP was activated.

Tables 8.1 and 8.2 show that depending on hardware setup the CUDA solution can compute $54000-103000$ particles while maintaining $\sim 45$ FPS. While the OpenMP solution on the CPU can only handle $20000-37000$ particles.

Calculations from Tables 8.1 and 8.2 show that real-time performance was achieved with CUDA for almost 154000 particles with 30 FPS on setup 1. The corresponding values for OpenMP on setup 2 (which had a better CPU) was approximately 39000 particles. The proposed solution can support up to about 4 times the amount of particles while running in real-time compared to the OpenMP-solution.

| Setup 2 | Physics - GPU |  | Physics - CPU (OpenMP) |  | Speedup |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Particles | Time (ms) | FPS | Time (ms) | FPS |  |
| 7600 | 4.58 | 219 | 5.34 | 188 | 1.17 |
| 20000 | 9.45 | 106 | 16.23 | 62 | 1.72 |
| 54000 | 23.18 | 43 | 46.23 | 22 | 1.99 |
| 103000 | 47.82 | 21 | 92.29 | 11 | 1.93 |
| 175000 | 83.06 | 12 | 161.06 | 6 | 1.94 |

Table 8.2: The average time measured on computer setup 2 for each scene with a calculated speed-up between the GPU and CPU, OpenMP was activated.

| Sequential CPU | Setup 1 |  | Setup 2 |  |
| ---: | ---: | ---: | ---: | ---: |
| Particles | Time (ms) | FPS | Time $(\mathrm{ms})$ | FPS |
| 7600 | 25.46 | 39 | 28.29 | 35 |
| 20000 | 72.91 | 14 | 86.24 | 12 |
| 54000 | 206.43 | 5 | 242.17 | 4 |
| 103000 | 409.60 | 2 | 478.97 | 2 |
| 175000 | 711.90 | 1 | 830.92 | 1 |

Table 8.3: The average time measured on both computer setups for the sequential CPU implementation.

As can be seen by comparing Tables 8.3 and 8.1 the performance is improved by a magnitude with CUDA compared to the sequential CPU-version. For realtime with 30 FPS the sequential CPU could at best handle approximately 9400 particles (calculated from Table 8.3 with setup 1). This is fewer than the CUDAimplementation with a factor of $\sim 19$.

The CPU time differences for OpenMP between the computer setups are probably mostly due to the CPU in setup 2 has two more cores than the CPU in setup 1, but also the additional $50 \%$ available cache memory. However, times measured on sequential CPU are faster on setup 1 because of the higher CPU frequency, even though it has fewer cores. This is because without parallelism (OpenMP), the program runs on one core which makes extra cores unnecessary. The differences between the GPUs however depend on numerous properties. For example the GPU in setup 1 can support twice the amount of CUDA blocks per multiprocessor which increases the possible parallelism accordingly.

The complexity of the scene had a marginal impact on the time measurements. While there exist minor deviations of computational time between scenes, though the particle count is identical, this can be caused by several factors. It may be that the allocated resources from the OS varied during the experiment. It is possible that the gallery-scene (which is more complex than the breaking dam) measured lower computation time due to it being constructed with a higher amount of static boundary particles. While these particles are still included in computing
the advection and pressure, they are being ignored in the integration process which results in fewer computations.

To get better times it is assumed that by excluding inactive boundary particles (boundary particles without an active fluid particle within its global support radius) from the computations the execution time is also reduced. It would not require any significant restructuring of the code-base to add the extra code needed. The saved time would most likely be more or less equal for each implementation which would not affect the overall speed-up gotten from the experiments.

With an increase of the particle count, it is the physics-kernels (DisplacementFactor, PredictDensity, Pressure, AdvectionFactor and SumPressureMovement in Figure 7.5) that are affected the most in terms of execution time. A trend is established for approximately more than 30000 particles where these kernels become dominant in execution time. This can be expected due to these kernels being heavily influenced of looping the neighbors of each particle and thus, adding a particle to the simulation will cause these kernels to increase their execution time.

There are two interesting paths to explore to increase the performance even more. First a shared memory approach which is capable of reaching $100 \%$ occupancy if the memory access to global memory turns out to be the major bottleneck. Secondly, to improve the proposed solution the number of registers used must be decreased as seen in Table 7.2 to reach a higher occupancy. Alternatively, if it is not a memory problem nor a register problem, a different algorithm structure or approach which includes the advection prediction and pressure solve procedures would be desired. This due to they are the procedures which takes up the majority of the execution time, as seen in Figure 7.5.

Compared with the numbers in Tables 8.1 and 8.2 it is obvious that there is a significant cost that comes with incompressibility, SPH runs on average 3.18 times as fast as compared with IISPH for setup 1 and 3.33 times for setup 2. However, since SPH would require smaller time-steps it would (for a given time-span) also need to process more frames than IISPH. IISPH can support a time-step up to 0.02 ms [3] while SPH can support to 0.0015 ms [20], which is a factor of up to approximately 13 time more frames required to simulate any given time-span. This would yield with e.g. 20000 particles a total execution time that would be 3.78 times as long for SPH than IISPH.

### 8.2 Memory usage

There are distinct similarities in the linear growth of the memory allocated between scenes in the CPU- and CUDA-versions respectively seen in Figure 7.6. This was expected due to allocations only depending on the amount of particles and the partitioning of the simulation domain into a uniform grid. An average memory usage for a scene depending on the number of particles can be compiled
and seen in Table 8.4.

| Particles | GPU (MB) | CPU (MB) |
| ---: | ---: | ---: |
| 7600 | 2.7 | 5.7 |
| 20000 | 7.3 | 15.6 |
| 54000 | 19.8 | 43.9 |
| 103000 | 38.1 | 86.2 |
| 175000 | 65.8 | 149.4 |

Table 8.4: Average memory usage for each scene depending on the total number of particles. In the test cases the CPU-versions utilized a little more than twice the amount of memory than that of the GPU-version.

As can be seen the CPU-versions utilize approximately twice the amount of memory than that of the CUDA-version. This can be explained by specific differences in how and what data is stored in the implementations.

In the CPU-versions padding occurs on the particle struct with 3 bytes per instance, which yields an additional usage of 0.5 MB for 175000 particles due to using AoS. This padding does not occur on the CUDA-version because of it following SoA. However it is only a fraction of the difference in memory usage between the implementations. Further, the CUDA-version allocates unused memory because of the need to use float4 instead of float3 to utilize the CUDA texture loads from global memory. While it was possible to merge certain variables to be stored in the same array to eliminate these empty allocations in the CUDA-version, some padding of this type could not be avoided.

The major variety however is caused by another difference in the implementations. The CPU-versions store certain neighbor data (such as distance between particle and neighbor, as well as kernel values) for each particle to reduce unnecessary repeated calculations. This data accounts for an additional 24 bytes of usage per neighbor of a particle. In the CUDA-implementation it was however considered that adding some extra computations in order to reduce memory bandwidth usage would be preferable. Averaging a particle to have 23 neighbors at any time this yields a decreased memory usage of 92.1 MB for 175000 particles.

It is assumed that the implementations would have similar memory usage if this neighbor data was not stored in the CPU-versions, however they would be required to perform more computations which would affect performance negatively. Further analysis would be necessary to confirm this however.

### 8.3 Physical precision

As can be seen in Figure 7.8 and in Table 8.5 the CUDA-solution deviate considerably from the sequential implementation while OpenMP does not deviate at all, see Figure 7.7. Note that the PSNR does not tell how large the total physical

|  | PSNR (dB) |  |
| ---: | :---: | :---: |
| Frame | Bottom, Figure 7.7 | Bottom, Figure 7.8 |
| 50 | $\infty$ | $\infty$ |
| 100 | $\infty$ | 35.2 |
| 150 | $\infty$ | 20.5 |

Table 8.5: The PSNR values from the comparisons between top and middle rows of Figures 7.7 and 7.8. In frame 100 the CUDA solution is still within the acceptable range. In frame 150 the value is below the threshold, this difference is visible when comparing the middle rows of Figures 7.7 and 7.8 for frame 150 .
error is, rather it conveys if there is a difference in the particles' positions relative to the camera.

The reason to the images being identical in the first 50 frames is because the particles are falling due to gravity. Since they are evenly spaced out when created they influence each other equally resulting in a standstill until the first particles hit the ground.

It is arguable if PSNR was a useful metric for the precision. As it tells if a pixel in an image differs from the original image but not to what extent, it only indicates if a deviation has occurred. Thus no conclusions can be made whether the error is within an acceptable range or not. It is also deemed to be subjective whether the differences seen between the middle rows of Figures 7.7 and 7.8 are acceptable or not.

### 8.4 Shared memory

There is a large difference in duration between the global and shared memory approach, approximately 9.2 times as much. Although there is a more expensive preparation stage for the global approach than the shared memory approach, the significant increase in duration between each kernel makes it less important for the overall time. As seen in Table 7.2 the occupancy for the kernel is 3 times as much for the global approach and the limiting factor is the registers used, whereas the shared memory approach implemented only had an occupancy of $25 \%$ and was limited by the number of blocks. The reason for the slower times could very well be because of mistakes in the implementation, however, it could also be that the shared memory described by Goswami et al. [13] no longer is a feasible solution for newer hardware where it seems to be worth more to run more particles in parallel than utilize memory efficiently for few particles at a time.

## Chapter 9

## Conclusions and Future Work

In summation, this thesis confirms that IISPH can be implemented as a parallel solution on the GPU using CUDA. As a proof-of-concept a global memory approach using SoA for data storage was proposed and implemented. An experimental approach using shared memory was investigated but the result from it was inferior to the global memory approach.

The proposed implementation achieved a positive speed-up compared to the sequential CPU-version as well as the parallel one. By using CUDA, a real-time performance was achieved for approximately 175000 particles. This was up to 4 times the amount of particles than that of using OpenMP and 19 times that of the sequential CPU-implementation.

We can conclude that the pressure solve procedure is the most time consuming section of the three procedures in the algorithm. The three most computational expensive kernels were the computeDisplacementFactor, predictDensity and computePressure, the latter two are found in the pressure solve procedure.

While the proposed solution did achieve a speed-up it however did alter the physical accuracy according to the PSNR. Why the visual outcome of the GPUversion was differing from the CPU-versions is not known. Even though the individual movements of the particles have been altered in the CUDA-solution, the overall behavior of the fluid is maintained. Due to this, the proposed solution is believed to maintain the nature of IISPH.

The memory usage differs, however, if the extra memory used to store precomputed values in the CPU-implementation is neglected, the deviation is minimal. As such our hypothesis stating that the memory usage is similar between implementations is supported.

