Single bead investigation of a clinical drug delivery system – A novel release mechanism

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ARTICLE INFO

Keywords:
- Microgel
- Drug delivery
- Release mechanism

ABSTRACT

Microgels, such as polymeric hydrogels, are currently used as drug delivery devices (DDSs) for chemotherapeutics and/or unstable drugs. The clinical DDS DC bead® was studied with respect to loading and release, measured as relative bead-volume, of six amphiphilic molecules in a micropipette-assisted microscopy method. Theoretical models for loading and release was used to increase the mechanistic understanding of the DDS. It was shown that equilibrium loading was independent of amphiphile concentration. The loading model showed that the rate-determining step was diffusion of the molecule from the bulk to the bead surface ('film control'). Calculations with the developed and applied release model on the release kinetics were consistent with the observations, as the amphiphiles distribute unevenly in the bead. The rate determining step of the release was the diffusion of the amphiphile molecule through the developed amphiphile-free depletion layer. The release rate is determined by the diffusivity and the tendency for aggregation of the amphiphile where a weak tendency for aggregation (i.e. a large cacb) lead to faster release. Salt was necessary for the release to happen, but at physiological concentrations the entry of salt was not rate-determining. This study provides valuable insights into the loading to and release from the DDS. Also, a novel release mechanism of the clinically used DDS is suggested.

1. Introduction

Microgels from synthetic or naturally occurring polymers, is an established type of drug delivery systems (DDSs) for chemotherapeutics and/or unstable drugs, such as proteins and peptides [1,2]. Future successful drug delivery research and development require multidisciplinary and novel approaches to solve issues for complex and novel types of active pharmaceutical ingredients (APIs) [3,4]. Drug release from the gel matrix can be controlled by reducing drug diffusion, most commonly via sterical hindrance and/or by electrostatic interaction mechanisms. An additional benefit of electrostatic interactions between APIs and gel networks is that they enable a high drug loading capacity. The release from charged microgels is often considered to be mediated by an ion exchange mechanism where the drug is replaced by electrolyte ions entering from the release medium. Many microgel DDSs have been designed based on this principle [5]. However, little attention has been given to the importance of self-associating properties of the drugs. Drug aggregates in solutions have been characterized by thermodynamic measurements and static light scattering, both in combination with simple models of self-assembly [6], but there are very few studies providing structural information about them [7,8]. One of the few direct evidences of a larger structure is a cTEM image of fiber-like doxorubicin (DOX) assemblies induced by divalent anions inside lipid vesicles [9]. And more recently, it was suggested that DOX self-assembled into long supramolecular aggregates of hundreds of DOX molecules in the presence of sufficient NaCl concentrations [10].

Although the interactions of simple surfactants and polyelectrolyte gels have been investigated in great detail, the more clinically relevant amphiphilic drugs have not [11]. It has been shown that ionic surfactants spontaneously bind to oppositely charged gels by replacing counterions bound to the charged network. The driving force behind this is attributed to the hydrophobic effect, which allows the surfactant to form micelles stabilized by electrostatic interactions with the charged network [12,13]. The replacement of small ions by surfactant micelles leads to a reduction in osmotic swelling pressure, which causes a decrease in gel-volume in weakly crosslinked networks [14]. During intermediate surfactant loadings the distribution of surfactant inside the gels is typically non-uniform (core-shell), an effect attributed to polyion-mediated attraction between surfactant micelles [15,16] and the hydrophobic effect [17]. Similar investigations of clinically used positively charged amphiphilic drugs with differences in flexibility and degrees of substitution is warranted to elucidate whether the same
mechanisms apply for these molecules.

There are several DDS microparticles in clinical use, for example DC bead®, HepaSphere™, Tandem™, and LifePearl™. The hydrogel DC bead® is currently available in three size ranges, covering a diameter-range of 70–700 μm. It is an ion-exchange hydrogel consisting of polyvinyl alcohol (PVA), integrated with negatively charged 2-acrylamido-2-methylpropanesulfonate (AMPS) [18]. Loaded with DOX (maximum loading of 45 mg DOX per ml beads) or irinotecan (IRI), the beads are used clinically for treating liver cancer [18–20].

The release of DOX and IRI from the beads has been investigated [21], but without systematically exploring the importance of their amphiphilic properties. Recently, a theoretical model was used to investigate whether the release of DOX from the beads was governed only by ion exchange, or if the internal drug aggregation must be considered [22]. The results confirmed that salt was required for the release of DOX. However, internal drug aggregation, drug-PVA interactions, and the equilibrium between protonated and deprotonated DOX, were also important. The applied model involved certain pre-assumptions regarding the distribution of DOX inside the beads, which limited the analysis [22].

The aim of this study was to further investigate and elucidate the bead–drug interactions in the DDS, and their implications for the mechanism(s) of drug release. To accomplish this, molecular binding, distribution and in vitro release were investigated using micropipette-assisted microscopy and the µDISS profiler, respectively. Five model substances—dodecylpyridinium chloride (DOPC), cetylpyridinium chloride (CPC), chlorpromazine hydrochloride (CHL), amitriptyline hydrochloride (AMI), and adiphenine hydrochloride (ADI)—known to form micellar-like aggregates in aqueous solution were selected (Fig. 1 and Table 1). Additionally, the clinically relevant doxorubicin hydrochloride (DOX), known to aggregate at low concentrations [23–25], was investigated. An improved theoretical transport model was derived accounting for electrokinetic effects and local micelle–monomer equilibrium.

