The design and simulated performance of a fast Level 1 track trigger for the ATLAS High Luminosity Upgrade

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Abstract. The ATLAS experiment at the High Luminosity LHC will face a fivefold increase in the number of interactions per bunch crossing relative to the ongoing Run 2. This will require a proportional improvement in rejection power at the earliest levels of the detector trigger system, while preserving good signal efficiency. One critical aspect of this improvement will be the implementation of precise track reconstruction, through which sharper trigger turn-on curves can be achieved, and b-tagging and tau-tagging techniques can in principle be implemented. The challenge of such a project comes in the development of a fast, custom electronic device integrated in the hardware based first trigger level of the experiment. This article will discuss the requirements, architecture and projected performance of the system in terms of tracking, timing and physics, based on detailed simulations. Studies are carried out using data from the strip subsystem only or both strip and pixel subsystems.

1 Introduction

ATLAS is an experiment at the Large Hadron Collider (LHC) aimed at studying the Standard Model of particle physics and to search for physics beyond the Standard Model by analysing high energy proton-proton interactions. The ATLAS detector consists of a number of subdetectors. Moving from the interaction point outwards they are: a tracker that consists of a silicon pixel detector, a silicon strip detector, and a straw tube detector; the electromagnetic and hadronic sampling calorimeters, which use liquid argon and plastic scintillators as active medium; and finally the muon spectrometer that consists of monitored drift tubes, cathode-strip chambers, resistive plate chambers, and thin gap chambers [1].

The High Luminosity LHC (HL-LHC) is scheduled to start running in 2026. The upgrade is expected to increase the instantaneous proton-proton luminosity to $7.5 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$, which translates to a sevenfold increase in the number of interactions per bunch crossing, so-called pile-up, compared to the LHC design luminosity. The ATLAS detector will be upgraded as well, in a project named the Phase-II upgrade, with installation scheduled to take place between 2024 and 2026. The upgrade will include a completely new tracker, as described in section 2.2, upgrades to the trigger and readout electronics, and replacements of parts of the calorimeter and muon spectrometer.

The vast amount of data generated by the increased luminosity puts strict demands on the ATLAS trigger system. Due to its high energy frontier physics program, ATLAS bases its trigger selection on

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high transverse momentum ($p_T$) lepton selection organised in two levels: one hardware (first-level) and one software. The left plot in figure 1 shows the ATLAS acceptance fraction of a few processes as a function of muon $p_T$ threshold. From it, it is clear that the current trigger $p_T$ threshold of 20 GeV needs to be maintained in order to take full advantage of the increase in luminosity. At the same time, trigger rates need to be kept at a reasonable level to avoid saturating the readout bandwidth. This is shown in the right plot of figure 1, where we see that the first-level electromagnetic trigger rate for electrons has a strong dependence on $p_T$ [2]. As an example, to limit the rate to 20 kHz one would have to increase the threshold to 40 GeV. The ATLAS Phase-II upgrade will introduce a hardware track trigger that can help to control the trigger rate by exploiting extremely good tracking resolution to increase the signal-to-background ratio.

Figure 1: The impact of $p_T$ threshold on acceptance fraction of a few processes (left) and trigger rate for the Level-0 electron trigger (right) for ATLAS at the HL-LHC [2, 3].

2 The ATLAS Phase II Upgrade

The ATLAS detector will be upgraded to make the most out of the HL-LHC. Large parts of the tracker will reach their end of life shortly after 2020 and must be replaced. Therefore, a project to develop a complete replacement of the tracker is in progress. This opens up the possibility of using data from the tracker in the trigger, as described below.

2.1 Trigger Architecture

The ATLAS trigger will consist of a hardware trigger, which uses hardware on and close to the detector, followed by the Event Filter, which is a software trigger running on a computer farm. Current hardware trigger systems, based on calorimeter and muon information, will change to cope with higher trigger rates and will represent the so-called L0 system. The hardware trigger will operate in a single-level (L0) mode but retain the option to evolve to a split-level (L0/L1) trigger. The architecture is presented in figure 2.