We believe that the implementation can be seen as a stepping stone for future GPGPU-implementations, such as a shared memory implementation. We do not believe that the proposed implementation is sufficient to be fully utilized in video games and virtual reality applications which demand real-time computations. However, with improved implementations and hardware, we believe there could be potential for GPGPU-implementations of IISPH in these types of real-time applications.

### 9.1 Future work

While the proposed solution did achieve a positive improvement of performance, it accesses spatially closely located particles' data from global memory multiple times. Investigations on an approach to store this data in shared memory with only a single access from global memory would be worthwhile and probably the most viable step to improve the performance.

Further analysis is required to identify to why the CUDA-implementation differs in physical accuracy from the sequential CPU-version, whereas the OpenMPimplementation does not. A data comparison method could be utilized to verify if the difference of the computed values is within an acceptable range. Alternatively, it may be viable to investigate whether the differences are acceptable or not. If the deviation is deemed to be acceptable then it may not be necessary to make any further investigations.

The implementation was limited to compute capability 3.0. A viable step would be to improve by taking advantage of latest feature-sets to allow for better kernel launches and optimizations. This is however likely to be easy modifications which would only yield minor performance improvements.

It would also be viable to exclude the inactive boundary particles from the computations. Since there is no need to compute pressure values for boundary particles which will not affect fluid particles in a given frame, it would be viable to exclude them completely from the simulation of that frame.

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## Appendix A

## Additional Experiments Data

Following is the partial relevant data that was gathered during the experiments.
Table A1 (Setup 1 [CUDA \& OpenMP]) contains data of execution times on computer setup 1 for physics and rendering using the proposed CUDA-solution and OpenMP.

Table A2 (Setup 2 [CUDA \& OpenMP]) contains data of execution times on computer setup 2 for physics and rendering using the proposed CUDA-solution and OpenMP.

Table A3 (Setup $1 \& 2$ [single-thread CPU]) contains data of execution times on computer setups 1 and 2 for physics and rendering using the sequential CPUimplementation.

Table A4 (Memory usage [VRAM \& RAM]) contains data of memory usage on computer setup 1 for physics and rendering using the proposed CUDA-solution and the CPU-implementations.

| Setup 1 (CUDA \& OpenMP) |  |  |  |  | Time: physics [GPU] (ms) | Time: rendering [GPU] (ms) | Time: physics [CPU] (ms) | Time: rendering [CPU] (ms) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Scene | Frames | Particles | Spacing | Time-step |  |  |  |  |
| SIMPLE | 300 | 4288 | 0.09 | 0.0035 | 2.248935 | 13.469247 | 4.268302 | 12.184612 |
| SIMPLE | 300 | 5650 | 0.09 | 0.0035 | 2.472281 | 13.179368 | 5.780956 | 10.669256 |
| SIMPLE | 300 | 7948 | 0.09 | 0.0035 | 2.593857 | 13.063757 | 9.214053 | 7.375593 |
| SIMPLE | 300 | 9776 | 0.09 | 0.0035 | 2.523607 | 13.182771 | 11.220481 | 5.857633 |
| SIMPLE | 300 | 15554 | 0.09 | 0.0035 | 3.344905 | 12.248573 | 17.094330 | 2.300213 |
| SIMPLE | 300 | 20972 | 0.09 | 0.0035 | 4.198549 | 11.455010 | 25.037664 | 3.386557 |
| SIMPLE | 300 | 32568 | 0.09 | 0.0035 | 6.276952 | 9.340478 | 39.546911 | 5.170774 |
| SIMPLE | 300 | 43825 | 0.09 | 0.0035 | 8.004032 | 7.670774 | 54.568949 | 7.689797 |
| SIMPLE | 300 | 57362 | 0.09 | 0.0035 | 10.264237 | 5.764541 | 64.831025 | 11.989330 |
| SIMPLE | 300 | 71890 | 0.09 | 0.0035 | 12.850800 | 3.763618 | 91.233588 | 13.812187 |
| SIMPLE | 300 | 89723 | 0.09 | 0.0035 | 17.900671 | 1.806938 | 116.450923 | 18.156967 |
| SIMPLE | 300 | 110754 | 0.09 | 0.0035 | 21.177983 | 2.177495 | 147.114191 | 23.174895 |
| SIMPLE | 300 | 132478 | 0.09 | 0.0035 | 28.837132 | 1.714149 | 175.204491 | 28.679991 |
| SIMPLE | 300 | 159523 | 0.09 | 0.0035 | 29.745489 | 1.306056 | 207.868697 | 35.992826 |
| SIMPLE | 300 | 189042 | 0.09 | 0.0035 | 36.415105 | 0.150745 | 249.727931 | 44.783583 |
| SIMPLE | 1000 | 4288 | 0.09 | 0.0035 | 2.242683 | 14.163314 | 17.889968 | 10.578171 |
| SIMPLE | 1000 | 5650 | 0.09 | 0.0035 | 2.341580 | 13.416295 | 18.269835 | 10.220225 |
| SIMPLE | 1000 | 7948 | 0.09 | 0.0035 | 2.483381 | 13.259445 | 7.986275 | 8.677942 |
| SIMPLE | 1000 | 9776 | 0.09 | 0.0035 | 2.570378 | 13.163953 | 16.954982 | 6.653696 |
| SIMPLE | 1000 | 15554 | 0.09 | 0.0035 | 3.276622 | 12.437155 | 17.662175 | 2.195612 |
| SIMPLE | 1000 | 20972 | 0.09 | 0.0035 | 4.287971 | 11.423180 | 25.764662 | 3.378650 |
| SIMPLE | 1000 | 32568 | 0.09 | 0.0035 | 6.204666 | 9.505436 | 42.499844 | 5.213715 |
| SIMPLE | 1000 | 43825 | 0.09 | 0.0035 | 7.509002 | 8.230111 | 54.358247 | 7.637247 |
| SIMPLE | 1000 | 57362 | 0.09 | 0.0035 | 11.551832 | 8.258636 | 51.805731 | 14.263311 |
| SIMPLE | 1000 | 71890 | 0.09 | 0.0035 | 17.656177 | 7.340355 | 89.420650 | 13.410000 |
| SIMPLE | 1000 | 89723 | 0.09 | 0.0035 | 23.635443 | 5.345737 | 111.417195 | 17.794919 |
| SIMPLE | 1000 | 110754 | 0.09 | 0.0035 | 31.996238 | 5.541827 | 139.359253 | 22.875106 |
| SIMPLE | 1000 | 132478 | 0.09 | 0.0035 | 31.418370 | 3.348619 | 167.868256 | 28.186616 |
| SIMPLE | 1000 | 159523 | 0.09 | 0.0035 | 40.680696 | 1.777909 | 203.634635 | 35.487840 |
| SIMPLE | 1000 | 189042 | 0.09 | 0.0035 | 48.974512 | 0.154148 | 244.242066 | 43.716657 |
| BREAKING_DAM | 300 | 3965 | 0.09 | 0.0035 | 2.201143 | 17.238369 | 3.454120 | 12.961759 |
| BREAKING_DAM | 300 | 5225 | 0.09 | 0.0035 | 2.341406 | 13.357940 | 4.623344 | 11.816158 |
| BREAKING_DAM | 300 | 7173 | 0.09 | 0.0035 | 2.438271 | 13.251337 | 6.425576 | 10.019831 |
| BREAKING_DAM | 300 | 9055 | 0.09 | 0.0035 | 2.548236 | 13.126017 | 8.365140 | 8.141726 |
| BREAKING_DAM | 300 | 14089 | 0.09 | 0.0035 | 3.051888 | 12.614225 | 14.487726 | 2.544145 |
| BREAKING_DAM | 300 | 19487 | 0.09 | 0.0035 | 3.967958 | 11.678625 | 21.993941 | 2.827219 |
| BREAKING_DAM | 300 | 31054 | 0.09 | 0.0035 | 5.944228 | 9.734457 | 37.289243 | 4.882897 |
| BREAKING_DAM | 300 | 41259 | 0.09 | 0.0035 | 7.389714 | 8.295574 | 50.292241 | 6.931067 |
| BREAKING_DAM | 300 | 53539 | 0.09 | 0.0035 | 9.471145 | 6.488437 | 65.908352 | 9.329675 |
| BREAKING_DAM | 300 | 68416 | 0.09 | 0.0035 | 12.837727 | 4.020064 | 84.932637 | 12.495220 |
| BREAKING_DAM | 300 | 83822 | 0.09 | 0.0035 | 15.575995 | 1.244797 | 105.082205 | 16.127214 |
| BREAKING_DAM | 300 | 103463 | 0.09 | 0.0035 | 20.223377 | 0.194287 | 131.268777 | 20.987790 |
| BREAKING_DAM | 300 | 125836 | 0.09 | 0.0035 | 22.630269 | 0.142737 | 160.728293 | 26.476872 |
| BREAKING_DAM | 300 | 149168 | 0.09 | 0.0035 | 29.653967 | 0.730201 | 192.511343 | 32.838191 |
| BREAKING_DAM | 300 | 176699 | 0.09 | 0.0035 | 32.961099 | 0.153147 | 231.291419 | 39.692685 |
| BREAKING_DAM | 1000 | 3965 | 0.09 | 0.0035 | 2.254822 | 14.080434 | 3.519283 | 12.983380 |
| BREAKING_DAM | 1000 | 5225 | 0.09 | 0.0035 | 2.352432 | 13.409789 | 4.853065 | 11.767811 |
| BREAKING_DAM | 1000 | 7173 | 0.09 | 0.0035 | 2.449202 | 13.300184 | 6.371324 | 10.127535 |
| BREAKING_DAM | 1000 | 9055 | 0.09 | 0.0035 | 2.562108 | 13.182371 | 8.318996 | 8.210492 |
| BREAKING_DAM | 1000 | 14089 | 0.09 | 0.0035 | 3.059666 | 12.670379 | 14.459799 | 2.520923 |
| BREAKING_DAM | 1000 | 19487 | 0.09 | 0.0035 | 3.987563 | 11.722968 | 21.949598 | 2.817410 |
| BREAKING_DAM | 1000 | 31054 | 0.09 | 0.0035 | 6.044994 | 9.671596 | 37.011075 | 4.737858 |
| BREAKING_DAM | 1000 | 41259 | 0.09 | 0.0035 | 7.679974 | 8.098284 | 49.870636 | 6.861600 |
| BREAKING_DAM | 1000 | 53539 | 0.09 | 0.0035 | 16.728078 | 10.981454 | 58.012977 | 10.930911 |
| BREAKING_DAM | 1000 | 68416 | 0.09 | 0.0035 | 15.875887 | 10.716800 | 84.366994 | 12.476402 |
| BREAKING_DAM | 1000 | 83822 | 0.09 | 0.0035 | 14.543119 | 2.880770 | 103.688565 | 16.059449 |
| BREAKING_DAM | 1000 | 103463 | 0.09 | 0.0035 | 33.800248 | 4.346278 | 129.807072 | 20.716530 |
| BREAKING_DAM | 1000 | 125836 | 0.09 | 0.0035 | 44.351176 | 3.840591 | 158.790029 | 26.317518 |
| BREAKING_DAM | 1000 | 149168 | 0.09 | 0.0035 | 28.351539 | 1.042401 | 191.421595 | 31.887577 |
| BREAKING_DAM | 1000 | 176699 | 0.09 | 0.0035 | 33.355676 | 0.254645 | 228.588220 | 39.077294 |
| TWO_BLOCKS | 300 | 4162 | 0.09 | 0.0035 | 2.230546 | 15.062879 | 3.686343 | 12.730236 |
| TWO_BLOCKS | 300 | 5418 | 0.09 | 0.0035 | 2.383969 | 13.295379 | 4.870081 | 11.641590 |
| TWO_BLOCKS | 300 | 7498 | 0.09 | 0.0035 | 2.462652 | 13.202590 | 6.692833 | 9.728651 |
| TWO_BLOCKS | 300 | 9456 | 0.09 | 0.0035 | 2.759705 | 12.894594 | 8.622288 | 7.812309 |
| TWO_BLOCKS | 300 | 14666 | 0.09 | 0.0035 | 3.133483 | 12.504219 | 14.657088 | 2.505509 |