2. Materials and methods

2.1. Chemicals and gels

Dodecylpyridinium chloride, cetylpyridinium chloride, chlorpromazine hydrochloride, amitriptyline hydrochloride, adiphenine hydrochloride, all obtained from Sigma-Aldrich, Germany, and doxorubicin hydrochloride purchased from Toronto Research Chemicals, Canada, were all used as received. All solutions were prepared in MilliQ water and all chemicals were of analytical grade. NaCl was obtained from Sigma-Aldrich, Germany. Rhodamine 6G (Sigma-Aldrich, Germany) and pyrene (Janssen Chimica, Belgium) were used as fluorescent probes. The investigated beads, DC bead®, were purchased in sizes 100–300 and 300–500 μm (Biocompatible, UK).

<table>
<thead>
<tr>
<th>Substance</th>
<th>cmc (mM)</th>
<th>Molar mass (g/mol)</th>
<th>pKa</th>
<th>D (×10⁻⁶ cm² s⁻¹)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Dodecylpyridinium chloride</td>
<td>17.8</td>
<td>284</td>
<td>–</td>
<td>4.7 b</td>
</tr>
<tr>
<td>Cetylpyridinium chloride</td>
<td>0.9 c</td>
<td>358</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>Chlorpromazine hydrochloride</td>
<td>19 d</td>
<td>355</td>
<td>9.2 f</td>
<td>6.92 e</td>
</tr>
<tr>
<td>Amitriptyline hydrochloride</td>
<td>30 e</td>
<td>314</td>
<td>9.4 g</td>
<td>6.95 d</td>
</tr>
<tr>
<td>Adiphenine hydrochloride</td>
<td>40 f</td>
<td>348</td>
<td>9.0 h</td>
<td>6.9</td>
</tr>
<tr>
<td>Doxorubicin hydrochloride</td>
<td>1 l</td>
<td>580</td>
<td>7.3, 8.5, and 9.5 i</td>
<td>–</td>
</tr>
</tbody>
</table>

a From reference [50]
b From reference [31]
c From reference [45]
d From reference [51]
e From reference [52]
f From reference [53]
g From reference [54]
h From reference [55, 56]
i From reference [57]
Based on the diffusion coefficients of chlorpromazine and amitriptyline
Forms aggregates of 40 molecules at 1 mM, from reference [23]
From reference [58]
The concentration of network-bound sulfate groups in beads was determined by a method developed earlier [27]. A small volume of the beads was transferred from the manufacturers vial to a custom-made microscopy cell and thoroughly rinsed with 10 mM NaCl aqueous solution, where salt was present to increase the contrast between beads and liquid. A picture of the beads spread out on the bottom of the cell was taken and analyzed with a software (https://imagej.nih.gov/ij/) that provides a list of the diameters of all spherical objects in the image from which the total bead volume was calculated. A coverslip containing a µm-scale (Olympus Tokyo) was used to calibrate the scale settings in the program to ensure correct size determination of the beads. The beads were then transferred to a Kjeldahl flask for degradation of the polymer network. The contents of the flask were mixed with 2 ml hydrogen peroxide and terminated with sulfur content with mass spectrometry. Prior to analysis, the beads were spherical [18,19] and the data were presented as mean values with standard deviations (SD).

### 2.3. Bead charge content

The concentration of network-bound sulfate groups in beads was determined by a method developed earlier [27]. A small volume of the beads was transferred from the manufacturers vial to a custom-made microscopy cell and thoroughly rinsed with 10 mM NaCl aqueous solution, where salt was present to increase the contrast between beads and liquid. A picture of the beads spread out on the bottom of the cell was taken and analyzed with a software (https://imagej.nih.gov/ij/) that provides a list of the diameters of all spherical objects in the image from which the total bead volume was calculated. A coverslip containing a µm-scale (Olympus Tokyo) was used to calibrate the scale settings in the program to ensure correct size determination of the beads. The beads were then transferred to a Kjeldahl flask for determination of sulfur content with mass spectrometry. Prior to analysis, the contents of the flask were mixed with 2 ml hydrogen peroxide and 4 ml nitric acid and diluted to 10 ml to degrade the polymer network. Two blanks containing bead-free NaCl solutions were treated in the same way. The whole procedure was carried out three times. For each sample, the sulfur content was analyzed at two different wavelengths (180.731 and 182.034 nm). The sulfur concentration in the microgel beads could be calculated from the average values, as 75.4, 58.6 and 59.9 mM, respectively. The estimated concentration of sulfate groups in a bead in equilibrium with 10 mM NaCl solution was 65 ± 9 mM, based on all three individual determinations.

### 2.4. NaCl effects

The changes in volumes for beads of 100 to 500 μm diameters were investigated in NaCl solution in the interval of 1.0–150 mM. The bead was equilibrated in a continuous flow of MilliQ water. The MilliQ water was changed to NaCl solution, which was pumped through the flow pipette, thereby exposing the bead to the NaCl solution. When the bead volume had adjusted to the new NaCl concentration the medium was exchanged to MilliQ water, and the procedure repeated for another NaCl concentration.

### 2.5. Amphiphile solutions

The bead-volume changes for beads of 200 μm diameters were investigated in amphiphile solutions. DOPC, CHL, AMI, and ADI were prepared in solutions of falling concentrations; cmc, cmc/10, cmc/100 and cmc/1000. In addition, the bead-volume change was investigated at different concentrations for DOX (0.02, 0.02 and 2 mM) and CPC (0.02 and 0.9 mM).

A schematic flow-chart of the solutions used in the micropipette-assisted microscopy experiments is shown in Fig. 2B. The beads were equilibrated in MilliQ water. Then the solution was exchanged to surfactant or amphiphilic drug solution to load the beads with the amphiphile molecule. When the bead volume had relaxed to a new level the medium was changed to NaCl (150 mM), which initiated the release of the loaded amphiphile molecules and an increase in bead volume. When the bead volume reached a plateau the NaCl solution was changed to MilliQ water, which was pumped through the flow pipette until the bead regained its original size.