The regional hardware track trigger provides tracking in Regions of Interest (RoIs), which are identified by the L0 muon and electromagnetic calorimeter triggers and expected to cover approximately 10% of the detector volume. In the single-level mode, it assists the Event Filter and is called...
EFTrack. In the split-level mode, it contributes to the event rejection before the Event Filter, in the so-called L1 trigger, and is called L1Track. The hardware is the same in both cases, but L1Track has a strict latency requirement and gains speed by increasing parallelism at the expense of reduced momentum acceptance, as explained in section 3.1.1. A comparison of the two working modes is presented in table 1. The Event Filter will also be assisted by FTK++, which provides full-event tracks at a rate of 100 kHz down to a $p_T$ of 1 GeV. FTK++ will not be discussed in this article; see Ref. [4] for further details.

<table>
<thead>
<tr>
<th>Trigger</th>
<th>Latency requirement</th>
<th>L0 rate [MHz]</th>
<th>Trigger threshold [GeV]</th>
</tr>
</thead>
<tbody>
<tr>
<td>EFTrack</td>
<td>0(s)</td>
<td>1</td>
<td>2</td>
</tr>
<tr>
<td>L1Track</td>
<td>30 µs</td>
<td>2–4</td>
<td>4</td>
</tr>
</tbody>
</table>

Table 1: Specifications for the regional track trigger when running as an Event Filter co-processor (EFTrack) and as an extra hardware trigger level (L1Track).

In the single-level mode, the muon and calorimeter triggers can issue a Level-0 Accept (L0A), which initiates full readout of all detectors at 1 MHz. In the split-level mode, L0A is running at a rate of 2–4 MHz and the Inner Tracker (ITk) modules in RoIs specified by the L0-trigger are read out at this rate following a Regional Readout Request (R3). The R3 data is sent to L1Track, which participates in the L1 decision (L1A) to start the full detector readout and Event Filter. The total L1 data rate consists of 10% of the R3 data plus the Level-1 Accept (L1A) data. If the maximum total readout rate for the ITk is fixed at 1 MHz, then 600–800 kHz is left for L1A, since 200–400 kHz is expected to be consumed by R3, which is prioritised over L1A.

Figure 2: Logical schematic of the two trigger options for the ATLAS Phase-II upgrade. FELIX is the Front-End LLink eXchange and LTI is the Local Trigger Interface. See Ref. [5] for further details.
2.2 The Inner Tracker

The current ATLAS tracker will be completely replaced during the Phase II upgrade. The new ITk will be all-silicon and consist of pixel detectors close to the beam pipe and strip detectors at larger radii. The final layout is not decided yet, but the proposed layouts typically have a barrel with 5 pixel layers and 4 strip stereo-layers (closely-spaced layers, slightly inclined with respect to each other) and an endcap with coverage up to a pseudorapidity ($\eta$) of 4.

An important factor for the hardware track trigger is the time it takes to read out data from the ITk. If it takes too long, the buffers in the frontend electronics will get overfilled, which results in loss of data. The left plot in figure 3 shows the result of discrete event simulations of the latency at which 99% of the event data is read out for the strip endcap in the single-level trigger mode, as a function of L0 rate. The baseline L0 rate is set to 1 MHz, which is below the point on the curve where the latency starts to rapidly increase. At 1 MHz the latency is approximately 6 µs for the module with highest occupancy.

The readout latency in the split-level L0/L1 mode is presented in the right plot of figure 3 for the module with the highest occupancy. The L1A latency is below 8 µs for a L1A rate of 800 kHz with a L0A rate of 2 MHz or a L1A rate of 600 kHz with a L0A rate of 4 MHz. In both cases the R3 latency is below 3 µs, leaving time to process data for a track trigger decision.

