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PARTICLE FILTERING FOR INDOOR RFID TAG TRACKING

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1. INTRODUCTION

In this paper, we propose a particle filtering (PF) method for indoor tracking using radio frequency identification (RFID) based on aggregated binary measurements. We use an Ultra High Frequency (UHF) RFID system that is composed of a standard RFID reader, a large set of standard passive tags whose locations are known, and a newly designed, special semi-passive tag attached to an object that is tracked. This semi-passive tag has the dual ability to sense the backscatter communication between the reader and other passive tags which are in its proximity and to communicate this sensed information to the reader using backscatter modulation. We refer to this tag as a sense-a-tag (ST). Thus, the ST can provide the reader with information that can be used to determine the kinematic parameters of the object on which the ST is attached. We demonstrate the performance of the method with data obtained in a laboratory environment.

Index Terms— particle filtering, tracking, RFID, tags

2. HARDWARE DESCRIPTION

Our approach is based on the use of STs in conjunction with a standard reader-tag RFID system. Passive tags with known locations are deployed in the area of tracking. The ST is placed on the object that needs to be tracked, and an RFID reader with one or more antennas is positioned so as to “illuminate” the tracking area. The ST has the following capabilities: i) to detect and decode backscatter signals from RFID tags in its proximity and ii) to communicate with the reader using backscatter modulation. For more on the characteristics of the ST, see [3,4].

In this paper, we propose a novel particle filtering method (called PF-BIN), based on aggregated binary measurements for indoor RFID tracking.† We use a passive RFID system, which is composed of a standard UHF, ISO 18000-6C (Class1, Gen2) compliant RFID reader, a large set of standard passive tags whose locations are known, and a specially designed semi-passive tag, which is attached to an object that is tracked. The new tag, referred to as sense-a-tag (ST) [4], can sense backscatter communication between the reader and passive tags that are in its proximity and communicate the sensed information to the reader using backscatter modulation. The ST will detect closer tags more often than distant ones in a fixed number of reader queries, and this information can be used for tracking. Therefore, our method for tracking belongs to the class of proximity-based methods.

The paper is organized as follows. In Section 2, we briefly describe the ST and the system used for tracking. In Section 3, we present the methods for indoor tag tracking. The experimental results are shown in Section 4. We conclude the paper with some final remarks in Section 5.
a novel locator protocol, which is fully compatible with the EPC (Electronic Product Code) Global Class 1 Gen 2 standard. This protocol enables the ST to communicate with a standard reader and conveys binary information about the presence or absence of a responding tag in its proximity. The protocol specifies two states of operation for the ST. In the first state or the listen state, the ST listens for backscattering tags in its vicinity. In the second state or the respond state, the ST itself functions as an RFID tag and conveys the information of the tags detected when it was in the listen state as part of its EPC ID payload. The transition between the two states is done using the Select function provided by the 18000-6C compliant RFID reader. The tracking algorithm (see Section 3), which runs on the host computer that also controls the reader, uses aggregated binary information from successive query rounds.

### 3. INDOOR TRACKING USING RFID SYSTEM

Let us assume that we have $K$ reference (passive) tags with known two-dimensional (2D) positions, $k_i$ ($k = 1, 2, \cdots, K$) and one ST attached to an object with an unknown position and velocity $x_i$ at time $t$. A reference tag can be detected by an ST with probability $p_{k_i}$. This probability depends on various factors, but primarily on the distance between the reference tag and the ST, orientation, and the power of the reader [5]. This probability is easily estimated by counting the number of detections of a tag by an ST in a fixed number of reader queries. Using this observation, our goal is to estimate $x_i$ at each time $t$.

#### 3.1. Standard Bayesian solutions

We use the following discrete state-space model:

\[
\begin{align*}
    x_{t+1} &= Ax_t + Bu_t \quad (1) \\
    y_t &= Cx_t + v_t \quad (2)
\end{align*}
\]

where $x_t = [x_{1,t} \ x_{2,t} \ \dot{x}_{1,t} \ \dot{x}_{2,t}]^T$ is the state vector at time $t$, which includes the position and velocity of the ST that we want to estimate. $u_t = [u_{1,t} \ u_{2,t}]^T$ is the process noise (which accounts for the variation of the speed), $y_t = [y_{1,t} \ y_{2,t}]^T$ is observation at time $t$, and $v_t = [v_{1,t} \ v_{2,t}]^T$ is observation noise. The observation is given as $y_t = \sum_k p_k i_k$, i.e., the weighted average of the positions of the detected tags. We have already shown in [3] that this position estimate is more accurate than other estimates found either by non-weighted average, or simply by association with the nearest reference point. It is also worth noting that, since our observations represent static position estimates, our model is linear (in contrast to distance-based methods). Given this observation, the sampling period $T_S$, and assuming random motion of the target, we can define the matrices $A$, $B$, and $C$ as follows:

\[
A = \begin{bmatrix} 1 & 0 & T_S & 0 \\ 0 & 1 & 0 & T_S \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}, \quad B = \begin{bmatrix} T_S \\ 0 \\ 0 \\ 1 \end{bmatrix}, \quad C = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}.
\]