### 2.6. Fluorescence microscopy

The use of fluorescence microscopy with a UV-lamp (Olympus U-RFL-T, Japan) enabled the investigation of the distribution of molecular aggregates inside the bead. To investigate if the polymer network itself had any fluorescence, approximately 300 μl beads were placed in a Petri dish containing MilliQ water. MilliQ water was gradually replaced with acetone to increase the internal polymer concentration by inducing shrinking of the beads. Thereafter, investigations of amphiphile aggregation inside a single bead (200 μm) were performed as described in “Amphiphile solution” with fluorescence microscopy. The investigations were performed at cmc or cmc/10 depending on the quality of the micrographs taken. For DOPC (1.78 mM), rhodamine 6G (mole fraction 1.9 × 10⁻³) was added as a fluorescent probe, and the applied...
filter was TRITC (U-MWIGA3) with excitation 530–550 nm, discriminating filter of 570 nm and emission of 575–625 nm. In the case of AMI (36 mM), pyrene (mole fraction 2.8 × 10−4) was used as a fluorescent probe, whereas both CHL (19 mM) and ADI (4.0 mM) showed fluorescence without addition of a fluorescence probe. The filter applied for AMI, CHL and ADI was DAPI (U-MVU2) with excitation 330–385 nm, dichroic mirror/discriminating filter of 400 nm and emission (long pass) of 420 nm.

2.7. Free-flowing release in μDISS profiler

A μDISS profiler with a free-flowing method (Fig. 2C) was used to investigate the release rate of the four model substances (DOPC, CHL, AMI, and ADI) from the investigated beads [22,28]. Each channel of the μDISS profiler was individually calibrated with stock solutions against a standard curve. The μDISS profiler measured the concentration of amphiphile substance using the area under the concentration wavelength curve of the second derivate spectrum [29]. The wavelength intervals were as follows: DOPC 280–285 nm, CHL 300–320 nm, AMI 270–295 nm, and ADI 270–278 nm.

To load the beads, one ml of 100–300 μm beads were equilibrated at room temperature overnight with the amphiphile solution in a 20-ml syringe. The beads were examined in a light microscope and were considered fully loaded when their visual appearance matched the visual appearance of micropipette-assisted microscopy experiments. The loading solution was discarded from the syringe using an 18 G filter needle (Becton Dickinson, New Jersey, USA), and MilliQ water was added to the remaining beads, giving a bead-water slurry with a ratio of 1:1.

The release experiment was initiated by transferring 50 μl of the bead-water slurry to a glass vial containing 20 ml of 150 mM NaCl. The release experiment was performed at room temperature (approximately 22 °C) and the release medium was stirred at 100 rpm using a Teflon coated magnet. The data are presented as mean values with SD.

3. Theory

3.1. Loading model

Consider a spherical bead of volume \( V \) with \( n \) moles of amphiphile molecules exclusively partitioned to a homogeneous shell in the outermost layer. Let \( \beta \) be the the amphiphile-to-polymer charge ratio in the bead and \( f \) the local polymer-to-amphiphile charge ratio in the shell:

\[
\beta = \frac{n_p}{n} \quad (1) \\
\hat{f} = \frac{n_{ps}}{n} \quad (2)
\]

where \( n_p \) and \( n_{ps} \) are the number of moles of polymer charges in the bead and in the shell, respectively. By introducing the volume per mole of polymer charges in the shell (\( v_s \)), in the core (\( v_c \)), and in the amphiphile-free bead (\( v_b \)) we can write:

\[
\frac{V}{n_p} = \frac{v_{ps}}{n_p} + v_c \left(1 - \frac{n_{ps}}{n_p} \right) = v_s \hat{f} + v_c (1 - \hat{f}) \quad (3)
\]

For \( v_c = v_0 \) we have:

\[
\frac{V}{v_0} = \frac{V}{v_0 n_p} = \frac{V}{V/n_p} = 1 - \left(1 - \frac{v_c}{v_0} \right) \hat{f} \quad (4)
\]

where \( V_0 \) is the volume of the amphiphile-free bead prior to loading.

The steady-state rate of transferring \( n \) moles of amphiphile molecules from the liquid bulk to the surface of the bead can be calculated from Eq. (5):

\[
\frac{dn}{dt}_s = 2\pi n_0 ShD(C - cac) \quad (5)
\]

where \( r_b \) is the bead radius, \( Sh \) is the Sherwood number, \( D \) is the diffusion coefficient of the amphiphile in the liquid (see Table 1), \( C \) is the concentration of amphiphile in the bulk, and the critical aggregation concentration (cac) is the concentration of amphiphile in the liquid at \( n_b \). Sh is related to the Reynolds (Re) and the Schmidt (Sc) numbers:

\[
Sh = 2.0 + 0.6Re^{1/2}Sc^{1/3} \quad (6a)
\]

\[
Re = \frac{2\rho v_b}{\eta} \quad (6b)
\]

\[
Sc = \frac{n}{\rho D} \quad (6c)
\]

where \( v \) is the flow rate of the liquid, \( \rho \) is the liquid density, and \( \eta \) is the liquid viscosity. Eq. (6a) is valid as a good approximation for single spheres under conditions of forced convection at moderate flow rates (\( Re < 20 \) [30]).

Assume that the rate of bead volume-change is controlled by the rate of amphiphile loading and that the latter process is determined by the transfer of amphiphile to the bead surface according to Eq. (5) (film control). Using Eq. (1) the loading rate can be written as:

\[
\frac{d\hat{f}}{dt} = \frac{3\hat{f} v_{ps} ShD(C - cac)}{2R_0^3} \quad (7)
\]

where \( R_0 \) is the bead radius at time zero. By substituting for \( t_b \) using \( n_b / R_0 = (V/V_0)^{1/3} = (1 - (1 - v_c/v_0)f)^{1/3} \), Eq. (7) can be integrated (for the full derivation see Supporting Information) to give:

\[
\frac{V(t)}{V_0} = (1 - kt)^{1/2} \quad (8a)
\]

\[
k = \frac{ShD(C - cac)(v_0 - v_c)f}{2R_0^2} \quad (8b)
\]

Eq. (8a-b) is valid for constant \( k \), the validity of which will be discussed later.