![Figure 3: Latencies for the inner tracker strip detector as a function of L0 rate for the so-called extended layout. The left plot is showing the latencies for the endcap modules, including the module with highest occupancy, in the single-level L0 trigger mode. The red dotted line indicates the boundary above which frontend buffers are starting to get overfilled. The right plot is showing the highest-occupancy endcap module in the split-level L0/L1 trigger mode. The blue numbers indicate the corresponding L1A rate. The figures are from Ref. [5] where further information can be found.](image)

3 The Regional Track Trigger

The L1Track/EFTrack trigger will provide fast regional hardware track triggering. As described in section 2.1, the regional track triggering will either run as part of an extra trigger level after L0 (L1Track) or as part of the Event Filter (EFTrack). An overview of the system is presented in figure 4. The system conceptually consists of three parts: pattern matching using Associative Memory (AM) chips [6], track fitting of the full-resolution hits using Field Programmable Gate Arrays (FPGAs), and selection of the best track candidates based on track parameters and the $\chi^2$ of the fit. The results
presented in this section are for the ITk layout described in the ATLAS Phase-II upgrade Letter of Intent (Ref. [2]).

![Logical schematic of the L1Track/EFTrack trigger and the objects passed between the system components.](image)

Figure 4: Logical schematic of the L1Track/EFTrack trigger and the objects passed between the system components.

### 3.1 Pattern Matching

The pattern matching step selects which hits to pass on to the track fitter. This is done using custom made AM ASICs that match the hits read out from the detector to predefined hit patterns from simulated tracks [7]. An alternative method using the Hough transform has also been studied.

#### 3.1.1 Associative Memory

At each clock cycle the AM chip compares the input combination of hits with all the predefined patterns stored in the AM, and outputs the address of the matched patterns, if any. In the regional hardware track trigger, pixels and strips are combined into coarser-resolution super-strips and simulated tracks of muons are used to generate patterns of super-strip hits. Data from the detector are sent to the AM chip and if it matches a pattern the associated ITk hits are sent to the track fitter.

The trigger uses 8 ITk layers, which can be a combination of strip and pixel layers. However, the occupancy of the innermost pixel layers is too high to be of use in the track trigger. It is assumed that each AM chip can contain half a million patterns, so that one million patterns can be stored for each $\Delta \eta = 0.2$ by $\Delta \phi = 0.2$ RoI using two AM chips. All the results showed here are under this assumption. The set of patterns stored for an RoI is called a pattern bank. Each pattern bank is trained separately using a total of 30 million simulated muon tracks. The same pattern can occur more than once during training, so the patterns are sorted according to how many times they occur and only the 1 million most frequent ones are stored in the pattern bank.

In L1Track the number of patterns in the AM chips can be duplicated to speed up the matching. In EFTrack the duplication is not needed because there is no latency constraint in the Event Filter. The AM used for the duplicated pattern bank in L1Track can in EFTrack be used to expand the pattern bank to cover a $p_T$ down to 2 GeV.

Ternary bits can be implemented in the AMs and used as don’t care bits, i.e. a bit that matches regardless of whether the input is a 0 or a 1. Don’t care bits can be used to combine patterns that are very similar to reduce the number of patterns needed. This is illustrated by track A and B in figure 5. Tracks with missing hits in one or two layers, such as track C in figure 5, can be handled using patterns with wild card layers, i.e. whole layers that match regardless of input.

The performance of the pattern matching has been studied for the central barrel region of $0.1 < \eta < 0.3$ and $0.3 < \phi < 0.5$ using a detailed emulation of the tracking system. The study was

\footnote{$\phi$ is the polar angle in the transverse plane of the detector and $\eta$ is the pseudorapidity.}
performed using single muon samples with the same track parameter distributions used for training, but embedded in 200 minimum bias events. The efficiency is shown in table 2, and is close to 99.5\% for both studied cases.

### 3.1.2 Hough Transform

The Hough transform is a possible alternative to using AM for the pattern matching step. One advantage of the Hough transform is that it can be implemented in commercially available FPGAs and so does not require development of custom ASICs. In general, the Hough transform is used to detect features that can be described by a few parameters, such as lines and circles, in image-like data. It does so by mapping each data point to the set of all parameter values consistent with the data point and accumulating them in a histogram-like parameter space called an accumulator. The point in the accumulator with the largest value corresponds to a candidate feature.