We apply the Bayesian approach to solve this tracking problem and in particular, we use Kalman filtering and particle filtering. At time $t$, our goal is to estimate the posterior distribution $p(x_t|y_{1:t})$ given the prior $p(x_t|y_{1:t-1})$ (initially, $p(x_0|y_0) = p(x_0)$ is available), the state evolution $p(x_t|x_{t-1})$ (defined by the motion model (1)), and the likelihood function $p(y_t|x_t)$ (defined by the measurement model (2)). This posterior can be found by following the prediction and filtering equations [6]:

\[
p(x_t|y_{1:t-1}) = \int p(x_t|x_{t-1})p(x_{t-1}|y_{1:t-1})dx_{t-1}
\]

A standard closed-form solution can be found using traditional Kalman filtering (KF) [7], assuming that the model is linear (as in our case), and that $u_t$ and $v_t$ are drawn from Gaussian distributions. The estimation of the process noise $u_t$ is generally very difficult (it requires an accelerometer or a similar device attached to the target). Thus, we approximate $u_t$ by a Gaussian distribution. To make the process reliable, we need to find an upper bound of the true noise, e.g., by injecting enough uncertainty into the covariance matrix. However, the measurement noise $v_t$ can be easily obtained using real samples. Generally, we cannot expect (especially, in indoor environment) that this noise $v_t$ is Gaussian, so KF is not an optimal solution for our problem.

Therefore, we apply the particle filtering (PF) method [6] in which we represent the posterior distribution by a set of random samples (particles) with associated weights. We apply the well-known sample-importance-resampling (SIR) method (called PF-SIR). In this method, the particles are drawn from $p(x_t|x_{t-1})$, then weighted by the likelihood function, $p(y_t|x_t)$, and finally, resampled in order to avoid the degeneracy problem (the situation in which all but one particle have negligible weights). The PF-SIR method is summarized in Alg. 1.

Note that the likelihood function does not have a parametric form, and therefore we want to find its kernel density estimate (KDE) [8]. Namely, given a set of $N_t$ calibration samples $v_i = y_i - Cx_i$, we have:

\[
p(v_i) = \sum_i K_h(v_i - v_i')
\]

where $K_h$ is the commonly used spherically symmetric Gaussian kernel: $K_h(x) = N(x, 0, hI)$, and $h$ is the bandwidth which controls the variance. To find $h$, we use the generalized cross entropy (GCE) estimator [9], which provides very accurate estimates. This kernel can be found offline prior to tracking. However, if the RFID system is fast enough to provide $N_t$ samples during the sampling period ($T_S$) and also to compute (5), the likelihood function can be obtained online, at each time frame. We can see that the main drawback of this method is high complexity.

#### 3.2. Improved PF method (PF-BIN)

We propose a model for the number of detections of a tag by an ST and show how we proceed with particle filtering. First, we model the

---

**Algorithm 1** SIR particle filtering for tracking (at time $t$)

1: for all particles $m = 1 \ldots N_m$ do
2: \hspace{1em} Draw particle $x_t^{(m)} \sim p(x_t|x_{t-1}^{(m)})$
3: \hspace{1em} Compute weight: $w_t^{(m)} = w_{t-1}^{(m)} \cdot p(y_t|x_t^{(m)})$
4: \hspace{1em} end for
5: \hspace{1em} Normalize weights: $w_t^{(m)} = w_t^{(m)} / \sum_m w_t^{(m)}$
6: \hspace{1em} Resample with replacement from multinomial distribution defined by $w_t^{(m)} (m = 1 \ldots N_m)$
probability of detection of a tag by an ST according to

\begin{align}
p &= \frac{1}{1 + e^{\alpha(d - d_0)}} \tag{6}\end{align}

where \(d\) is the distance between a tag and the ST, and \(\alpha > 0, d_0 > 0\) are parameters of the model, with \(d_0\) being the distance at which the probability of detection is equal to 1/2, and \(\alpha\) being the parameter which determines the steepness of the function.

Our measurements represent the number of times a tag is detected by an ST in \(N\) query rounds. We assume that during the \(N\) query rounds, the location of the object with the ST has not changed much (recall that the object with the attached ST is moving). Let the number of detections of the \(k\)th tag be equal to \(n_k\). Then the probability of detection is modeled by the binomial distribution, i.e.,

\begin{align}
P(n_k) &= \binom{N}{n_k} p_k^n (1 - p_k)^{N - n_k} \tag{7}\end{align}

where \(p_k\) is given by (6) with \(d\) replaced by \(d_k\), the distance between the ST and the \(k\)th tag. In the field, there are total of \(K\) tags and for each of them we have a number of detections \(n_k \in \{0, 1, \ldots, N\}\), \(k = 1, 2, \ldots, K\).