| TWO_BLOCKS | 300 | 20272 | 0.09 | 0.0035 | 4.120137 | 11.507461 | 22.418148 | 3.061745 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| TWO_BLOCKS | 300 | 31922 | 0.09 | 0.0035 | 6.024593 | 9.589918 | 37.091853 | 4.900414 |
| TWO_BLOCKS | 300 | 42704 | 0.09 | 0.0035 | 8.201786 | 7.629633 | 50.539779 | 7.160187 |
| TWO_BLOCKS | 300 | 55304 | 0.09 | 0.0035 | 13.969603 | 11.345505 | 65.918661 | 9.835862 |
| TWO_BLOCKS | 300 | 70004 | 0.09 | 0.0035 | 18.661212 | 14.277523 | 83.877223 | 12.630450 |
| TWO_BLOCKS | 300 | 85698 | 0.09 | 0.0035 | 15.121357 | 8.600767 | 103.232327 | 16.302583 |
| TWO_BLOCKS | 300 | 106380 | 0.09 | 0.0035 | 18.145589 | 0.140635 | 130.130482 | 21.161258 |
| TWO_BLOCKS | 300 | 128360 | 0.09 | 0.0035 | 33.812315 | 3.479748 | 157.958730 | 26.807490 |
| TWO_BLOCKS | 300 | 152052 | 0.09 | 0.0035 | 36.209479 | 3.109489 | 189.378329 | 32.483950 |
| TWO_BLOCKS | 300 | 181056 | 0.09 | 0.0035 | 56.472420 | 0.471453 | 227.167754 | 40.070950 |
| TWO_BLOCKS | 1000 | 4162 | 0.09 | 0.0035 | 3.355358 | 13.683052 | 3.795848 | 12.727834 |
| TWO_BLOCKS | 1000 | 5418 | 0.09 | 0.0035 | 2.395146 | 13.343426 | 4.940949 | 11.598348 |
| TWO_BLOCKS | 1000 | 7498 | 0.09 | 0.0035 | 2.487922 | 13.243630 | 6.990219 | 9.645171 |
| TWO_BLOCKS | 1000 | 9456 | 0.09 | 0.0035 | 2.608105 | 13.116808 | 8.848005 | 7.694396 |
| TWO_BLOCKS | 1000 | 14666 | 0.09 | 0.0035 | 3.167942 | 12.546159 | 15.061477 | 2.348658 |
| TWO_BLOCKS | 1000 | 20272 | 0.09 | 0.0035 | 4.186237 | 11.513967 | 22.909420 | 3.087069 |
| TWO_BLOCKS | 1000 | 31922 | 0.09 | 0.0035 | 6.209261 | 9.493725 | 37.559602 | 4.949861 |
| TWO_BLOCKS | 1000 | 42704 | 0.09 | 0.0035 | 8.626104 | 7.318134 | 51.148864 | 7.283706 |
| TWO_BLOCKS | 1000 | 55304 | 0.09 | 0.0035 | 13.069616 | 11.173338 | 66.035673 | 9.788416 |
| TWO_BLOCKS | 1000 | 70004 | 0.09 | 0.0035 | 21.177088 | 10.779363 | 84.567887 | 12.844857 |
| TWO_BLOCKS | 1000 | 85698 | 0.09 | 0.0035 | 22.782838 | 9.022175 | 104.078841 | 16.449924 |
| TWO_BLOCKS | 1000 | 106380 | 0.09 | 0.0035 | 31.129338 | 8.721983 | 131.176487 | 21.667845 |
| TWO_BLOCKS | 1000 | 128360 | 0.09 | 0.0035 | 42.003998 | 3.551714 | 158.621367 | 26.786769 |
| TWO_BLOCKS | 1000 | 152052 | 0.09 | 0.0035 | 58.951295 | 2.833925 | 189.778515 | 32.612674 |
| TWO_BLOCKS | 1000 | 181056 | 0.09 | 0.0035 | 32.476677 | 0.354641 | 228.138787 | 40.482345 |
| GALLERY | 300 | 4450 | 0.09 | 0.0035 | 3.190760 | 15.052569 | 3.922270 | 12.522937 |
| GALLERY | 300 | 5626 | 0.09 | 0.0035 | 2.398090 | 13.294379 | 4.846358 | 11.611861 |
| GALLERY | 300 | 7802 | 0.09 | 0.0035 | 3.205151 | 12.481297 | 6.857592 | 9.594022 |
| GALLERY | 300 | 9592 | 0.09 | 0.0035 | 2.605574 | 13.067560 | 8.572540 | 7.973664 |
| GALLERY | 300 | 14598 | 0.09 | 0.0035 | 3.129832 | 12.534748 | 14.188038 | 2.589689 |
| GALLERY | 300 | 19376 | 0.09 | 0.0035 | 3.882021 | 11.768512 | 20.312624 | 2.427435 |
| GALLERY | 300 | 29170 | 0.09 | 0.0035 | 5.364282 | 10.316116 | 32.689521 | 3.752810 |
| GALLERY | 300 | 38416 | 0.09 | 0.0035 | 6.675506 | 8.977029 | 43.945540 | 5.161565 |
| GALLERY | 300 | 49410 | 0.09 | 0.0035 | 8.308464 | 7.505314 | 56.819815 | 7.147275 |
| GALLERY | 300 | 61388 | 0.09 | 0.0035 | 11.924198 | 7.673377 | 70.931680 | 8.821386 |
| GALLERY | 300 | 74385 | 0.09 | 0.0035 | 13.199854 | 5.118321 | 87.070392 | 11.517479 |
| GALLERY | 300 | 91618 | 0.09 | 0.0035 | 19.848427 | 3.764120 | 108.530720 | 14.783822 |
| GALLERY | 300 | 108848 | 0.09 | 0.0035 | 18.541126 | 2.280794 | 129.645316 | 18.108120 |
| GALLERY | 300 | 128099 | 0.09 | 0.0035 | 39.742483 | 4.216252 | 153.990116 | 22.286539 |
| GALLERY | 300 | 151586 | 0.09 | 0.0035 | 25.749033 | 2.771464 | 184.459802 | 27.649299 |
| GALLERY | 1000 | 4450 | 0.09 | 0.0035 | 3.350924 | 12.418036 | 4.004549 | 12.497312 |
| GALLERY | 1000 | 5626 | 0.09 | 0.0035 | 2.418512 | 13.334817 | 5.311905 | 11.457813 |
| GALLERY | 1000 | 7802 | 0.09 | 0.0035 | 3.303592 | 12.442659 | 7.037364 | 9.583311 |
| GALLERY | 1000 | 9592 | 0.09 | 0.0035 | 2.629064 | 13.105397 | 8.605672 | 7.958850 |
| GALLERY | 1000 | 14598 | 0.09 | 0.0035 | 3.140309 | 12.585597 | 14.391533 | 2.465570 |
| GALLERY | 1000 | 19376 | 0.09 | 0.0035 | 3.943328 | 11.771815 | 20.784378 | 2.314927 |
| GALLERY | 1000 | 29170 | 0.09 | 0.0035 | 5.460632 | 10.266568 | 32.760790 | 3.558623 |
| GALLERY | 1000 | 38416 | 0.09 | 0.0035 | 6.684185 | 9.070218 | 43.859358 | 5.002512 |
| GALLERY | 1000 | 49410 | 0.09 | 0.0035 | 13.673903 | 7.258576 | 56.677478 | 6.847186 |
| GALLERY | 1000 | 61388 | 0.09 | 0.0035 | 12.176595 | 6.633175 | 71.022267 | 8.706575 |
| GALLERY | 1000 | 74385 | 0.09 | 0.0035 | 26.266393 | 9.161805 | 86.401850 | 11.259331 |
| GALLERY | 1000 | 91618 | 0.09 | 0.0035 | 23.890609 | 8.039227 | 107.876491 | 14.612156 |
| GALLERY | 1000 | 108848 | 0.09 | 0.0035 | 29.158459 | 6.739578 | 128.798301 | 17.872693 |
| GALLERY | 1000 | 128099 | 0.09 | 0.0035 | 44.064187 | 5.161362 | 153.058320 | 22.214370 |
| GALLERY | 1000 | 151586 | 0.09 | 0.0035 | 25.406326 | 1.101259 | 183.138934 | 27.225391 |