Theoretical volume relaxation curves were calculated by means of Eq. (8a-b) with parameters relevant for the DOPC systems in Fig. 3: \( D = 4.7 \times 10^{-6} \text{ cm}^2 \text{ s}^{-1} \) [31]; \( v_0 = 0.022 \text{ m}^3/\text{mol} \); \( v_c = 0.002 \text{ m}^3/\text{mol} \); \( R_0 = 100 \mu \text{m} ; f = 1.1 ; \text{ cac} = 0 ; \text{ Sh} = 30 \). Here, Sh was calculated from Eqs. (6a-c) by setting \( n_b = R_0 \) i.e., neglecting variations of the ‘stagnant layer’ thickness, a good approximation for a large part of the curve [26]. The liquid flow rate \( v \) was set to twice the measured average liquid velocity in the flow-pipette, consistent with a parabolic velocity profile [30] and the bead positioned at the center of the pipette [26]. \( V_0 \) was determined as described in the experimental section. \( v_c \) was obtained by setting \( v_c/v_0 = V_w/V_0 = 0.1 \), meaning that the volume per polymer charged group in the shell is assumed to be the same as in the fully collapsed homogeneous bead. \( f \) was used as a global fitting parameter [16,26,32].

3.2. Lag time

In the above equations \( cac \) is defined as the concentration of amphiphile in the liquid in local equilibrium with the aggregated molecules in the shell, and Eq. (8a-b) describe how the bead volumes vary with time after the shell appears on the bead surface. Assume that aggregation of the amphiphile starts when the concentration inside the bead reaches a critical value, denoted \( cacb \), and that the lag time \( t_L \) needed to reach that concentration coincides with the onset of shrinking [33]. Under the experimental conditions of interest there was no simple electrolyte present in the solution. At time zero all network counterions (Na+) are in the bead and the concentration of the amphiphile (D+) and its counterion (Cl−) are uniformly distributed in the liquid. After a very short time (\( < < 1 \text{ s} \) [34], local equilibrium is
established at the bead boundary, mediated by the ion exchange between \( \text{Na}^+ \) and \( \text{D}^+ \) (\( \text{Cl}^- \) is assumed to be excluded by a Donnan potential). By assuming that the ligand in the bead has the same preference for \( \text{Na}^+ \) and \( \text{D}^+ \) (below \( \text{cac}_b \)) the equilibrium condition becomes:

\[
\frac{C_r}{C} = \frac{C'_r}{C'_+} \tag{9}
\]

where \( C_r \) is the concentration of \( \text{D}^+ \) in the liquid at the bead boundary, \( C' \) is the concentration of \( \text{D}^+ \) in the bead, and \( C'_+ \) is the total
concentration of counterions in the bead (Na⁺ + D⁻). This is valid during binding without extra salt in the system and it is assumed that the chloroide ions are evenly distributed in the solution (see Fig. S1 for a schematic illustration). At every instance, the rate of transferring D⁻ from the bulk liquid to the bead surface is assumed to be given by Eq. (5) with $c_{ac}$ replaced by $C_c(t)$. With $n = C'4m_\text{p}v_\text{f}/3$ and by substituting for $C_c$ using Eq. (9), the rate of increasing the concentration of D⁻ in the bead under conditions of film control is obtained:

$$\frac{dC_c}{dt} = \frac{3ShDC_a}{2\eta^2} \left(1 - \frac{C_c}{C'_c}\right)$$

(10)

The integrated form of (10) can be used to express the time for $C_c$ to reach $c_{ac}$:

$$t_i = \frac{2n^2C_c}{3ShDC_a} \ln \left(1 - \frac{c_{ac}}{C'_c}\right)$$

(11)

For $c_{ac} \ll C_c$, Eq. (11) simplifies to $t_i \approx \frac{2n^2c_{ac}}{3ShDC_a}$.

3.3. Release model

3.3.1. Overview

Being an improvement of a previous theory [22], the current objectives were: (i) to make no presumption about the distribution of amphiphile within the bead during release and (ii) to take the electric coupling of the diffusion of charged species into account. Meanwhile, fitting parameters should be kept at a minimum, only including such parameters that have an actual predictive value.

Consider a system consisting of a spherical gel bead immersed in the surrounding solution. Apart from the polymer in the bead, the system contains water, a cationic amphiphile and a univalent salt. The amphiphile may exist as free ions of permanent charge, or as aggregates of a fixed aggregation number $N$ and charge, interconvertible through the physical reaction

$N$ free amphiphile ions $\rightarrow$ aggregate

(12)

The polymer in the bead facilitates this reaction, shifting the equilibrium concentration of free amphiphile towards lower values. The aggregates are considered immobilized by interactions with the (like-)immobile polymer chains, meaning that they only form and dissolve locally in equilibrium with the local concentration of free amphiphile. Water is treated as being in excess and not explicitly taking part in the transport process. This means that volume changes of the bead and any accompanying convective fluxes within it are ignored, a simplification than can be justified by the relatively small volume changes that were observed experimentally during release of amphiphile.

The mobile components of the system are the free amphiphile ions and the monovalent salt ions; these three species move through the system according to their own unique diffusivities, unaffected by the gel. However, being charged species, their movements are coupled through the requirement of large-scale electroneutrality. This coupling is included in the form of Nernst-Planck flux equations and Gauss’ law, physically equivalent to the Poisson-Nernst-Planck theories [35]. This is a standard method in various fields of science, even though it does not conserve momentum and does not ensure non-negative entropy production.