Under the assumption that the parameters of the model in (6) are known (they are estimated offline), we proceed with particle filtering as follows (note that we also assume that at time \(t - 1\) we have the set of particles \(x_{t-1}^{(m)}\):

**Step 1:** Propagate the particles by using the prior, that is,

\begin{align}
x_{t}^{(m)} &\sim p(x_t|x_{t-1}^{(m)}) \tag{8}\end{align}

**Step 2:** Compute the likelihood of the particles \(x_{t}^{(m)}\) given the measurements \(y_t = [n_{1,t}, n_{2,t}, \ldots, n_{K,t}]^T\). The likelihood function is given by

\begin{align}
p(y_{t}|x_{t}^{(m)}) &= \prod_{k=1}^{K} \binom{N}{n_k}^{p_{k,t}^{(m)}} (1 - p_{k,t}^{(m)})^{N - n_k,t} \tag{9}\end{align}

where

\begin{align}
p_{k,t}^{(m)} &= \frac{1}{1 + e^{\alpha(d_{k,t}^{(m)} - d_0)}} \tag{10}\end{align}

and \(d_{k,t}^{(m)}\) is the distance between the ST (whose location is defined by the particle \(x_{t}^{(m)}\)) and the \(k\)th tag at time \(t\). We note that the weights of the particles are

\begin{align}
a_t^{(m)} &\propto p(y_{t}|x_{t}^{(m)}). \tag{11}\end{align}

**Step 3:** Resample with replacement.

4. EXPERIMENTAL RESULTS

Figure 1 shows our experimental setup. We deployed 9 reference tags in an area of 3m x 1.6m. The reader antenna was at a distance of about 2m from the center of the area, and its power level was set to 28dBm. The ST was placed on a chair with wheels that could be moved easily. Our objective was to track the ST during a period of 6s \((T_s \approx 0.7s)\). In the experiment the speed of the movement was approximately constant.

In the first set of experiments, our goal was to obtain calibration samples\(^2\) used for estimation of the likelihood (for PF-SIR), measurement covariance matrix (for KF) and probability of detection (for PF-BIN). To that end, we acquired 20 independent measurements at 20 grid points. Using these samples, we obtained empirical KDE of the measurement noise used for the PF-SIR method. For the KF method, we estimated the measurement covariance matrix \(R = diag(0.025, 0.027)\), and assumed (without measuring) that the process covariance matrix was given by \(Q = diag(0.2V, 0.2V)\) where \(V\) is the speed of movement. Finally, for the PF-BIN method, we estimated the parameters of our model for probability of detection as \(\alpha = 3.059\) and \(d_0 = 0.32m\). The estimation was performed based on fitting with the exponential curve as shown in Figure 3. Having defined all the parameters, we tracked the ST over a number of different tracks. We applied the KF, PF-SIR and PF-BIN methods. The results for two tracks are shown in Figure 2.

Finally, we conducted simulations of 100 random tracks. We used the same model, obtained from the real data. We changed the number of reference tags \((K = 16)\), the sampling period \((T_s = 0.3)\), and the deployment area \((4m x 4m)\). According to Figure 4, where we show the averaged RMSE over the 100 tracks, the PF-BIN consistently performed better than the PF-SIR. On the other hand, the KF had the worst performance during some initial period,

\(^2\)Due to the complex location protocol (see Section 2), our RFID system was not fast enough to obtain the likelihood online.
probably because of the setup time that is necessary for parameter tuning. In Figure 5, we plotted the cumulative distribution functions (CDF) of the errors of each of the methods. As we can see, PF-BIN performed the best of all methods.

Regarding complexity, we found that PF-BIN was twice faster than the PF-SIR, but about 10 times slower than the KF. Thus, one may conclude that the KF is an option for a low-cost application where high accuracy is not crucial. However, if one wants to have a robust algorithm, PF-based methods should be applied. In our experiments, we did not detect large outliers, but in general, they can be expected.

5. CONCLUSIONS

In this paper, we presented three methods for RFID based tracking of objects using aggregated binary measurements in indoor environments. They include two PF methods and a Kalman filtering method. The two PF methods are based on two different observation models. With simulations and experimentation with real data obtained using a novel semi-passive RFID system, we showed that the PF method referred to as PF-BIN performed the best in terms of both RMSE and CDF. There remain a few issues we plan to explore. They include the implementation of a real-time PF-BIN method that estimates the parameters $\alpha$ and $d_0$ online.

6. REFERENCES