| Setup 2 (CUDA \& OpenMIP) |  |  |  |  | Time: physics [GPU] (ms) | Time: rendering [GPU] (ms) | Time: physics [CPU] (ms) | Time: rendering [CPU1 (ms) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Scene | Frames | Particles | Spacing | Time-step |  |  |  |  |
| SIMPLE | 300 | 4288 | 0.09 | 0.0035 | 3.357967 | 12.05651 | 3.026798 | 13.099016 |
| SIMPLE | 300 | 5650 | 0.09 | 0.0035 | 3.621356 | 11.791873 | 3.990074 | 12.288427 |
| SIMPLE | 300 | 7948 | 0.09 | 0.0035 | 4.662431 | 10.572622 | 5.751108 | 10.554658 |
| SIMPLE | 300 | 9776 | 0.09 | 0.0035 | 5.634961 | 9.739258 | 7.204202 | 9.136849 |
| SIMPLE | 300 | 15554 | 0.09 | 0.0035 | 7.111207 | 8.319203 | 12.411283 | 3.931052 |
| SIMPLE | 300 | 20972 | 0.09 | 0.0035 | 9.106135 | 6.458088 | 17.441939 | 5.107641 |
| SIMPLE | 300 | 32568 | 0.09 | 0.0035 | 13.50496 | 2.042992 | 27.863477 | 8.521931 |
| SIMPLE | 300 | 43825 | 0.09 | 0.0035 | 18.672306 | 0.328791 | 38.249731 | 12.513929 |
| SIMPLE | 300 | 57362 | 0.09 | 0.0035 | 24.312019 | 0.389096 | 50.023962 | 17.401201 |
| SIMPLE | 300 | 71890 | 0.09 | 0.0035 | 33.483269 | 0.475704 | 63.999325 | 22.328248 |
| SIMPLE | 300 | 89723 | 0.09 | 0.0035 | 40.686855 | 0.520612 | 80.91167 | 29.820824 |
| SIMPLE | 300 | 110754 | 0.09 | 0.0035 | 52.713871 | 0.550123 | 101.234777 | 38.091911 |
| SIMPLE | 300 | 132478 | 0.09 | 0.0035 | 60.075089 | 0.523178 | 122.227333 | 46.754661 |
| SIMPLE | 300 | 159523 | 0.09 | 0.0035 | 73.461044 | 0.88565 | 149.104439 | 58.666823 |
| SIMPLE | 300 | 189042 | 0.09 | 0.0035 | 94.957253 | 1.001127 | 177.580268 | 71.636569 |
| SIMPLE | 1000 | 4288 | 0.09 | 0.0035 | 3.311753 | 12.188667 | 3.098009 | 12.997973 |
| SIMPLE | 1000 | 5650 | 0.09 | 0.0035 | 3.728399 | 11.7614 | 4.074437 | 12.294201 |
| SIMPLE | 1000 | 7948 | 0.09 | 0.0035 | 4.651156 | 10.816087 | 5.811413 | 10.554979 |
| SIMPLE | 1000 | 9776 | 0.09 | 0.0035 | 5.800931 | 9.688897 | 7.314227 | 9.061789 |
| SIMPLE | 1000 | 15554 | 0.09 | 0.0035 | 7.147046 | 8.412227 | 12.656993 | 3.625357 |
| SIMPLE | 1000 | 20972 | 0.09 | 0.0035 | 9.159836 | 6.337478 | 17.893264 | 5.090961 |
| SIMPLE | 1000 | 32568 | 0.09 | 0.0035 | 13.316824 | 2.285175 | 27.752811 | 8.35513 |
| SIMPLE | 1000 | 43825 | 0.09 | 0.0035 | 18.580275 | 0.340338 | 38.233051 | 12.432774 |
| SIMPLE | 1000 | 57362 | 0.09 | 0.0035 | 24.739269 | 0.390699 | 49.980657 | 17.488451 |
| SIMPLE | 1000 | 71890 | 0.09 | 0.0035 | 34.157181 | 0.425343 | 64.081122 | 22.157277 |
| SIMPLE | 1000 | 89723 | 0.09 | 0.0035 | 40.550907 | 0.50746 | 81.104454 | 29.435898 |
| SIMPLE | 1000 | 110754 | 0.09 | 0.0035 | 48.952339 | 0.535367 | 101.724916 | 37.814765 |
| SIMPLE | 1000 | 132478 | 0.09 | 0.0035 | 58.485191 | 0.556217 | 122.308809 | 46.285693 |
| SIMPLE | 1000 | 159523 | 0.09 | 0.0035 | 71.10099 | 0.961352 | 149.214784 | 58.184383 |
| SIMPLE | 1000 | 189042 | 0.09 | 0.0035 | 85.640785 | 0.98573 | 177.775939 | 71.30874 |
| BREAKING_DAM | 300 | 3965 | 0.09 | 0.0035 | 3.313157 | 12.217216 | 2.845883 | 13.226363 |
| BREAKING_DAM | 300 | 5225 | 0.09 | 0.0035 | 3.648968 | 11.810157 | 3.725117 | 12.542478 |
| BREAKING_DAM | 300 | 7173 | 0.09 | 0.0035 | 4.251536 | 11.215127 | 4.945652 | 11.399891 |
| BREAKING_DAM | 300 | 9055 | 0.09 | 0.0035 | 5.042572 | 10.361233 | 6.531545 | 9.850245 |
| BREAKING_DAM | 300 | 14089 | 0.09 | 0.0035 | 6.521958 | 8.944066 | 10.986417 | 5.337634 |
| BREAKING_DAM | 300 | 19487 | 0.09 | 0.0035 | 10.128682 | 6.536677 | 16.129022 | 4.418624 |
| BREAKING_DAM | 300 | 31054 | 0.09 | 0.0035 | 12.904405 | 2.676836 | 26.561787 | 8.395226 |
| BREAKING_DAM | 300 | 41259 | 0.09 | 0.0035 | 17.486607 | 0.338414 | 36.245552 | 11.335737 |
| BREAKING_DAM | 300 | 53539 | 0.09 | 0.0035 | 25.360052 | 0.397115 | 47.30318 | 15.363662 |
| BREAKING_DAM | 300 | 68416 | 0.09 | 0.0035 | 29.985325 | 0.400964 | 61.416795 | 20.633934 |
| BREAKING_DAM | 300 | 83822 | 0.09 | 0.0035 | 36.886059 | 0.506498 | 76.400985 | 26.813593 |
| BREAKING_DAM | 300 | 103463 | 0.09 | 0.0035 | 52.243568 | 0.546915 | 95.240524 | 34.395664 |
| BREAKING_DAM | 300 | 125836 | 0.09 | 0.0035 | 59.358273 | 0.567444 | 117.161713 | 43.31086 |
| BREAKING_DAM | 300 | 149168 | 0.09 | 0.0035 | 70.370201 | 0.962314 | 140.224848 | 53.171049 |
| BREAKING_DAM | 300 | 176699 | 0.09 | 0.0035 | 92.228828 | 1.003693 | 168.025454 | 65.092834 |
| BREAKING_DAM | 1000 | 3965 | 0.09 | 0.0035 | 3.307386 | 12.253784 | 2.79905 | 13.326122 |
| BREAKING_DAM | 1000 | 5225 | 0.09 | 0.0035 | 3.603721 | 11.909596 | 3.698172 | 12.689391 |
| BREAKING_DAM | 1000 | 7173 | 0.09 | 0.0035 | 4.309541 | 11.242071 | 4.937632 | 11.473989 |
| BREAKING_DAM | 1000 | 9055 | 0.09 | 0.0035 | 5.075775 | 10.463559 | 6.508449 | 9.903814 |
| BREAKING_DAM | 1000 | 14089 | 0.09 | 0.0035 | 6.49544 | 9.100923 | 10.881845 | 5.475887 |
| BREAKING_DAM | 1000 | 19487 | 0.09 | 0.0035 | 11.00409 | 6.370839 | 16.110417 | 4.39168 |
| BREAKING_DAM | 1000 | 31054 | 0.09 | 0.0035 | 12.8311 | 2.795522 | 26.351682 | 7.715191 |
| BREAKING_DAM | 1000 | 41259 | 0.09 | 0.0035 | 17.307695 | 0.327828 | 35.78717 | 11.201013 |
| BREAKING_DAM | 1000 | 53539 | 0.09 | 0.0035 | 25.41254 | 0.384284 | 46.938783 | 15.174407 |
| BREAKING_DAM | 1000 | 68416 | 0.09 | 0.0035 | 29.218731 | 0.397756 | 60.802198 | 20.402979 |
| BREAKING_DAM | 1000 | 83822 | 0.09 | 0.0035 | 35.877808 | 0.51163 | 76.21173 | 26.463952 |
| BREAKING_DAM | 1000 | 103463 | 0.09 | 0.0035 | 45.702606 | 0.54467 | 94.351025 | 33.917714 |
| BREAKING_DAM | 1000 | 125836 | 0.09 | 0.0035 | 56.870388 | 0.543066 | 116.323538 | 42.793777 |
| BREAKING_DAM | 1000 | 149168 | 0.09 | 0.0035 | 65.036209 | 0.693828 | 139.409768 | 52.423652 |
| BREAKING_DAM | 1000 | 176699 | 0.09 | 0.0035 | 80.91629 | 0.881479 | 167.42497 | 64.2383 |
| TWO_BLOCKS | 300 | 4162 | 0.09 | 0.0035 | 3.370628 | 12.104946 | 2.94853 | 13.107677 |
| TWO_BLOCKS | 300 | 5418 | 0.09 | 0.0035 | 3.697771 | 11.724511 | 3.779969 | 12.486985 |
| TWO_BLOCKS | 300 | 7498 | 0.09 | 0.0035 | 4.65298 | 10.792671 | 5.156398 | 11.152576 |
| TWO_BLOCKS | 300 | 9456 | 0.09 | 0.0035 | 5.419012 | 10.043991 | 6.776935 | 9.563796 |
| TWO_BLOCKS | 300 | 14666 | 0.09 | 0.0035 | 6.924841 | 8.637088 | 11.144557 | 5.124321 |