The surrounding solution is well stirred and large enough to maintain a constant concentration of all species. Between the bead and the solution is a stagnant layer of a constant thickness equal to all species, determined by the Sherwood number (Eq. (6)).

The time-and-space evolution of the concentrations in the bead and stagnant layer can then be solved by a numerical procedure. It is necessary to solve for the time evolution because the system will generally not reach a steady state during release.

3.3.2. Transport equations

For the set of time-dependent fields of concentration $c_i(r,t)$ the equations to solve are conservation laws for the amphiphile and salt ions,

$$\frac{\partial c_i(r,t)}{\partial t} = -\nabla \cdot J_i(r,t)$$

(13)

Nernst-Planck equations for the fields of flux $J_i(r,t)$ of free amphiphile and salt,

$$J_i(r,t) = -D_i \left( \frac{\partial c_i(r,t)}{\partial r} - \frac{q_i}{k_BT} c_i(r,t)E(r,t) \right)$$

(14)

and Gauss’ law for the quasi-static electric field $E(r,t)$,

$$\varepsilon \nabla E(r,t) = \sum q_i c_i(r,t)$$

(15)

The equations depend on the charges $q_i$ and diffusion coefficients $D_i$ of the species, the permittivity $\varepsilon$ of the medium and the thermal energy $k_BT$. The system is reduced to a single polar space coordinate $r$ by the assumption of spherical symmetry.

The relaxation time of the aggregation reaction should be very small on the diffusive time scale. Two separate conservation laws for the free amphiphile and aggregate would include production terms with unknown rate constants. To avoid these free parameters, the proportions between free and aggregated amphiphile can be required to satisfy a condition of local equilibrium. This eliminates a variable and leaves a single conservation law for the total concentration of amphiphile $c_f + Nc_{ac}$, in which the flux comes only from the free amphiphile.

3.3.3. Condition for local equilibrium

The free amphiphile is always in local equilibrium with aggregated amphiphile everywhere inside the bead. If the free amphiphile is ideally mixed and the solvent is in large excess, equilibrium requires that

$$N \ln c_f = \ln c_{ac} + NW_a$$

(16)

where $N$ is a constant aggregation number and $W_a$ the change in free energy per amphiphile molecule of the aggregation reaction in units of $k_BT$ (including standard state differences, entropy loss of confinement and hard-sphere excluded volume, hydrophobic effects and electric interactions). For convenience, Eq. (16) can be used to define $c_f$ and $c_{ac}$ explicitly as functions of the total amphiphile concentration $c_f + Nc_{ac}$ in the form of a cubic spline.

For sufficiently large $N$, $W_a$ determines a $c_{ac}$ according to

$$c_{ac} \approx \exp(W_a)$$

(17)

For simplicity, $W_a$ is taken to be a constant depending only on the amphiphile and treated as a direct representation of the $c_{ac}$ inside the bead. The constant $W_a$ is a simplification to the theory and must be expected to limit its applicability to a certain range of aggregate concentrations. Realistically, $W_a$ should depend in a non-trivial way on (at least) the concentration of aggregates and salt.

3.3.4. Parameters

Bead diameter and charge concentration were chosen by calculating time averages (trapezoid quadrature rule) from the release experiments, based on the measured polymer charge contents and the observed volume changes. For the CHL experiment (having the largest number of measured points), this resulted in a bead diameter of 150 μm and charge concentration of 150 mM. While the calculated release times depend on the size and amount of polymer charge in the bead, the qualitative behaviour is insensitive to variations in these parameters.

Diffusion coefficients of sodium and chloride ions were set to $1.3 \times 10^{-5} \text{cm}^2\text{s}^{-1}$ [36] and $2.0 \times 10^{-5} \text{cm}^2\text{s}^{-1}$ [36], respectively, whereas that of the amphiphile was tested in the range of $2 \times 10^{-6} \text{cm}^2\text{s}^{-1}$ (DOX) to $7 \times 10^{-6} \text{cm}^2\text{s}^{-1}$ (CHL). The permittivity of the medium was assumed to be that of water at 25 °C [37]. Liquid
flow rate was set to twice the average flow rate in the experiment, as described in the binding model. This results in a stagnant-layer thickness of about 10% of the bead diameter, only slightly dependent on the diffusion coefficient.

The aggregation number was set to 50, which is reasonable for a variety of self-assembling substances [10,23,38]. This number is large enough to yield a well-defined cacb, which is the only function of this parameter in the present theory. It does not otherwise affect the transport kinetics.

The cacb was chosen in the range of 0.25–2 mM to reproduce the experimentally observed release rates (excluding DOX and CPC, where information on release time was incomplete). The cacb is the only free parameter in the model and reflects the accuracy of the approximations. If an unrealistic cacb is required to reproduce correct release rates, it is likely that some important effect has been neglected.

3.3.5. Solution

The system of coupled partial differential equations (Eqs. (13)-(15)) was solved by an implicit finite-difference scheme, similar to the classic method of Brumleve and Buck in 1978 [39]. The domain of the problem was defined to include the bead and the stagnant layer, with a larger density of points around the discontinuous bead surface. As boundary conditions, constant concentrations of all species were required at the well-stirred boundary while zero flux and electric field was required at the bead center. As initial conditions, the bead was considered to be equilibrated with a dilute amphiphile solution (no extra salt such as sodium and chloride ions). To be consistent with the transport equations, the uniform concentrations of free amphiphile, aggregate and counterion in the bead in this state were determined by a Donnan equilibrium together with the aggregation equilibrium condition (Eq. (16)).