In the case of tracks of charged particles in the transverse plane of the ATLAS detector, the feature we are looking for is a circular arc. If the vertex is constrained to the collision point and if the track’s polar angle $\phi_0$ is small, the track through a hit with the polar coordinates $(r, \varphi)$ is described by the transverse momentum $p_T$, the charge of the particle $q$, and $\phi_0$ by

$$\frac{A}{qp_T} = \frac{\phi_0 - \varphi}{r},$$

where $A \approx 3 \times 10^{-4}$ GeV mm$^{-1}$ is the curvature constant for the 2 T magnetic field in the ATLAS tracker. Figure 6 shows an illustration of applying equation 1 to a toy model of a tracker. The coordinates in the accumulator where the lines from the signal cross are the track parameters of that track.

An implementation of a Hough transform using equation 1 has been studied with the ATLAS ITk layout. Just as for pattern matching using AM chips, the method is looking at RoIs of size $\Delta \phi = 0.2$ by $\Delta \eta = 0.2$ separately. The accumulator is implemented as a two-dimensional histogram with $A/(qp_T)$ on one axis and $\phi_0$ on the other. Each bin holds the information about which layers have been hit and the associated hits’ hashes for the part of the parameter space the bins spans. After the Hough accumulator has been filled, a threshold is applied to require that at least 6 unique detector layers have been hit. Nearby bins that pass the selection are grouped together and duplicate hits are removed. The end result is a collection of hit groups, i.e. hits that might be from the same track, that can be passed on to the track fitter.
To reduce the number of hits in each bin in the accumulator, the RoI is sliced up in $z$, as illustrated in figure 7, and an accumulator is filled for each slice. This greatly reduces the occupancy in the $A/(q\eta_T)$ vs. $\phi_0$ accumulator space, which in turn reduces the number of hit combinations that the track fitter needs to take into account. However, it comes at the cost of having more accumulators. There will also be an overlap between RoI slices. This makes it possible for one hit to end up in more than one hit group, which increases the number of hit combinations. In the end, it is a trade-off between the two effects.

The efficiency of the Hough transform has been simulated in the central barrel region of $0.1 < \eta < 0.3$ and $0.3 < \phi < 0.5$. The study was performed using the same simulation samples used in studying the performance of the pattern matching using AM chips. Just as for the AM-based system, eight ITk layers were used. It was found that slicing up the RoI in approximately 12 slices in $z$ and having an accumulator with approximately 1200 bins in $A/(q\eta_T)$ and 50 bins in $\phi_0$ produced good results. An efficiency of 98.3% was achieved while having a background rejection close to 80% [8]. Although pattern matching using AM chips continues to be the main focus, the Hough transform will be continued to be studied in more detail.
3.2 Track Fitting

Track fitting is performed in an FPGA. It takes the full-resolution hits from the patterns passed by the pattern matching and calculates the track parameters and $\chi^2$ of the fit. The track parameters $p_i$ are calculated using a linear interpolation:

$$p_i = \sum_{j=1}^{N} C_{ij} x_j + q_i$$

(2)

where $x_j$ are the full-resolution hit cluster positions and $(C_{ij}, q_j)$ are constants that are unique for each sector (set of ITk modules). The constants are trained using simulated tracks of muons with the same track parameter ranges and distributions as used to train the patterns.

The simulated track fitting efficiency and the average number of fits for minimum bias events with pile-up 200 is shown in table 2. Two detector layer configurations are used in the simulation, one with 8 strip layers only and one where a strip layer is replaced with the outer pixel layer. The efficiency reaches above 99.5 % with respect to the events with a matched pattern.

The track parameter resolutions, defined as the RMS of the residuals with the simulated true particle, are presented in table 3 for the central barrel region. The resolutions for $p_T$, $\phi$, $\eta$, and the impact parameter $d_0$ are very similar for the strip only and strip plus one pixel case while the resolution in $z_0$, i.e. the coordinate of the interaction point along the beam axis, is significantly improved by using one pixel layer.

Table 2: Pattern matching (using AM chips) and track fitting efficiency for simulated muons of $p_T > 4$ GeV in the central barrel region of $0.1 < \eta < 0.3$ and $0.3 < \phi < 0.5$. The pattern matching efficiency is defined as the fraction of single muon events with a matching pattern. The track fitting efficiency is defined as the fraction of events selected by the pattern matching that has a successful fit with $\chi^2 < 40$. Also shown is the average number of track fits needed in minimum bias events with a pile-up of 200. [9].