| TWO_BLOCKS | 300 | 20272 | 0.09 | 0.0035 | 8.846799 | 6.653117 | 16.337202 | 4.672996 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| TWO_BLOCKS | 300 | 31922 | 0.09 | 0.0035 | 12.969267 | 2.564566 | 26.296189 | 8.013508 |
| TWO_BLOCKS | 300 | 42704 | 0.09 | 0.0035 | 19.464207 | 0.326545 | 35.902006 | 11.696925 |
| TWO_BLOCKS | 300 | 55304 | 0.09 | 0.0035 | 22.398964 | 0.387812 | 47.07447 | 15.693415 |
| TWO_BLOCKS | 300 | 70004 | 0.09 | 0.0035 | 33.236233 | 0.397756 | 60.299549 | 20.820302 |
| TWO_BLOCKS | 300 | 85698 | 0.09 | 0.0035 | 38.129269 | 0.505215 | 74.569701 | 26.803649 |
| TWO_BLOCKS | 300 | 106380 | 0.09 | 0.0035 | 48.756798 | 0.536971 | 94.241963 | 34.76423 |
| TWO_BLOCKS | 300 | 128360 | 0.09 | 0.0035 | 54.971565 | 0.559425 | 114.619921 | 43.125134 |
| TWO_BLOCKS | 300 | 152052 | 0.09 | 0.0035 | 67.040535 | 0.895914 | 137.482895 | 53.168162 |
| TWO_BLOCKS | 300 | 181056 | 0.09 | 0.0035 | 80.524124 | 0.993749 | 165.434584 | 65.285297 |
| TWO_BLOCKS | 1000 | 4162 | 0.09 | 0.0035 | 3.604253 | 11.881689 | 2.97772 | 13.136867 |
| TWO_BLOCKS | 1000 | 5418 | 0.09 | 0.0035 | 3.750336 | 11.76974 | 3.83867 | 12.540874 |
| TWO_BLOCKS | 1000 | 7498 | 0.09 | 0.0035 | 8.640626 | 6.961058 | 5.320313 | 11.076553 |
| TWO_BLOCKS | 1000 | 9456 | 0.09 | 0.0035 | 5.755675 | 9.751768 | 6.899149 | 9.844792 |
| TWO_BLOCKS | 1000 | 14666 | 0.09 | 0.0035 | 6.968998 | 8.615596 | 11.567333 | 4.764416 |
| TWO_BLOCKS | 1000 | 20272 | 0.09 | 0.0035 | 9.169113 | 6.463541 | 16.654445 | 4.729452 |
| TWO_BLOCKS | 1000 | 31922 | 0.09 | 0.0035 | 13.066149 | 2.539867 | 26.663793 | 8.10589 |
| TWO_BLOCKS | 1000 | 42704 | 0.09 | 0.0035 | 20.338459 | 0.345471 | 36.454053 | 11.819139 |
| TWO_BLOCKS | 1000 | 55304 | 0.09 | 0.0035 | 23.398626 | 0.400964 | 47.457791 | 15.929181 |
| TWO_BLOCKS | 1000 | 70004 | 0.09 | 0.0035 | 31.196497 | 0.406096 | 60.917675 | 21.072749 |
| TWO_BLOCKS | 1000 | 85698 | 0.09 | 0.0035 | 38.008766 | 0.510668 | 75.099295 | 27.123137 |
| TWO_BLOCKS | 1000 | 106380 | 0.09 | 0.0035 | 48.919518 | 0.542424 | 94.657683 | 35.16359 |
| TWO_BLOCKS | 1000 | 128360 | 0.09 | 0.0035 | 55.035233 | 0.558463 | 115.345185 | 43.730429 |
| TWO_BLOCKS | 1000 | 152052 | 0.09 | 0.0035 | 65.253983 | 0.826628 | 138.05066 | 53.491178 |
| TWO_BLOCKS | 1000 | 181056 | 0.09 | 0.0035 | 84.76133 | 0.99407 | 166.550868 | 66.093962 |
| GALLERY | 300 | 4450 | 0.09 | 0.0035 | 3.60334 | 11.948089 | 3.103783 | 12.990916 |
| GALLERY | 300 | 5626 | 0.09 | 0.0035 | 3.758291 | 11.756909 | 3.809159 | 12.473192 |
| GALLERY | 300 | 7802 | 0.09 | 0.0035 | 4.736365 | 10.699647 | 5.493208 | 10.876713 |
| GALLERY | 300 | 9592 | 0.09 | 0.0035 | 5.418283 | 10.01031 | 6.617191 | 9.749202 |
| GALLERY | 300 | 14598 | 0.09 | 0.0035 | 7.054163 | 8.705412 | 10.853297 | 5.49385 |
| GALLERY | 300 | 19376 | 0.09 | 0.0035 | 9.724667 | 6.971964 | 15.003435 | 3.491916 |
| GALLERY | 300 | 29170 | 0.09 | 0.0035 | 11.584375 | 3.956393 | 23.052549 | 5.67701 |
| GALLERY | 300 | 38416 | 0.09 | 0.0035 | 15.101686 | 0.522216 | 31.196612 | 8.14727 |
| GALLERY | 300 | 49410 | 0.09 | 0.0035 | 20.64867 | 0.349961 | 40.515338 | 11.084252 |
| GALLERY | 300 | 61388 | 0.09 | 0.0035 | 26.868971 | 0.416361 | 50.959972 | 14.364138 |
| GALLERY | 300 | 74385 | 0.09 | 0.0035 | 30.046797 | 0.408983 | 62.452566 | 18.517485 |
| GALLERY | 300 | 91618 | 0.09 | 0.0035 | 37.557682 | 0.508743 | 78.457129 | 24.18006 |
| GALLERY | 300 | 108848 | 0.09 | 0.0035 | 49.207813 | 0.553972 | 93.47147 | 29.471824 |
| GALLERY | 300 | 128099 | 0.09 | 0.0035 | 53.260437 | 0.556538 | 111.110042 | 36.285969 |
| GALLERY | 300 | 151586 | 0.09 | 0.0035 | 64.533104 | 0.763756 | 133.219203 | 44.943586 |
| GALLERY | 1000 | 4450 | 0.09 | 0.0035 | 3.651572 | 11.97343 | 3.090311 | 13.070788 |
| GALLERY | 1000 | 5626 | 0.09 | 0.0035 | 3.784943 | 11.743437 | 3.813329 | 12.60984 |
| GALLERY | 1000 | 7802 | 0.09 | 0.0035 | 5.264343 | 10.295154 | 5.366183 | 11.074629 |
| GALLERY | 1000 | 9592 | 0.09 | 0.0035 | 5.628757 | 9.945835 | 6.711498 | 9.728352 |
| GALLERY | 1000 | 14598 | 0.09 | 0.0035 | 7.14989 | 8.709261 | 10.910073 | 5.487755 |
| GALLERY | 1000 | 19376 | 0.09 | 0.0035 | 9.30679 | 6.922244 | 15.079779 | 3.470104 |
| GALLERY | 1000 | 29170 | 0.09 | 0.0035 | 11.426493 | 4.064814 | 23.105156 | 5.644612 |
| GALLERY | 1000 | 38416 | 0.09 | 0.0035 | 15.123842 | 0.584766 | 31.115136 | 8.063869 |
| GALLERY | 1000 | 49410 | 0.09 | 0.0035 | 21.011576 | 0.347075 | 40.325442 | 10.993474 |
| GALLERY | 1000 | 61388 | 0.09 | 0.0035 | 26.650871 | 0.401606 | 50.705921 | 14.120994 |
| GALLERY | 1000 | 74385 | 0.09 | 0.0035 | 29.755447 | 0.40353 | 61.942219 | 18.311229 |
| GALLERY | 1000 | 91618 | 0.09 | 0.0035 | 36.924942 | 0.511309 | 77.976934 | 23.868271 |
| GALLERY | 1000 | 108848 | 0.09 | 0.0035 | 50.434681 | 0.546915 | 92.99288 | 29.046482 |
| GALLERY | 1000 | 128099 | 0.09 | 0.0035 | 51.35955 | 0.55301 | 110.741155 | 35.754451 |
| GALLERY | 1000 | 151586 | 0.09 | 0.0035 | 61.874756 | 0.654373 | 132.908055 | 44.353688 |