4. Results and discussion

4.1. Response to osmotic stress

The responses of the beads to osmotic stress was investigated using the micropipette-assisted microscopy method by exposing single beads with diameters of 100–500 μm to solutions containing 1–150 mM NaCl. The bead volume in salt solution relative to that in pure water (VNaCl/V0) is shown as a function of NaCl concentration in Fig. S2. The volume change is much larger than that caused by the addition of NaCl (see above). This shows that shrinkage induced by the amphiphiles was not simply due to an increase of the osmotic pressure in the solution. Instead, it must be attributed to substantial loading of the amphiphile and self-assembly inside the beads. This is in agreement with the behavior of regular surfactant loading into oppositely charged gels [11,40,41], where shrinkage has been shown to be a consequence of surfactant micelles replacing the network counter ions. In those systems, volume changes similar to the ones observed here typically require bound surfactant-to-network charge ratios (β) as high as 0.8 [13]. The concentration of network charges in the beads in the fully contracted state is ca. 400 mM, based on the estimated charge content of the network in 10 mM NaCl (see Experimental section) and the bead salt-response data in Fig. S2. This means that for β ≥ 0.8, the amphiphile concentration in the fully contracted state is at least an order of magnitude larger than the cmc for all substances studied here. The critical aggregation concentration inside the bead (cacb) is expected to be lower than cmc [13]. The conclusion is that most of the amphiphiles inside the beads are aggregated.

Fig. 4 (left panel) shows representative pictures of the beads during loading of amphiphiles in the micropipette-assisted microscopy method. A shell could always be observed with the light microscope at the rim of the bead soon after shrinkage started. The shell grew in thickness and a sharp core/shell boundary could be seen migrating towards the center of the bead. DOPC, CHL, AMI, and ADI showed similar behaviors with only minor differences in coloration and shell thickness. In light microscopy, a homogeneous sphere with refractive index different from that of the surrounding medium can display a dark field at the rim, easily mistaken for a shell. This is due to the reflection of the incoming light at large incidence angles [42]. However, fluorescence microscopy confirmed that the amphiphiles were mainly partitioned to the shell during the binding process (Fig. 4).

DOPC appeared to be uniformly distributed in the bead when the experiment was interrupted (Fig. 4). This is the expected behavior of regular surfactants under the present conditions, where the concentration in the solution is fixed [16]. CHL, AMI, and ADI appeared to be non-uniformly distributed, as shown by the fluorescence images (Fig. 4). The reason for this is not clear; for a discussion, see Supporting Information.

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Table 2

<table>
<thead>
<tr>
<th>Substance</th>
<th>Dodecylpyridinium</th>
<th>Chlorpromazine</th>
<th>Amitriptyline</th>
<th>Adiphenine</th>
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<tr>
<td>Conc (mM)</td>
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<td>19</td>
<td>36</td>
<td>40</td>
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<td>VNaCl/V0</td>
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<td>0.11 ± 0.01</td>
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<td>4</td>
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<tr>
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<td>0.09 ± 0.01</td>
<td>0.09 ± 0.01</td>
<td>0.12 ± 0.00</td>
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<td>0.36</td>
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<tr>
<td>VNaCl/V0</td>
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<td>0.10 ± 0.01</td>
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<td>Conc (mM)</td>
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<td>0.019</td>
<td>0.036</td>
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<tr>
<td>VNaCl/V0</td>
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<td>0.11 ± 0.00</td>
<td>0.14 ± 0.01</td>
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<tr>
<td>tL (s)</td>
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<td>145</td>
<td>151</td>
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4.3. Rate determining step during loading

The loading kinetics were evaluated by comparing the recorded volume relaxation curves with theoretical curves calculated from Eq. (8a-b). The result for DOPC is shown in Fig. 5A. The experimental data are the same as in Fig. 3A, but shown without error bars and with data for an additional concentration of DOPC concentration added. The theoretical curves have been adjusted horizontally to start where the experimental lag phase ends. Apart from that, all curves have been calculated with the parameters given in 'Loading model' except for the
amphiphile concentration. Eq. (8a-b) is valid for core-shell beads when the process controlling the shrinking rate is the mass transfer of the amphiphile from the bulk liquid to the bead surface (‘film control’). Agreement between theory and experiment indicates that this is the case for the three lowest concentrations (Fig. 5A). At the highest concentrations investigated, the shrinkage rate is overestimated by the model, suggesting that the shrinking of the beads caused by the binding of dodecylpyridinium was film-controlled.

4.4. Relationship between cac\textsubscript{b} and cmc

The lag phase observed prior to shrinkage for all the amphiphiles increases with decreasing concentration in the solution (Fig. 3). This is in agreement with expectations for a film-controlled process in which shrinkage starts when the concentration of amphiphile inside the beads exceeds a critical value. In Eq. (11) the critical concentration is equal to cac\textsubscript{b}, i.e., the critical aggregation concentration of the amphiphile inside the bead. The relationship was used to calculate cac\textsubscript{b} for the investigated amphiphiles from the lag times determined at the lowest concentrations in Fig. 3. The diffusion coefficients used in the calculations are given in Table 1. The result is presented in Fig. 5B as a plot of cac\textsubscript{b} vs. cmc. The correlation between the values (cac\textsubscript{b} = 0.72 \times cmc – 7.6 with a r\textsuperscript{2} of 0.99) supports the hypothesis that the shrinkage is directly related to the formation of aggregates inside the beads. Furthermore, it shows that amphiphilic drugs with a large tendency to form micelles in pure water also have a large tendency to form micelles in the beads. All cac\textsubscript{b} values are in the millimolar range and 2–3 times smaller than the corresponding cmc values. This is in agreement with previous studies of surfactant self-assembly in polyelectrolyte gels [13]. Investigations of surfactants also show that cac can be much lower than cac\textsubscript{b}, where cac is the concentration of surfactant in the liquid solution in (local) equilibrium with the beads (see above). This explains why the rate of shrinkage was practically the same for all the amphiphiles, since cac was negligible compared to the concentration in the bulk solution (i.e., in Eq. 8b, C – cac = C).