<table>
<thead>
<tr>
<th>Detector layers</th>
<th>Matching eff.</th>
<th>Fitting eff.</th>
<th>&lt;N_fits&gt;</th>
</tr>
</thead>
<tbody>
<tr>
<td>Strip only</td>
<td>99.4%</td>
<td>99.5%</td>
<td>114</td>
</tr>
<tr>
<td>Strip + 1 pixel</td>
<td>99.5%</td>
<td>99.7%</td>
<td>331</td>
</tr>
</tbody>
</table>

Table 3: Track parameter resolution for simulated muons of $p_T > 4$ GeV embedded in 200 minimum bias events in the central barrel region of $0.1 < \eta < 0.3$ and $0.3 < \phi < 0.5$. The resolution is defined as the RMS of the residual between the fit and the simulated true particle track parameters [9].

<table>
<thead>
<tr>
<th>Layout</th>
<th>$q/p_T$ [GeV$^{-1}$]</th>
<th>$\phi$ [rad]</th>
<th>$\eta$</th>
<th>$d_0$ [mm]</th>
<th>$z_0$ [mm]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Strip only</td>
<td>0.003</td>
<td>0.001</td>
<td>0.002</td>
<td>0.3</td>
<td>1.7</td>
</tr>
<tr>
<td>Strip + 1 pixel</td>
<td>0.003</td>
<td>0.001</td>
<td>0.001</td>
<td>0.2</td>
<td>0.3</td>
</tr>
</tbody>
</table>
3.3 Trigger Selection

The track parameters and the $\chi^2$ computed by the track fit can be used as trigger parameters. Preliminary studies on the trigger efficiency have been performed using two simple selection strategies. The first one, strategy A, is selecting the maximum $p_T$ track while the second one, strategy B, selects the maximum $p_T$ track of the two tracks with best $\chi^2$.

Figure 8 shows the background versus signal trigger efficiency for events triggered by the muon and electromagnetic triggers. The signal is represented by single muons (left) and electrons (right) as described before, while the background is simulated by muons from $b$-jets and jets respectively, with the same $p_T$ distribution as expected by the L0 system (MU20 and EM18 respectively). The muon seeded trigger reaches an efficiency of almost 98 % while rejecting 80 % of the background. The electromagnetic seeded trigger reaches close to 93 % efficiency while rejecting 80 % of the background. Strategy B performs better than strategy A in both cases. By using more advanced strategies even better results are expected.

![Graph showing signal vs. background efficiency for muon and electromagnetic triggers.](image)

Figure 8: Signal efficiency vs. background efficiency when the track trigger is seeded by muons (left) and by the electromagnetic calorimeter trigger (right). The data point labels show the $p_T$ cut applied in GeV [5].

4 Summary and Outlook

ATLAS will use a single-level hardware trigger, running at a maximum rate of 1 MHz, based on muon and calorimeter information. The trigger can, with increasing luminosity or if new trigger demands arise, evolve into a two-level trigger with L1Track providing regional tracking at a rate up to 4 MHz. In the single-level trigger case the regional track trigger, here called EFTrack, will assist the Event Filter. The readout latency of the tracker is below 10 $\mu$s for both trigger scenarios, which is required by the detector systems in ATLAS to avoid saturating frontend buffers.

The regional track trigger consists of a pattern matching step that selects hits followed by a track fitting step. An efficiency of 99.5 % is reached by the pattern matching step (98.3 % for the alternative method using the Hough transform) and 99.7 % for the track fitting. Preliminary studies on the track selection shows a trigger efficiency of 98 % for a muon seeded track trigger and 93 % for a calorimeter seeded track trigger with backgrounds reduced by a factor of 5.

The regional track trigger will continue to be studied and optimised based on detailed emulation of the system. Studies of the impact of different proposed ITk layouts on the trigger performance are under way, in preparation of the technical design report due to be ready by the end of 2017.
References