| Setup 1 \& 2 (single-thread CPU) |  |  |  |  | Time: physics [Setup 1] (ms) | Time: rendering [Setup 1] (ms) | Time: physics [Setup 2] (ms) | Time: rendering [Setup 2] (ms) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Scene | Frames | Particles | Spacing | Time-step |  |  |  |  |
| SIMPLE | 300 | 4288 | 0.09 | 0.0035 | 13.421374 | 2.979458 | 15.032616 | 1.308425 |
| SIMPLE | 300 | 5650 | 0.09 | 0.0035 | 18.467714 | 0.848914 | 20.470007 | 1.145794 |
| SIMPLE | 300 | 7948 | 0.09 | 0.0035 | 26.844249 | 1.145899 | 30.990657 | 1.572741 |
| SIMPLE | 300 | 9776 | 0.09 | 0.0035 | 33.444580 | 1.455196 | 39.038161 | 2.005461 |
| SIMPLE | 300 | 15554 | 0.09 | 0.0035 | 55.441580 | 2.204715 | 66.621267 | 3.491593 |
| SIMPLE | 300 | 20972 | 0.09 | 0.0035 | 77.390233 | 3.203172 | 92.171646 | 4.736185 |
| SIMPLE | 300 | 32568 | 0.09 | 0.0035 | 123.553212 | 5.164654 | 145.830553 | 6.831141 |
| SIMPLE | 300 | 43825 | 0.09 | 0.0035 | 169.728504 | 7.564556 | 200.180402 | 9.580470 |
| SIMPLE | 300 | 57362 | 0.09 | 0.0035 | 223.950013 | 10.440414 | 265.578248 | 12.914885 |
| SIMPLE | 300 | 71890 | 0.09 | 0.0035 | 286.233956 | 13.410864 | 335.268331 | 16.215620 |
| SIMPLE | 300 | 89723 | 0.09 | 0.0035 | 362.147972 | 17.786661 | 424.643174 | 21.276104 |
| SIMPLE | 300 | 110754 | 0.09 | 0.0035 | 451.788155 | 22.797868 | 528.956006 | 27.170915 |
| SIMPLE | 300 | 132478 | 0.09 | 0.0035 | 543.700918 | 28.045401 | 638.646243 | 32.965003 |
| SIMPLE | 300 | 159523 | 0.09 | 0.0035 | 663.541069 | 35.481434 | 778.285594 | 41.332958 |
| SIMPLE | 300 | 189042 | 0.09 | 0.0035 | 793.472399 | 43.150490 | 928.716325 | 50.135879 |
| SIMPLE | 1000 | 4288 | 0.09 | 0.0035 | 13.779317 | 2.677969 | 15.468865 | 0.963917 |
| SIMPLE | 1000 | 5650 | 0.09 | 0.0035 | 19.018743 | 0.846512 | 21.106096 | 1.158946 |
| SIMPLE | 1000 | 7948 | 0.09 | 0.0035 | 27.592867 | 1.143797 | 31.067321 | 1.622139 |
| SIMPLE | 1000 | 9776 | 0.09 | 0.0035 | 34.315115 | 1.389433 | 39.622286 | 1.994555 |
| SIMPLE | 1000 | 15554 | 0.09 | 0.0035 | 56.173382 | 2.180091 | 67.508199 | 3.410117 |
| SIMPLE | 1000 | 20972 | 0.09 | 0.0035 | 78.546942 | 3.273740 | 93.281193 | 4.657917 |
| SIMPLE | 1000 | 32568 | 0.09 | 0.0035 | 123.668523 | 5.059853 | 145.912671 | 6.792969 |
| SIMPLE | 1000 | 43825 | 0.09 | 0.0035 | 170.643481 | 7.503297 | 200.097963 | 9.476540 |
| SIMPLE | 1000 | 57362 | 0.09 | 0.0035 | 223.583061 | 10.451525 | 262.206944 | 12.893394 |
| SIMPLE | 1000 | 71890 | 0.09 | 0.0035 | 286.182306 | 13.269128 | 334.519010 | 16.048177 |
| SIMPLE | 1000 | 89723 | 0.09 | 0.0035 | 361.078046 | 17.568051 | 422.498820 | 21.001845 |
| SIMPLE | 1000 | 110754 | 0.09 | 0.0035 | 450.547065 | 22.673548 | 526.265057 | 26.755516 |
| SIMPLE | 1000 | 132478 | 0.09 | 0.0035 | 540.431982 | 27.674846 | 630.921755 | 32.556661 |
| SIMPLE | 1000 | 159523 | 0.09 | 0.0035 | 660.158624 | 34.747530 | 769.646908 | 40.861104 |
| SIMPLE | 1000 | 189042 | 0.09 | 0.0035 | 788.554882 | 42.677236 | 919.122062 | 49.484072 |
| BREAKING_DAM | 300 | 3965 | 0.09 | 0.0035 | 12.034343 | 4.354177 | 13.591712 | 2.728158 |
| BREAKING_DAM | 300 | 5225 | 0.09 | 0.0035 | 16.638660 | 0.748918 | 18.490849 | 0.976427 |
| BREAKING_DAM | 300 | 7173 | 0.09 | 0.0035 | 23.436881 | 0.990350 | 25.887830 | 1.310350 |
| BREAKING_DAM | 300 | 9055 | 0.09 | 0.0035 | 30.397858 | 1.214365 | 34.890912 | 1.803375 |
| BREAKING_DAM | 300 | 14089 | 0.09 | 0.0035 | 48.972474 | 1.849174 | 58.442567 | 2.538262 |
| BREAKING_DAM | 300 | 19487 | 0.09 | 0.0035 | 71.196792 | 2.829014 | 84.928314 | 4.122550 |
| BREAKING_DAM | 300 | 31054 | 0.09 | 0.0035 | 118.092174 | 4.737344 | 138.752098 | 6.378212 |
| BREAKING_DAM | 300 | 41259 | 0.09 | 0.0035 | 160.305465 | 6.842663 | 188.691985 | 8.727219 |
| BREAKING_DAM | 300 | 53539 | 0.09 | 0.0035 | 210.057187 | 9.247670 | 246.538238 | 11.497398 |
| BREAKING_DAM | 300 | 68416 | 0.09 | 0.0035 | 273.574413 | 12.389284 | 320.311417 | 15.015294 |
| BREAKING_DAM | 300 | 83822 | 0.09 | 0.0035 | 338.122527 | 15.937487 | 396.485247 | 19.134957 |
| BREAKING_DAM | 300 | 103463 | 0.09 | 0.0035 | 422.917863 | 20.525588 | 495.162451 | 24.509477 |
| BREAKING_DAM | 300 | 125836 | 0.09 | 0.0035 | 518.772206 | 25.914858 | 606.823186 | 30.590334 |
| BREAKING_DAM | 300 | 149168 | 0.09 | 0.0035 | 620.897465 | 31.885184 | 725.726931 | 37.489479 |
| BREAKING_DAM | 300 | 176699 | 0.09 | 0.0035 | 743.496662 | 39.019427 | 868.640072 | 45.434337 |
| BREAKING_DAM | 1000 | 3965 | 0.09 | 0.0035 | 12.130736 | 4.322947 | 13.633092 | 2.739064 |
| BREAKING_DAM | 1000 | 5225 | 0.09 | 0.0035 | 16.778894 | 0.748318 | 18.611780 | 0.964559 |
| BREAKING_DAM | 1000 | 7173 | 0.09 | 0.0035 | 23.583121 | 0.974735 | 26.163052 | 1.297519 |
| BREAKING_DAM | 1000 | 9055 | 0.09 | 0.0035 | 30.522477 | 1.210761 | 35.143680 | 1.786695 |
| BREAKING_DAM | 1000 | 14089 | 0.09 | 0.0035 | 49.107304 | 1.839565 | 58.457001 | 2.534412 |
| BREAKING_DAM | 1000 | 19487 | 0.09 | 0.0035 | 71.346636 | 2.802588 | 84.812195 | 4.107794 |
| BREAKING_DAM | 1000 | 31054 | 0.09 | 0.0035 | 117.226744 | 4.667677 | 137.935415 | 6.297378 |
| BREAKING_DAM | 1000 | 41259 | 0.09 | 0.0035 | 158.982396 | 6.767291 | 187.900964 | 8.639328 |
| BREAKING_DAM | 1000 | 53539 | 0.09 | 0.0035 | 208.205911 | 9.147074 | 244.409281 | 11.367806 |
| BREAKING_DAM | 1000 | 68416 | 0.09 | 0.0035 | 270.840891 | 12.203105 | 316.887507 | 14.834700 |
| BREAKING_DAM | 1000 | 83822 | 0.09 | 0.0035 | 334.127195 | 15.692152 | 390.771352 | 18.840490 |
| BREAKING_DAM | 1000 | 103463 | 0.09 | 0.0035 | 418.001247 | 20.200376 | 488.557775 | 24.073870 |
| BREAKING_DAM | 1000 | 125836 | 0.09 | 0.0035 | 512.669753 | 25.463525 | 598.562047 | 30.118480 |
| BREAKING_DAM | 1000 | 149168 | 0.09 | 0.0035 | 615.374868 | 31.309232 | 718.014953 | 36.773197 |
| BREAKING_DAM | 1000 | 176699 | 0.09 | 0.0035 | 736.086754 | 38.460591 | 859.836509 | 44.752378 |
| TWO_BLOCKS | 300 | 4162 | 0.09 | 0.0035 | 12.709391 | 3.692642 | 14.275275 | 1.951571 |
| TWO_BLOCKS | 300 | 5418 | 0.09 | 0.0035 | 17.123325 | 0.784352 | 19.061822 | 1.028713 |
| TWO_BLOCKS | 300 | 7498 | 0.09 | 0.0035 | 24.355161 | 1.024583 | 27.013416 | 1.398883 |
| TWO_BLOCKS | 300 | 9456 | 0.09 | 0.0035 | 31.401420 | 1.299647 | 36.445369 | 1.895757 |
| TWO_BLOCKS | 300 | 14666 | 0.09 | 0.0035 | 50.047506 | 1.973193 | 59.726613 | 2.657909 |


| TWO_BLOCKS | 300 | 20272 | 0.09 | 0.0035 | 72.303053 | 2.971650 | 86.360878 | 4.298974 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| TWO_BLOCKS | 300 | 31922 | 0.09 | 0.0035 | 117.936625 | 4.873375 | 138.114726 | 6.511974 |
| TWO_BLOCKS | 300 | 42704 | 0.09 | 0.0035 | 160.552602 | 7.048661 | 189.107063 | 8.957212 |
| TWO_BLOCKS | 300 | 55304 | 0.09 | 0.0035 | 209.975208 | 9.479192 | 246.304717 | 11.756902 |
| TWO_BLOCKS | 300 | 70004 | 0.09 | 0.0035 | 270.231006 | 12.447840 | 316.672590 | 15.112167 |
| TWO_BLOCKS | 300 | 85698 | 0.09 | 0.0035 | 334.038910 | 15.977726 | 390.776163 | 19.230547 |
| TWO_BLOCKS | 300 | 106380 | 0.09 | 0.0035 | 420.793025 | 20.697653 | 491.905021 | 24.710600 |
| TWO_BLOCKS | 300 | 128360 | 0.09 | 0.0035 | 511.516947 | 25.736486 | 597.620905 | 30.403966 |
| TWO_BLOCKS | 300 | 152052 | 0.09 | 0.0035 | 612.311029 | 31.656665 | 715.265303 | 37.141121 |
| TWO_BLOCKS | 300 | 181056 | 0.09 | 0.0035 | 737.142567 | 39.192393 | 860.644853 | 45.465452 |
| TWO_BLOCKS | 1000 | 4162 | 0.09 | 0.0035 | 13.104570 | 3.348212 | 14.682976 | 1.662236 |
| TWO_BLOCKS | 1000 | 5418 | 0.09 | 0.0035 | 17.702881 | 0.792760 | 19.573451 | 1.024543 |
| TWO_BLOCKS | 1000 | 7498 | 0.09 | 0.0035 | 25.171645 | 1.033892 | 27.987598 | 1.404015 |
| TWO_BLOCKS | 1000 | 9456 | 0.09 | 0.0035 | 32.529302 | 1.294542 | 37.598541 | 1.917249 |
| TWO_BLOCKS | 1000 | 14666 | 0.09 | 0.0035 | 51.741130 | 1.983402 | 61.738169 | 2.884694 |
| TWO_BLOCKS | 1000 | 20272 | 0.09 | 0.0035 | 74.629385 | 2.999277 | 88.709564 | 4.318862 |
| TWO_BLOCKS | 1000 | 31922 | 0.09 | 0.0035 | 121.695030 | 4.952951 | 141.708003 | 6.570675 |
| TWO_BLOCKS | 1000 | 42704 | 0.09 | 0.0035 | 164.208309 | 7.115025 | 192.939957 | 9.037084 |
| TWO_BLOCKS | 1000 | 55304 | 0.09 | 0.0035 | 214.218879 | 9.574384 | 250.888536 | 11.864360 |
| TWO_BLOCKS | 1000 | 70004 | 0.09 | 0.0035 | 275.241612 | 12.570658 | 321.986805 | 15.279289 |
| TWO_BLOCKS | 1000 | 85698 | 0.09 | 0.0035 | 339.034202 | 16.150992 | 396.563194 | 19.362705 |
| TWO_BLOCKS | 1000 | 106380 | 0.09 | 0.0035 | 425.905128 | 20.942388 | 497.783151 | 24.935782 |
| TWO_BLOCKS | 1000 | 128360 | 0.09 | 0.0035 | 515.648010 | 26.032570 | 603.170245 | 30.790816 |
| TWO_BLOCKS | 1000 | 152052 | 0.09 | 0.0035 | 616.671511 | 31.901400 | 720.014961 | 37.416343 |
| TWO_BLOCKS | 1000 | 181056 | 0.09 | 0.0035 | 740.340334 | 39.544631 | 864.818726 | 45.988629 |
| GALLERY | 300 | 4450 | 0.09 | 0.0035 | 13.777215 | 2.639532 | 15.379690 | 0.946595 |
| GALLERY | 300 | 5626 | 0.09 | 0.0035 | 17.540725 | 0.707178 | 19.450596 | 0.923500 |
| GALLERY | 300 | 7802 | 0.09 | 0.0035 | 25.045524 | 0.910774 | 27.960332 | 1.256460 |
| GALLERY | 300 | 9592 | 0.09 | 0.0035 | 30.990926 | 1.123678 | 35.972552 | 1.661273 |
| GALLERY | 300 | 14598 | 0.09 | 0.0035 | 48.341569 | 1.638672 | 57.921314 | 2.257266 |
| GALLERY | 300 | 19376 | 0.09 | 0.0035 | 66.193993 | 2.303810 | 79.107602 | 3.511481 |
| GALLERY | 300 | 29170 | 0.09 | 0.0035 | 102.751659 | 3.616069 | 121.161332 | 4.981575 |
| GALLERY | 300 | 38416 | 0.09 | 0.0035 | 138.336693 | 4.998595 | 162.519310 | 6.634829 |
| GALLERY | 300 | 49410 | 0.09 | 0.0035 | 179.777943 | 6.774798 | 212.041233 | 8.670763 |
| GALLERY | 300 | 61388 | 0.09 | 0.0035 | 225.516916 | 8.662409 | 266.094368 | 10.835006 |
| GALLERY | 300 | 74385 | 0.09 | 0.0035 | 276.957458 | 11.186030 | 325.040225 | 13.668377 |
| GALLERY | 300 | 91618 | 0.09 | 0.0035 | 345.975059 | 14.505113 | 406.007016 | 17.465665 |
| GALLERY | 300 | 108848 | 0.09 | 0.0035 | 413.530258 | 17.698977 | 484.957119 | 21.284444 |
| GALLERY | 300 | 128099 | 0.09 | 0.0035 | 492.360072 | 21.830039 | 577.376400 | 25.949418 |
| GALLERY | 300 | 151586 | 0.09 | 0.0035 | 589.539887 | 26.987486 | 692.038590 | 31.839417 |
| GALLERY | 1000 | 4450 | 0.09 | 0.0035 | 14.045072 | 2.425126 | 15.622193 | 0.851647 |
| GALLERY | 1000 | 5626 | 0.09 | 0.0035 | 17.877048 | 0.706578 | 19.792859 | 0.919651 |
| GALLERY | 1000 | 7802 | 0.09 | 0.0035 | 25.506766 | 0.899062 | 28.641008 | 1.254536 |
| GALLERY | 1000 | 9592 | 0.09 | 0.0035 | 31.530244 | 1.108063 | 36.592282 | 1.668010 |
| GALLERY | 1000 | 14598 | 0.09 | 0.0035 | 49.149945 | 1.637471 | 58.507362 | 2.233208 |
| GALLERY | 1000 | 19376 | 0.09 | 0.0035 | 67.099662 | 2.288495 | 80.225168 | 3.494801 |
| GALLERY | 1000 | 29170 | 0.09 | 0.0035 | 103.685255 | 3.573428 | 121.392288 | 4.950460 |
| GALLERY | 1000 | 38416 | 0.09 | 0.0035 | 138.412065 | 4.907307 | 164.520922 | 6.572279 |
| GALLERY | 1000 | 49410 | 0.09 | 0.0035 | 179.722089 | 6.679907 | 212.038346 | 8.547266 |
| GALLERY | 1000 | 61388 | 0.09 | 0.0035 | 225.184797 | 8.557008 | 266.687474 | 10.682960 |
| GALLERY | 1000 | 74385 | 0.09 | 0.0035 | 275.318786 | 11.023874 | 323.044387 | 13.486179 |
| GALLERY | 1000 | 91618 | 0.09 | 0.0035 | 343.955022 | 14.308124 | 403.547664 | 17.229577 |
| GALLERY | 1000 | 108848 | 0.09 | 0.0035 | 409.642429 | 17.454242 | 479.304171 | 20.927747 |
| GALLERY | 1000 | 128099 | 0.09 | 0.0035 | 487.594801 | 21.507230 | 571.025133 | 25.558719 |
| GALLERY | 1000 | 151586 | 0.09 | 0.0035 | 582.602032 | 26.600415 | 681.756915 | 31.397074 |