4.5. Release kinetics

4.5.1. Microscopy studies

In each of the above experiments, the release of the amphiphile from the loaded beads was initiated by changing the liquid in the flow-pipette from amphiphilic solution to 150 mM NaCl solution. This always resulted in immediate swelling (without a lag phase) (Fig. 3) accompanied by the appearance of a depletion layer, with less intense coloration, in the outermost layer of the bead (Fig. 4 right panel). In Fig. 3 the dotted horizontal lines indicate a relative volume of 0.34, which corresponds to V\textsubscript{NaCl}/V\textsubscript{0} for beads in equilibrium with 150 mM NaCl (Fig. S2). All the investigated amphiphilic molecules reached this plateau, indicating that the amphiphilic molecules had been completely released. The fluorescence images of CHL revealed some anomalies (see Fig. 4D), probably due to photo-induced effects (for further discussion see Supporting Information).

For each amphiphile the swelling profile was independent of the concentration in the solution during loading (cmc to cmc/1000). This indicates that all concentrations were higher than that needed to reach the maximum loading capacity. This is in agreement with the observation that the final relative bead volume was independent of the concentration in the solution after loading was completed (Fig. 3). Interestingly, each amphiphile had a swelling rate distinctly different from the others. The shortest time to reach the plateau was observed for ADI (< 300 s), followed by AMI (< 450 s), DOPC (< 1000 s), and CHL (< 1500 s). Apart from the fact that the last two appear in the reverse
order, the swelling rate increased with increasing cmc. This suggests that the swelling rate (and presumably also the release rate) is controlled by the amphiphile rate of diffusion through the depletion layer, which will be further discussed below. Thus, by assuming that the concentration of monomers in local equilibrium with the aggregates in the amphiphile rich core increases with increasing cmc, the amphiphile with the largest cmc should have the largest concentration gradient in the depletion layer, and thereby also the largest transport rate out of the bead. In order to accurately describe the quantitative release of an amphiphile from the beads novel experimental techniques that enables determination of the release from single beads or the amphiphile concentration inside the beads are warranted.

4.5.2. Free-flowing release in μDISS profiler

The release from beads suspended in 150 mM NaCl solution was measured using the free-flowing method in a μDISS profiler, previously used to study the release of DOX [22]. Initial release rates were determined from the initial slope of the curve for each amphiphile (see Supporting information Fig. S3) and compared with initial swelling rates determined from the initial slope of the curves in Fig. 3. Fig. 6 shows that there is a correlation between the swelling and release rates ($r^2$ was 0.99 and $p$-value < .0001). The result confirms that the rate of swelling of a single bead in the flow-pipette experiment is directly related to the release rate from the beads in a stirred suspension.

4.5.3. The impact of amphiphilic self-assembly on binding and release of doxorubicin

The in vitro release rate was determined with a μDISS method, as previously described [22], and was found to depend on the stirring rate, temperature, and the size of the beads. However, no information of the internal morphology of the beads during release could be collected. Therefore, the micropipette-assisted microscopy method was used to study the loading and release of DOX using the same conditions as the other amphiphiles. The microscopy images show that a sharp DOX diffusion front migrated to the center of the bead during loading (Fig. 7A). A depletion layer developed in the outer parts during release (Fig. 7B). Similar observations of the release of DOX from DC beads have been reported earlier by Biondi [43], and from polyacrylate-co-acrylamide colloidal microgels by Kiser [44]. The behavior is qualitatively the same as for the other amphiphiles. This suggests that the rate of shrinkage during loading was chiefly controlled by mass transfer in the liquid layers surrounding the bead. Meanwhile, the rate of swelling was coupled to the release rate, which is mainly controlled by diffusive mass transport through the depletion layer in the bead.

DOX is amphiphilic but the hydrophobic and hydrophilic moieties are not as well separated as for regular surfactants or the other amphiphilic drugs (Fig. 1). CPC was included due to the simpler chemical structure but comparable hydrophobicity to DOX. The result, presented in Fig. 7-D, shows that the behavior of DOX and CPC was very similar with respect to both loading and release.

The rate of shrinkage upon loading of DOX and CPC was nearly the same as for the other amphiphilic drugs when compared at similar concentrations (Figs. 3 and 7C). However, the final relative bead volume was slightly larger for DOX (0.14 ± 0.0027) compared to the other amphiphilic molecules (Table 2). The swelling rate upon release was independent of the concentration of DOX or CPC in the solution during loading (Fig. 7D). However, it was considerably slower, with an uncompleted release after 6000 s, compared to the other amphiphiles, all of which were completely released after 1500 s. CPC has a cmc of 0.9 mM [45] and DOX has been reported to form dimers at 5–20 μM in aqueous solution and larger assemblies, with an aggregation number of 40 at 1 mM [9,23,24]. This is more than one order of magnitude smaller than the cmc of the other amphiphiles studied here (Table 1), suggesting that the slow release of DOX and CPC is an effect of their self-
assembling properties. The resulting low concentration of free monomers in the depletion layer directly affects the rate of diffusive transport out from the bead. In fact, the data for all the substances investigated here suggest that there is a scaling relationship between \( \text{cmc} \) and swelling rate (i.e., release rate) (see Fig. 8). This further suggests that the tendency to self-aggregate plays an important part in the release of an amphiphile molecule from the bead.

4.5.4. Release mechanism

The release model was used to investigate the interplay between aggregation and molecular transport processes. Fig. 9 shows the calculated release of an example amphiphile molecule with \( D = 5 \times 10^{-6} \text{ cm}^2 \text{ s}^{-1} \), \( \text{cacb} = 0.5 \text{ mM in 150 mM NaCl} \); other input parameters and conditions are described in the Theory section. The first step of the process is for salt to enter the bead. This step is fast; the concentration of salt in the centre of the bead reaches the bulk value of 150 mM within a few seconds (Fig. 9). The second step is for the amphiphile to leave the bead, fully depleting the outermost layer first. This is coupled to an enrichment of sodium and a depletion of chloride, finally resulting in a Donnan equilibrium of the salt with the solution.