| Memory usage (VRAM \& RAM) |  |  |  |  | VRAM: physics [GPU] (MB) | VRAM:rendering[GPU] (MB) | RAM: physics [CPU] (MB) | VRAM:rendering[CPU] (MB) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Scene | Frames | Particles | Spacing | Time-step |  |  |  |  |
| SIMPLE | 300 | 4288 | 0.09 | 0.0035 | 1.477272 | 0.147217 | 3.163944 | 0.114502 |
| SIMPLE | 300 | 5650 | 0.09 | 0.0035 | 1.997223 | 0.193977 | 4.242290 | 0.150871 |
| SIMPLE | 300 | 7948 | 0.09 | 0.0035 | 2.769882 | 0.272873 | 5.988449 | 0.212234 |
| SIMPLE | 300 | 9776 | 0.09 | 0.0035 | 3.489441 | 0.335632 | 7.482788 | 0.261047 |
| SIMPLE | 300 | 15554 | 0.09 | 0.0035 | 5.473457 | 0.534004 | 12.027813 | 0.415337 |
| SIMPLE | 300 | 20972 | 0.09 | 0.0035 | 7.539986 | 0.720016 | 16.529243 | 0.560013 |
| SIMPLE | 300 | 32568 | 0.09 | 0.0035 | 11.645233 | 1.118134 | 26.009525 | 0.869659 |
| SIMPLE | 300 | 43825 | 0.09 | 0.0035 | 15.794048 | 1.504612 | 35.627861 | 1.170254 |
| SIMPLE | 300 | 57362 | 0.09 | 0.0035 | 20.814217 | 1.969368 | 46.955414 | 1.531731 |
| SIMPLE | 300 | 71890 | 0.09 | 0.0035 | 26.325989 | 2.468147 | 59.716366 | 1.919670 |
| SIMPLE | 300 | 89723 | 0.09 | 0.0035 | 33.062908 | 3.080395 | 75.415771 | 2.395863 |
| SIMPLE | 300 | 110754 | 0.09 | 0.0035 | 40.501534 | 3.802437 | 93.352249 | 2.957451 |
| SIMPLE | 300 | 132478 | 0.09 | 0.0035 | 48.821823 | 4.548271 | 112.362701 | 3.537544 |
| SIMPLE | 300 | 159523 | 0.09 | 0.0035 | 59.039623 | 5.476788 | 136.379303 | 4.259724 |
| SIMPLE | 300 | 189042 | 0.09 | 0.0035 | 70.293777 | 6.490242 | 162.654770 | 5.047966 |
| SIMPLE | 1000 | 4288 | 0.09 | 0.0035 | 1.477272 | 0.147217 | 3.244560 | 0.114502 |
| SIMPLE | 1000 | 5650 | 0.09 | 0.0035 | 1.997223 | 0.193977 | 4.345043 | 0.150871 |
| SIMPLE | 1000 | 7948 | 0.09 | 0.0035 | 2.769882 | 0.272873 | 6.127918 | 0.212234 |
| SIMPLE | 1000 | 9776 | 0.09 | 0.0035 | 3.489441 | 0.335632 | 7.645008 | 0.261047 |
| SIMPLE | 1000 | 15554 | 0.09 | 0.0035 | 5.473457 | 0.534004 | 12.235241 | 0.415337 |
| SIMPLE | 1000 | 20972 | 0.09 | 0.0035 | 7.539986 | 0.720016 | 16.776646 | 0.560013 |
| SIMPLE | 1000 | 32568 | 0.09 | 0.0035 | 11.645233 | 1.118134 | 26.260185 | 0.869659 |
| SIMPLE | 1000 | 43825 | 0.09 | 0.0035 | 15.794048 | 1.504612 | 35.885357 | 1.170254 |
| SIMPLE | 1000 | 57362 | 0.09 | 0.0035 | 20.814217 | 1.969368 | 46.955414 | 1.531731 |
| SIMPLE | 1000 | 71890 | 0.09 | 0.0035 | 26.325989 | 2.468147 | 59.859921 | 1.919670 |
| SIMPLE | 1000 | 89723 | 0.09 | 0.0035 | 33.062908 | 3.080395 | 75.511337 | 2.395863 |
| SIMPLE | 1000 | 110754 | 0.09 | 0.0035 | 40.501534 | 3.802437 | 93.377914 | 2.957451 |
| SIMPLE | 1000 | 132478 | 0.09 | 0.0035 | 48.821823 | 4.548271 | 112.232925 | 3.537544 |
| SIMPLE | 1000 | 159523 | 0.09 | 0.0035 | 59.039623 | 5.476788 | 136.192047 | 4.259724 |
| SIMPLE | 1000 | 189042 | 0.09 | 0.0035 | 70.293777 | 6.490242 | 162.492172 | 5.047966 |
| BREAKING_DAM | 300 | 3965 | 0.09 | 0.0035 | 1.377468 | 0.136127 | 2.917358 | 0.105877 |
| BREAKING_DAM | 300 | 5225 | 0.09 | 0.0035 | 1.865902 | 0.179386 | 3.923534 | 0.139523 |
| BREAKING_DAM | 300 | 7173 | 0.09 | 0.0035 | 2.530415 | 0.246265 | 5.374973 | 0.191540 |
| BREAKING_DAM | 300 | 9055 | 0.09 | 0.0035 | 3.266659 | 0.310879 | 6.959625 | 0.241795 |
| BREAKING_DAM | 300 | 14089 | 0.09 | 0.0035 | 5.020786 | 0.483707 | 10.881569 | 0.376217 |
| BREAKING_DAM | 300 | 19487 | 0.09 | 0.0035 | 7.081135 | 0.669033 | 15.476978 | 0.520359 |
| BREAKING_DAM | 300 | 31054 | 0.09 | 0.0035 | 11.177422 | 1.066154 | 25.109829 | 0.829231 |
| BREAKING_DAM | 300 | 41259 | 0.09 | 0.0035 | 15.001179 | 1.416515 | 34.042011 | 1.101734 |
| BREAKING_DAM | 300 | 53539 | 0.09 | 0.0035 | 19.632946 | 1.838116 | 44.563118 | 1.429646 |
| BREAKING_DAM | 300 | 68416 | 0.09 | 0.0035 | 25.252556 | 2.348877 | 57.635815 | 1.826904 |
| BREAKING_DAM | 300 | 83822 | 0.09 | 0.0035 | 31.239555 | 2.877800 | 71.256691 | 2.238289 |
| BREAKING_DAM | 300 | 103463 | 0.09 | 0.0035 | 38.248684 | 3.552120 | 88.254761 | 2.762760 |
| BREAKING_DAM | 300 | 125836 | 0.09 | 0.0035 | 46.769508 | 4.320236 | 108.197334 | 3.360184 |
| BREAKING_DAM | 300 | 149168 | 0.09 | 0.0035 | 55.840027 | 5.121277 | 128.911102 | 3.983215 |
| BREAKING_DAM | 300 | 176699 | 0.09 | 0.0035 | 66.479904 | 6.066479 | 153.878418 | 4.718372 |
| BREAKING_DAM | 1000 | 3965 | 0.09 | 0.0035 | 1.377468 | 0.136127 | 2.947292 | 0.105877 |
| BREAKING_DAM | 1000 | 5225 | 0.09 | 0.0035 | 1.865902 | 0.179386 | 3.960438 | 0.139523 |
| BREAKING_DAM | 1000 | 7173 | 0.09 | 0.0035 | 2.530415 | 0.246265 | 5.416817 | 0.191540 |
| BREAKING_DAM | 1000 | 9055 | 0.09 | 0.0035 | 3.266659 | 0.310879 | 7.000561 | 0.241795 |
| BREAKING_DAM | 1000 | 14089 | 0.09 | 0.0035 | 5.020786 | 0.483707 | 10.918152 | 0.376217 |
| BREAKING_DAM | 1000 | 19487 | 0.09 | 0.0035 | 7.081135 | 0.669033 | 15.495964 | 0.520359 |
| BREAKING_DAM | 1000 | 31054 | 0.09 | 0.0035 | 11.177422 | 1.066154 | 25.048519 | 0.829231 |
| BREAKING_DAM | 1000 | 41259 | 0.09 | 0.0035 | 15.001179 | 1.416515 | 33.815331 | 1.101734 |
| BREAKING_DAM | 1000 | 53539 | 0.09 | 0.0035 | 19.632946 | 1.838116 | 44.420872 | 1.429646 |
| BREAKING_DAM | 1000 | 68416 | 0.09 | 0.0035 | 25.252556 | 2.348877 | 57.176338 | 1.826904 |
| BREAKING_DAM | 1000 | 83822 | 0.09 | 0.0035 | 31.239555 | 2.877800 | 70.748245 | 2.238289 |
| BREAKING_DAM | 1000 | 103463 | 0.09 | 0.0035 | 38.248684 | 3.552120 | 87.573914 | 2.762760 |
| BREAKING_DAM | 1000 | 125836 | 0.09 | 0.0035 | 46.769508 | 4.320236 | 107.426582 | 3.360184 |
| BREAKING_DAM | 1000 | 149168 | 0.09 | 0.0035 | 55.840027 | 5.121277 | 128.325485 | 3.983215 |
| BREAKING_DAM | 1000 | 176699 | 0.09 | 0.0035 | 66.479904 | 6.066479 | 153.346039 | 4.718372 |
| TWO_BLOCKS | 300 | 4162 | 0.09 | 0.0035 | 1.438339 | 0.142891 | 3.055344 | 0.111137 |
| TWO_BLOCKS | 300 | 5418 | 0.09 | 0.0035 | 1.925537 | 0.186012 | 4.026253 | 0.144676 |
| TWO_BLOCKS | 300 | 7498 | 0.09 | 0.0035 | 2.630836 | 0.257423 | 5.554531 | 0.200218 |
| TWO_BLOCKS | 300 | 9456 | 0.09 | 0.0035 | 3.390564 | 0.324646 | 7.149052 | 0.252502 |
| TWO_BLOCKS | 300 | 14666 | 0.09 | 0.0035 | 5.199074 | 0.503517 | 11.103291 | 0.391624 |