The mechanism by which the amphiphile is released from the bead is by forming a depletion layer, free of amphiphile aggregates, at the surface of the bead that grows in thickness over time. This is schematically illustrated in Fig. 10. When the free amphiphile molecules diffuse out of the bead, they are immediately replaced through dissolution of aggregates. Due to the high cooperativity of the aggregation equilibrium, the local concentration of free amphiphile stays nearly constant at the \( \text{cacb} \), while there are aggregates remaining [46]. In the absence of an appreciable concentration gradient, the flux of amphiphile within the loaded parts of the bead is always very small. Instead, only the free amphiphile in the outermost layer of the bead can be released, and its concentration is continuously kept constant through replenishing by the local aggregates. Release of amphiphile molecules from the second-outermost layer does not start until all the aggregates in the outermost layer have been dissolved. The results from the release model have similarities to the Higuchi equation which describes the release of a substance present above its solubility in the DDS [47]. Similar release models have previously been developed and applied to the release of catanionic mixtures from gels [48].

The effect of varying the \( \text{cacb} \) of the example amphiphile molecule is shown in Fig. 11. Despite the complex mechanism, the time for complete release is approximately inversely proportional to the \( \text{cacb} \). A higher \( \text{cacb} \) increases the release rate by increasing the concentration gradient in the depletion layer. The amphiphile concentration in the depletion layer will always vary from the \( \text{cacb} \) at the inner boundary to zero at the outer boundary, so a larger \( \text{cacb} \) yields a larger concentration gradient. Thus, the faster release of an amphiphile with lower tendency for aggregation in the bead is caused by a larger concentration gradient in the depletion layer, not by faster or less obstructed movement of individual amphiphile molecules. The conditions match those of the simple internal depletion-layer model derived earlier [22], from which the time for complete release can be shown to be inversely proportional to \( \text{cacb} \) (for further discussion see Supporting Information).

Ion exchange is sometimes held as the primary release mechanism of charged drugs from oppositely charged beads [21,43,49]. However, the calculations presented here affirm that ion exchange is not rate limiting for the release, nor does it determine the release mechanism. Inevitably, the release of an amphiphile from the bead must be coupled to movement of other charged species, but at physiological salt concentrations (approximately 150 mM NaCl) there are enough sodium and chloride ions to enable free movement of the amphiphile. This can be verified by changing the diffusion coefficients of sodium and

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**Fig. 8.** Relationship of swelling rate (s\(^{-1}\)) and critical micelle concentration (\( \text{cmc} \)) for the investigated substances. On a log-log scale to separate doxorubicin and cetylpyridinium from axis-origin.

**Fig. 9.** Calculated distributions of amphiphile and salt during release in 150 mM NaCl. Diffusion coefficient of the amphiphile molecule is \( 5 \times 10^{-6} \text{ cm}^2 \text{ s}^{-1} \) and the critical aggregation concentration inside the bead (\( \text{cacb} \)) is 0.5 mM. Bead diameter is 150 \( \mu \text{m} \) and the concentration of fixed charges is 150 mM.
chloride; reducing or increasing these by an order of magnitude has a negligible effect on the calculated release rate. At physiological salt concentrations the ion exchange taking place is not rate determining, partly since both sodium ions and chloride ions are involved in the exchange. In order to leave the bead, the amphiphiles must either be exchanged by sodium ions or accompanied by chloride ions. The effect of the drug leaving the bead will thus be a simultaneous enrichment of sodium and depletion of chloride. Salt has an effect on the release rate, but this effect depends on the concentration. The behaviour at physiological salt concentration represents an intermediate between two limiting cases. At the high-concentration limit, the mechanism described in Fig. 10 is exact. At the low-concentration limit, release happens through a film-controlled mechanism with a steady flux of amphiphile through the whole bead, and a constant even distribution of amphiphile in the bead. At this limit, diffusion of sodium ions is rate-limiting for the release of the amphiphile, due to both the slow influx of sodium and the inability to deplete chloride (whose concentration is always close to zero). At physiological salt concentrations, there is a small flux of amphiphile within the loaded regions (due to the electric field), but the mechanism in Fig. 10 is nearly correct.

Thus, a strict ion-exchange mechanism of release where sodium ions exchange the amphiphile ions one at a time is only valid at the limit of zero salt concentration. Additionally, such a mechanism would not explain the observed depletion layers without assuming that the amphiphile-loaded bead is impermeable to small ions. With aggregates estimated to occupy < 10% of the volume, the rest being an aqueous solution of loosely cross-linked polymer chains, this assumption is unrealistic. It is much more plausible that the observed mechanism is due to an aggregation reaction.

5. Conclusions

This study provides valuable insights and a mechanistic understanding of amphiphile molecules loading to and release from a PVA based bead DDS. It was shown that loading was film controlled and independent of amphiphile concentration. The release rate was determined by diffusion of the amphiphile through the depletion layer in the polymeric network. Both the mechanism and rate of release were shown to be strongly dependent on aggregation reactions. The release rate was not dependent on ion exchange mechanisms at physiological conditions. Fundamental knowledge in these mechanisms is crucial to understand the clinical performance of the DDS with direct implications on efficacy and safety. The proposed experimental and analytical methods in this study can be applied in the development of future DDSs.

Acknowledgments

Financial support was provided by the Swedish Research Council, grant number 521-2011-373. The authors wish to acknowledge Martin Nilsson and Jean Pettersson for the kind assistance in determining the charge contents of the beads.

Appendix A. Supplementary data

Supplementary data to this article can be found online at https://doi.org/10.1016/j.jconrel.2018.11.011.

References