| TWO_BLOCKS | 300 | 20272 | 0.09 | 0.0035 | 7.323692 | 0.695984 | 15.704231 | 0.541321 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| TWO_BLOCKS | 300 | 31922 | 0.09 | 0.0035 | 11.445625 | 1.095955 | 25.057598 | 0.852409 |
| TWO_BLOCKS | 300 | 42704 | 0.09 | 0.0035 | 15.447670 | 1.466125 | 34.101059 | 1.140320 |
| TWO_BLOCKS | 300 | 55304 | 0.09 | 0.0035 | 20.178314 | 1.898712 | 44.658298 | 1.476776 |
| TWO_BLOCKS | 300 | 70004 | 0.09 | 0.0035 | 25.743233 | 2.403397 | 57.135658 | 1.869308 |
| TWO_BLOCKS | 300 | 85698 | 0.09 | 0.0035 | 31.819221 | 2.942207 | 70.733582 | 2.288383 |
| TWO_BLOCKS | 300 | 106380 | 0.09 | 0.0035 | 39.150009 | 3.652267 | 88.243362 | 2.840652 |
| TWO_BLOCKS | 300 | 128360 | 0.09 | 0.0035 | 47.549400 | 4.406891 | 107.312767 | 3.427582 |
| TWO_BLOCKS | 300 | 152052 | 0.09 | 0.0035 | 56.731155 | 5.220291 | 128.165131 | 4.060226 |
| TWO_BLOCKS | 300 | 181056 | 0.09 | 0.0035 | 67.826180 | 6.216064 | 153.904114 | 4.834717 |
| TWO_BLOCKS | 1000 | 4162 | 0.09 | 0.0035 | 1.438339 | 0.142891 | 3.128616 | 0.111137 |
| TWO_BLOCKS | 1000 | 5418 | 0.09 | 0.0035 | 1.925537 | 0.186012 | 4.127617 | 0.144676 |
| TWO_BLOCKS | 1000 | 7498 | 0.09 | 0.0035 | 2.630836 | 0.257423 | 5.700142 | 0.200218 |
| TWO_BLOCKS | 1000 | 9456 | 0.09 | 0.0035 | 3.390564 | 0.324646 | 7.347347 | 0.252502 |
| TWO_BLOCKS | 1000 | 14666 | 0.09 | 0.0035 | 5.199074 | 0.503517 | 11.400040 | 0.391624 |
| TWO_BLOCKS | 1000 | 20272 | 0.09 | 0.0035 | 7.323692 | 0.695984 | 16.115936 | 0.541321 |
| TWO_BLOCKS | 1000 | 31922 | 0.09 | 0.0035 | 11.445625 | 1.095955 | 25.648907 | 0.852409 |
| TWO_BLOCKS | 1000 | 42704 | 0.09 | 0.0035 | 15.447670 | 1.466125 | 34.829514 | 1.140320 |
| TWO_BLOCKS | 1000 | 55304 | 0.09 | 0.0035 | 20.178314 | 1.898712 | 45.482456 | 1.476776 |
| TWO_BLOCKS | 1000 | 70004 | 0.09 | 0.0035 | 25.743233 | 2.403397 | 58.008976 | 1.869308 |
| TWO_BLOCKS | 1000 | 85698 | 0.09 | 0.0035 | 31.819221 | 2.942207 | 71.651093 | 2.288383 |
| TWO_BLOCKS | 1000 | 106380 | 0.09 | 0.0035 | 39.150009 | 3.652267 | 89.116806 | 2.840652 |
| TWO_BLOCKS | 1000 | 128360 | 0.09 | 0.0035 | 47.549400 | 4.406891 | 108.051849 | 3.427582 |
| TWO_BLOCKS | 1000 | 152052 | 0.09 | 0.0035 | 56.731155 | 5.220291 | 128.819916 | 4.060226 |
| TWO_BLOCKS | 1000 | 181056 | 0.09 | 0.0035 | 67.826180 | 6.216064 | 154.365829 | 4.834717 |
| GALLERY | 300 | 4450 | 0.09 | 0.0035 | 1.527328 | 0.152779 | 3.235279 | 0.118828 |
| GALLERY | 300 | 5626 | 0.09 | 0.0035 | 1.989807 | 0.193153 | 4.088100 | 0.150230 |
| GALLERY | 300 | 7802 | 0.09 | 0.0035 | 2.724770 | 0.267860 | 5.685009 | 0.208336 |
| GALLERY | 300 | 9592 | 0.09 | 0.0035 | 3.432587 | 0.329315 | 7.098858 | 0.256134 |
| GALLERY | 300 | 14598 | 0.09 | 0.0035 | 5.178062 | 0.501183 | 10.817299 | 0.389809 |
| GALLERY | 300 | 19376 | 0.09 | 0.0035 | 7.046837 | 0.665222 | 14.650669 | 0.517395 |
| GALLERY | 300 | 29170 | 0.09 | 0.0035 | 10.595284 | 1.001472 | 22.365108 | 0.778923 |
| GALLERY | 300 | 38416 | 0.09 | 0.0035 | 14.122719 | 1.318909 | 30.079132 | 1.025818 |
| GALLERY | 300 | 49410 | 0.09 | 0.0035 | 18.357124 | 1.696358 | 39.215424 | 1.319389 |
| GALLERY | 300 | 61388 | 0.09 | 0.0035 | 23.080971 | 2.107590 | 49.252178 | 1.639236 |
| GALLERY | 300 | 74385 | 0.09 | 0.0035 | 28.323612 | 2.553806 | 60.487488 | 1.986294 |
| GALLERY | 300 | 91618 | 0.09 | 0.0035 | 34.588692 | 3.145454 | 74.845917 | 2.446465 |
| GALLERY | 300 | 108848 | 0.09 | 0.0035 | 41.520378 | 3.737000 | 89.591202 | 2.906555 |
| GALLERY | 300 | 128099 | 0.09 | 0.0035 | 49.329906 | 4.397930 | 106.517624 | 3.420612 |
| GALLERY | 300 | 151586 | 0.09 | 0.0035 | 58.720230 | 5.204292 | 127.191910 | 4.047783 |
| GALLERY | 1000 | 4450 | 0.09 | 0.0035 | 1.527328 | 0.152779 | 3.305641 | 0.118828 |
| GALLERY | 1000 | 5626 | 0.09 | 0.0035 | 1.989807 | 0.193153 | 4.176140 | 0.150230 |
| GALLERY | 1000 | 7802 | 0.09 | 0.0035 | 2.724770 | 0.267860 | 5.798283 | 0.208336 |
| GALLERY | 1000 | 9592 | 0.09 | 0.0035 | 3.432587 | 0.329315 | 7.235817 | 0.256134 |
| GALLERY | 1000 | 14598 | 0.09 | 0.0035 | 5.178062 | 0.501183 | 10.992577 | 0.389809 |
| GALLERY | 1000 | 19376 | 0.09 | 0.0035 | 7.046837 | 0.665222 | 14.855721 | 0.517395 |
| GALLERY | 1000 | 29170 | 0.09 | 0.0035 | 10.595284 | 1.001472 | 22.549973 | 0.778923 |
| GALLERY | 1000 | 38416 | 0.09 | 0.0035 | 14.122719 | 1.318909 | 30.231258 | 1.025818 |
| GALLERY | 1000 | 49410 | 0.09 | 0.0035 | 18.357124 | 1.696358 | 39.282608 | 1.319389 |
| GALLERY | 1000 | 61388 | 0.09 | 0.0035 | 23.080971 | 2.107590 | 49.190067 | 1.639236 |
| GALLERY | 1000 | 74385 | 0.09 | 0.0035 | 28.323612 | 2.553806 | 60.244865 | 1.986294 |
| GALLERY | 1000 | 91618 | 0.09 | 0.0035 | 34.588692 | 3.145454 | 74.410103 | 2.446465 |
| GALLERY | 1000 | 108848 | 0.09 | 0.0035 | 41.520378 | 3.737000 | 88.891457 | 2.906555 |
| GALLERY | 1000 | 128099 | 0.09 | 0.0035 | 49.329906 | 4.397930 | 105.511383 | 3.420612 |
| GALLERY | 1000 | 151586 | 0.09 | 0.0035 | 58.720230 | 5.204292 | 125.914871 | 4.047783 |


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